



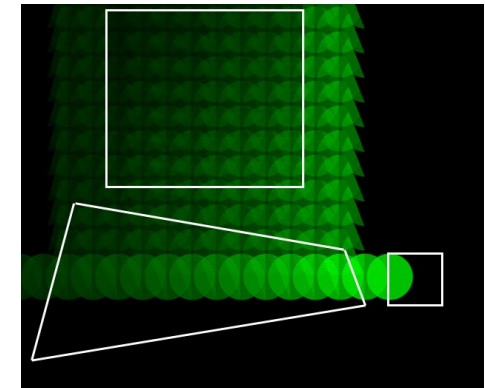
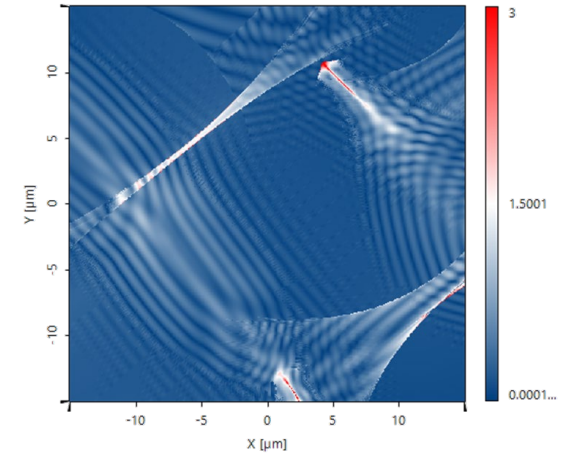
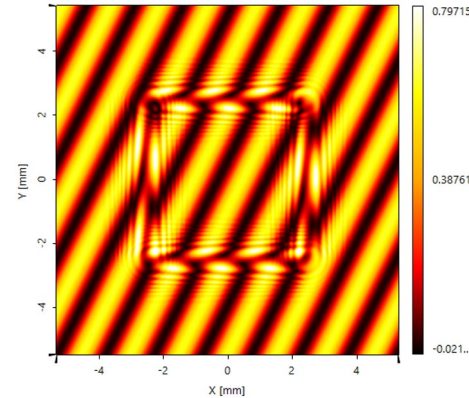
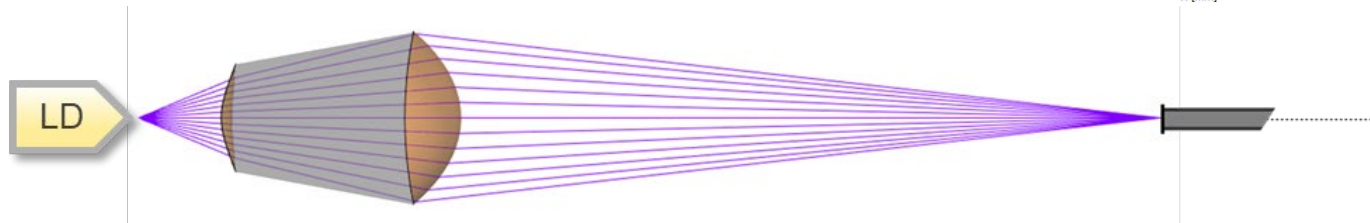
Webinar Photonics Media, 18.01.2022

Next Generation Optics Software – Trends in Technology

Frank Wyrowski

Content Overview

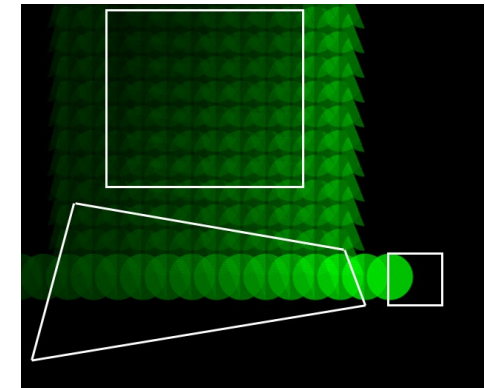
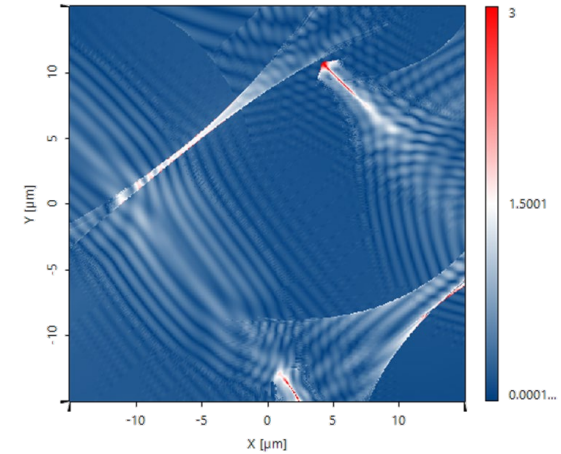
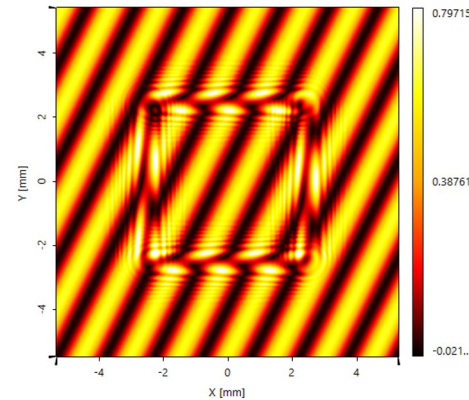
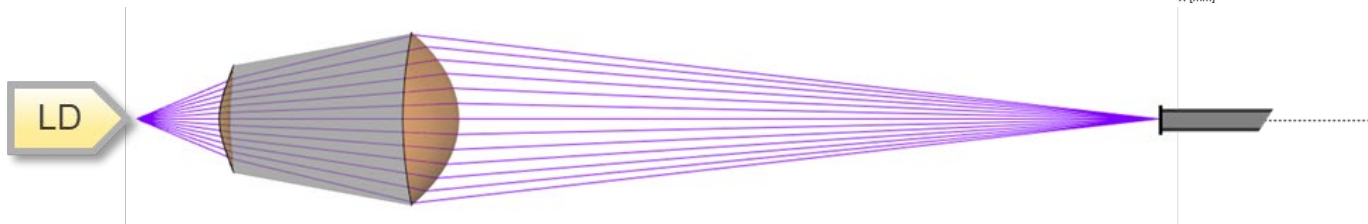
- Introduction to a unified approach in optical modeling
- Theoretical considerations on physical optics modeling
- Modeling examples
 - Talk
 - Follow-up material



Content Overview

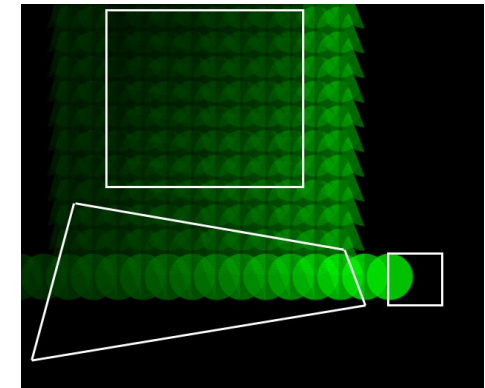
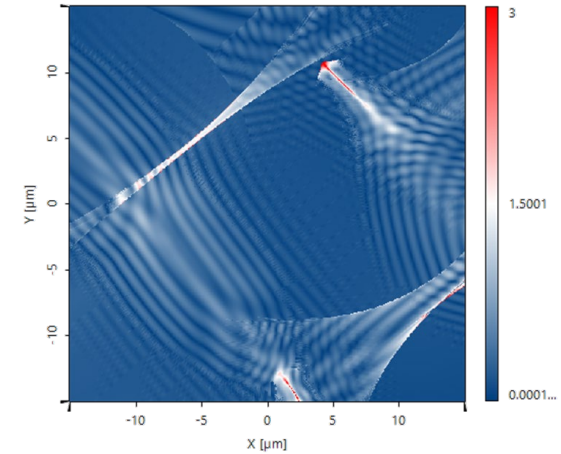
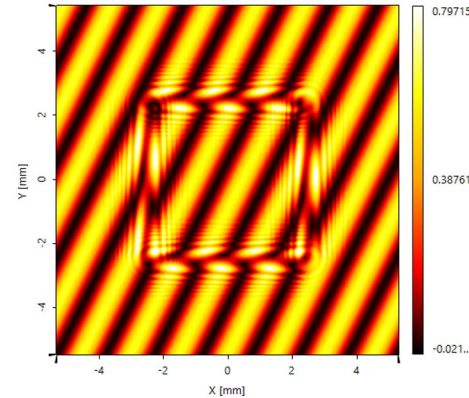
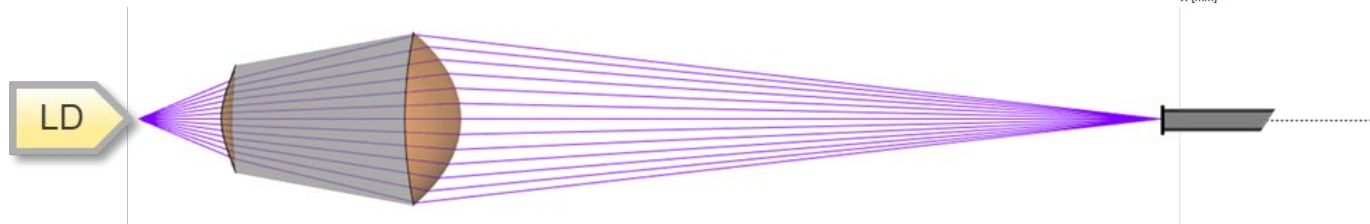
- Introduction to a unified approach
- Physical modeling
- Theoretical considerations on physical optics modeling
- Modeling examples
 - Talk
 - Follow-up material

Almost
equation free!



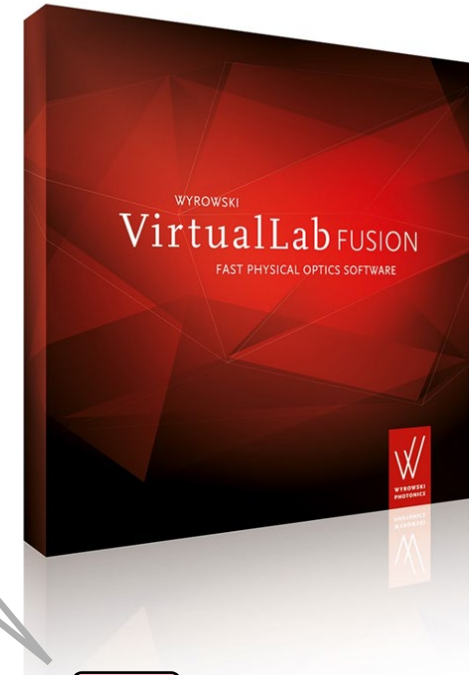
Content Overview

- **Introduction to a unified approach in optical modeling**
- Theoretical considerations on physical optics modeling
- Modeling examples
 - Talk
 - Follow-up material



VirtualLab Fusion Software

We aim to develop and apply algorithms, whose numerical complexity is linear in number of sampling points wherever possible.



Diffractive
Optics

Fast Physical Optics

1999

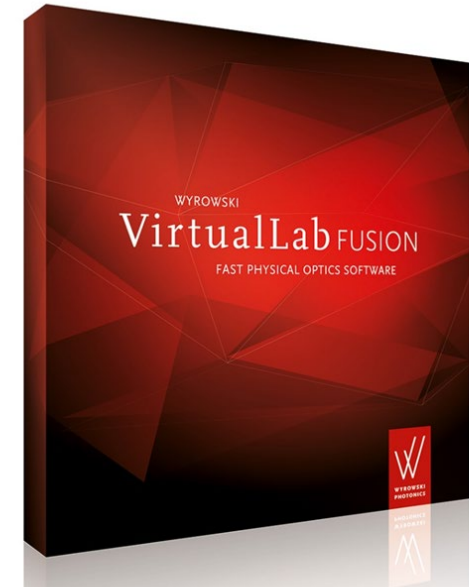
2016

2022

VirtualLab Fusion Software

All examples in the talk are done with this software.

The software is based on ideas and concepts presented in talk.



Diffractive
Optics

1999

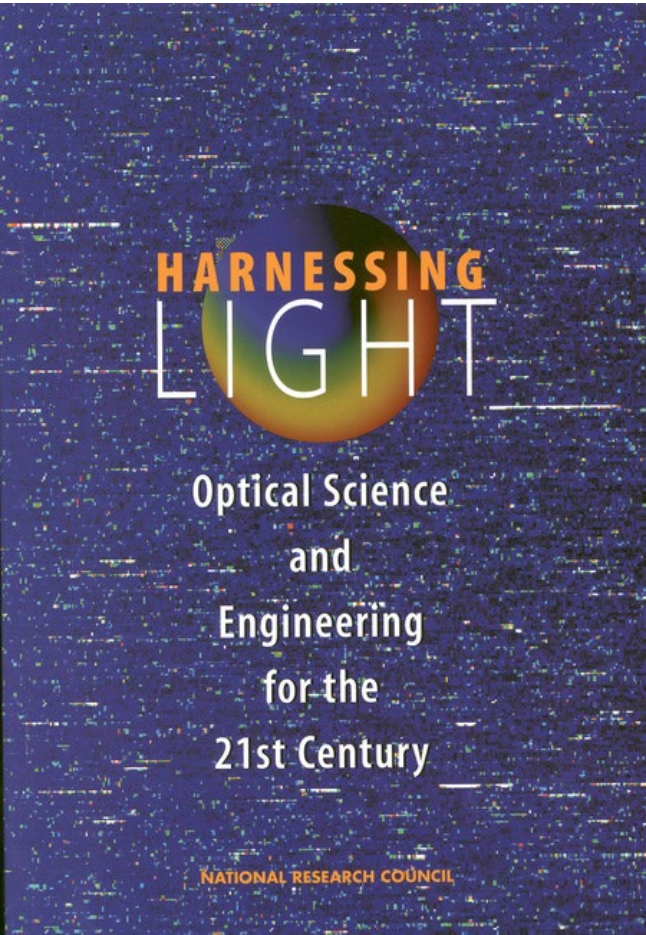
Fast Physical Optics

2016

2022

Steady
development!

Optics: A Pervasive Enabler



Harnessing Light
Optical Science and Engineering for the 21st Century

Committee on Optical Science and Engineering

Board on Physics and Astronomy

National Materials Advisory Board

Commission on Physical Sciences, Mathematics, and Applications

Commission on Engineering and Technical Systems

National Research Council

National Academy Press
Washington, D.C.
1998

1998

OVERVIEW

6

fiber-optic communications, compact disks, laser surgery of the retina, and laser welding. Other developments in optics have perhaps been less obvious, but their impact can be equally well seen in the commodities and conveniences of our world. Examples include optical lithography systems for making computer chips, high-resolution microscopes, adaptive optics for ground-based astronomy, infrared sensors for a multitude of applications, and highly efficient lighting sources. The sidebar on page 7 suggests some of the ways in which these and other optical technologies affect our everyday lives.

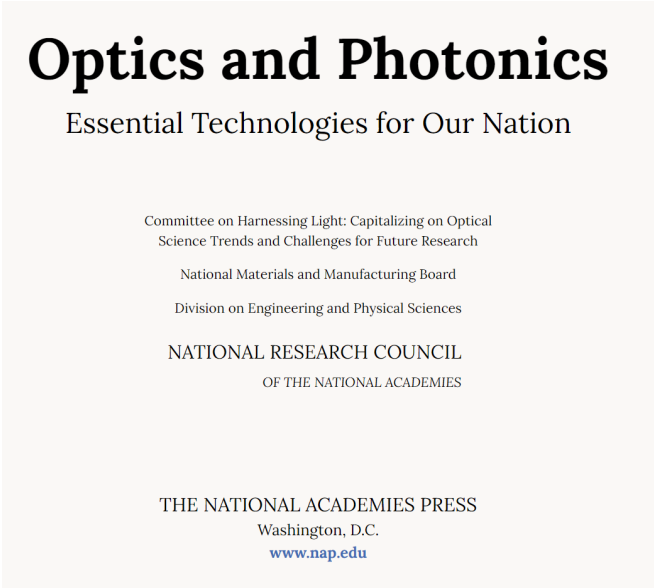
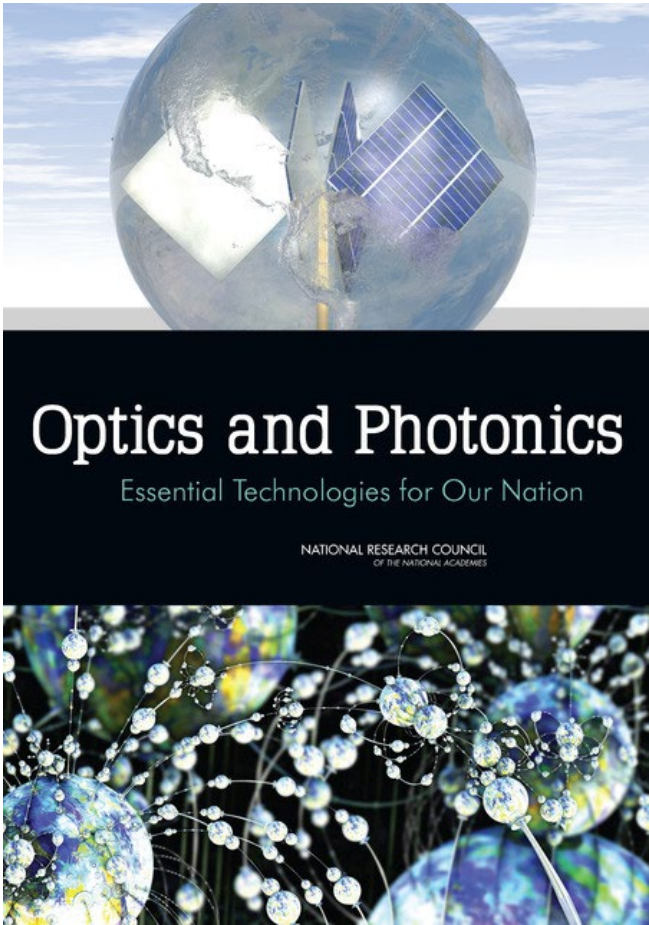
OPTICS: A PERVERSIVE ENABLER

Not surprisingly, then, optics is rapidly becoming an important focus for new businesses in the global economy. In the United States, both large and small businesses are significant players in emerging optics business activity. Optics-related companies number more than 5,000, and their net financial impact amounts to more than \$50 billion annually. More significant than this, however, is the role of optics as an *enabler*. Just as a lens in a pair of glasses enables clear vision, so an investment of a few hundred million dollars in optical-fiber technology has enabled a trillion-dollar worldwide communications revolution. A mere six laser transmitters are used in a transatlantic undersea telephone transmission system that can carry 40 million simultaneous conversations. The cost of the lasers is a tiny fraction of the cost of the system or the revenue it generates, but without them the system would be useless. Indeed, in his report to Congress on July 22, 1997, Federal Reserve chairman Alan Greenspan alluded to this enabling role: "We may be observing ... a number of key technologies, some even mature, finally interacting to create significant new opportunities for value creation. For example, the applications for the laser were modest until the later development of fiber optics engendered a revolution in telecommunications."

As another instance, a compact disk player incorporates hundreds of intricate electronic and mechanical parts, all working together and all absolutely dependent on a single laser costing less than a dollar to illuminate the spinning disk. The following pages contain dozens of additional examples. Often, perhaps even usually, those who developed the enabling optical technologies never imagined their ultimate applications. In this report, the committee has thus sought to address the pivotal question, *How does one support and strengthen a field such as optics whose value is primarily enabling?*

The remarkable breadth of optics' enabling role is both an indicator of the field's importance and a source of challenges. Virtually every

Optics and Photonics: Enabling Technology



2013

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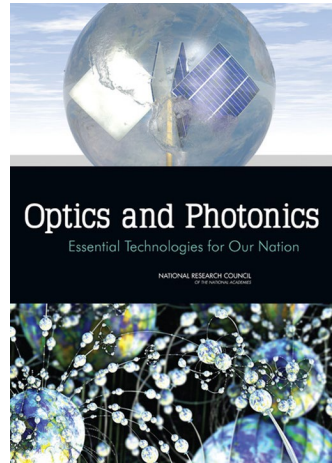
Optics and Photonics: Essential Technologies for Our Nation

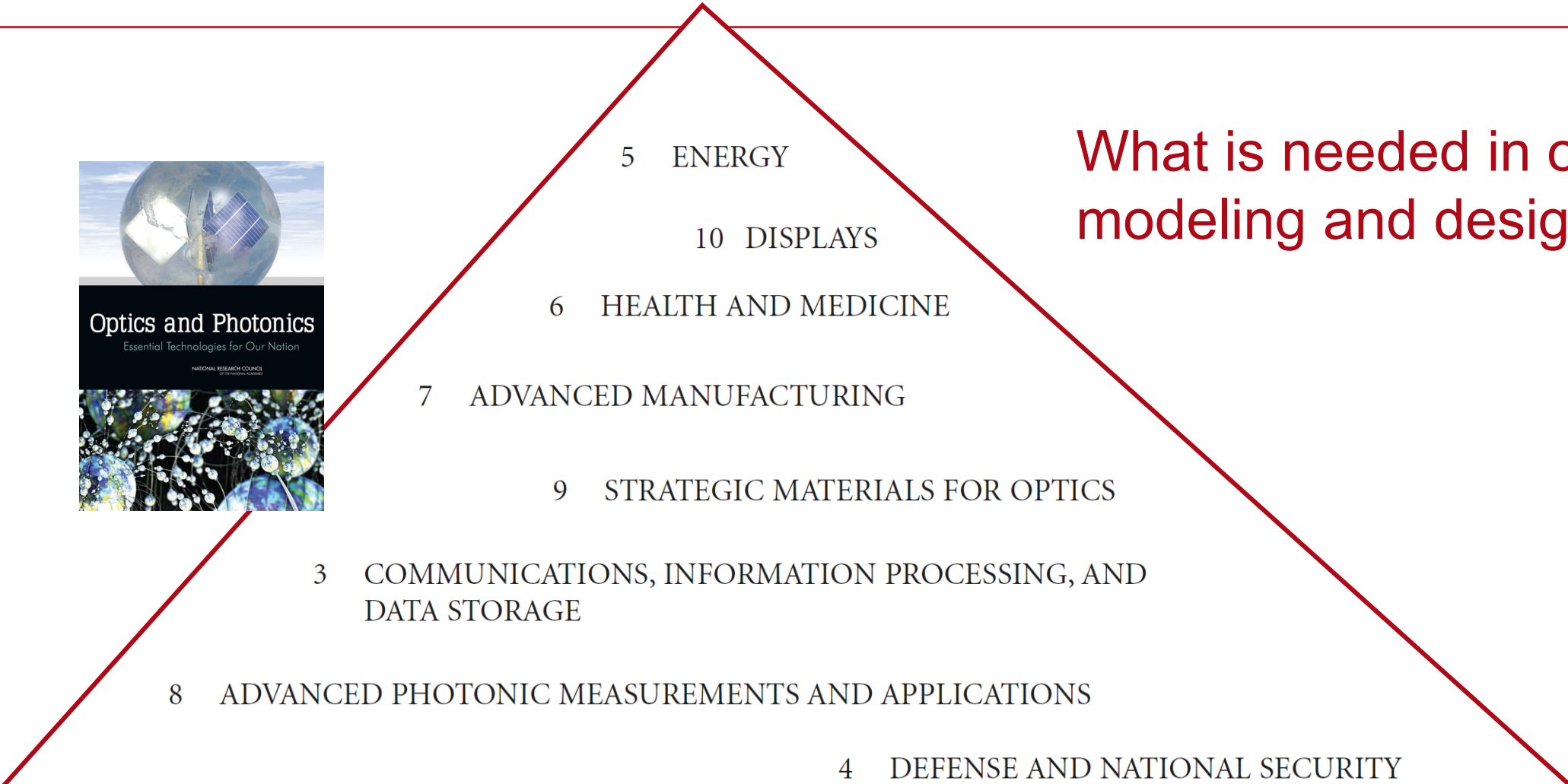
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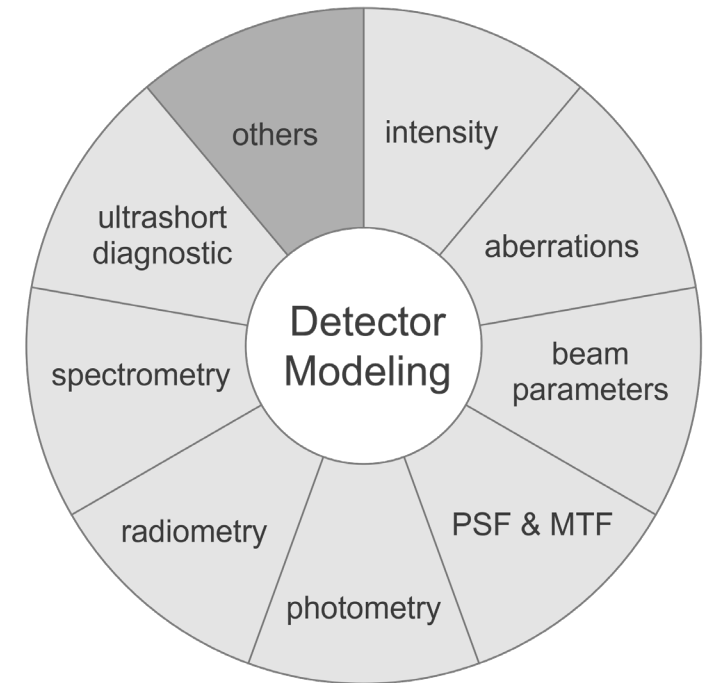
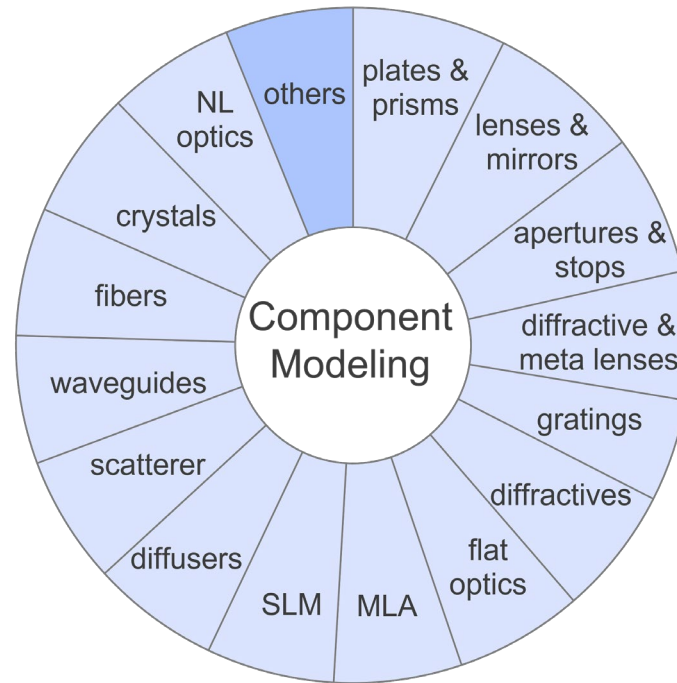
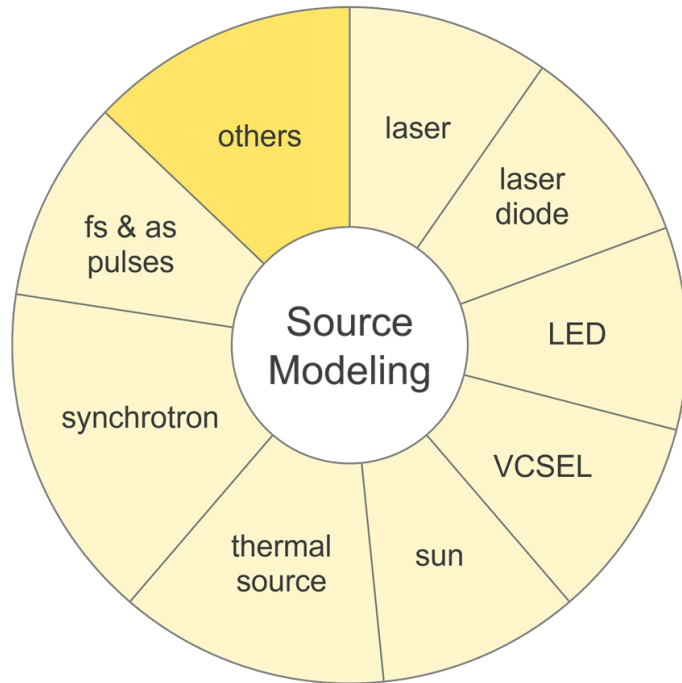
Optics and Photonics: Enabling Technology



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- 5 ENERGY
- 10 DISPLAYS
- 6 HEALTH AND MEDICINE
- 7 ADVANCED MANUFACTURING
- 9 STRATEGIC MATERIALS FOR OPTICS
- 3 COMMUNICATIONS, INFORMATION PROCESSING, AND DATA STORAGE
- 8 ADVANCED PHOTONIC MEASUREMENTS AND APPLICATIONS
- 4 DEFENSE AND NATIONAL SECURITY

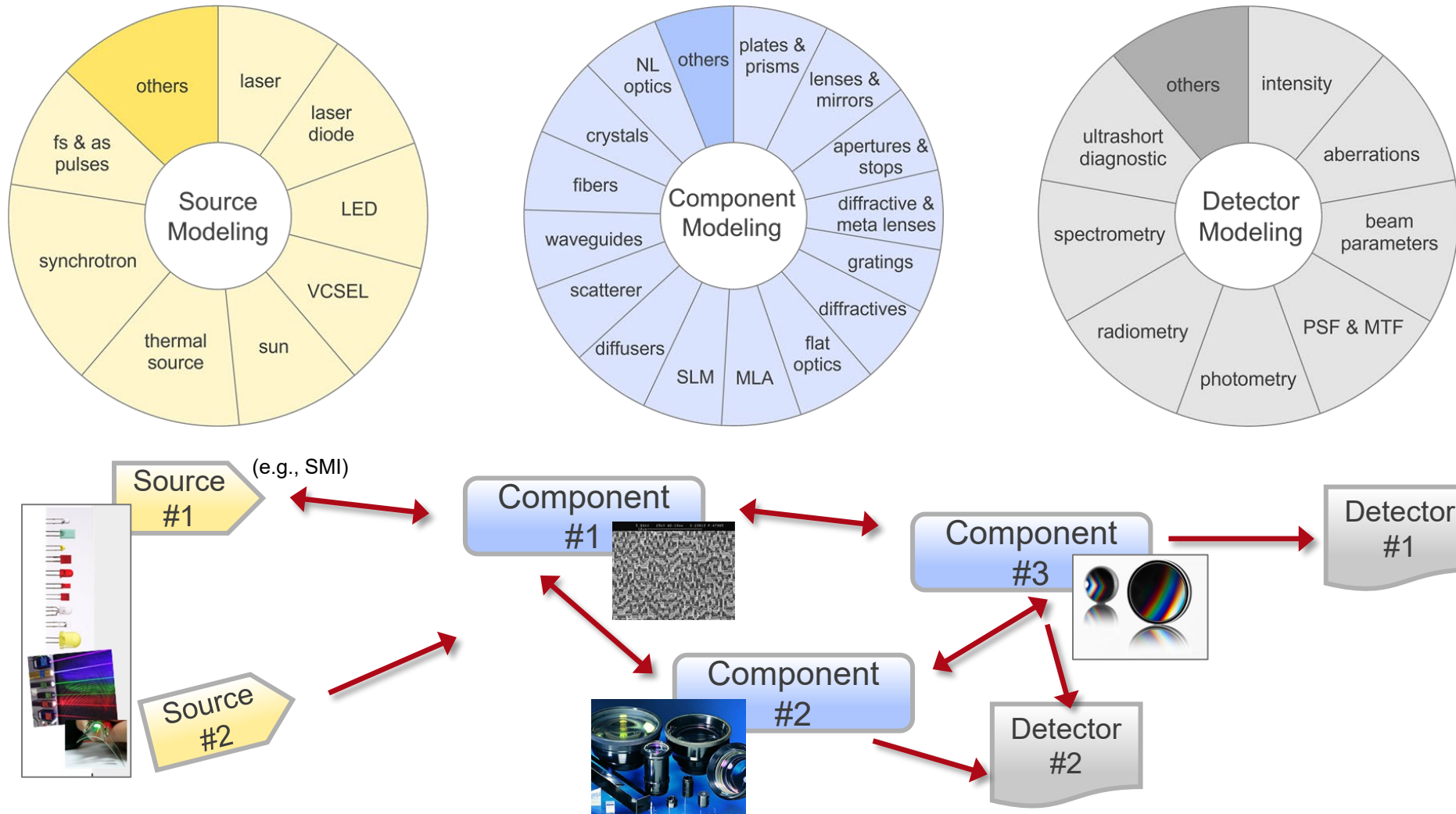
What is needed in optical modeling and design?

Sources, Components, and Detectors

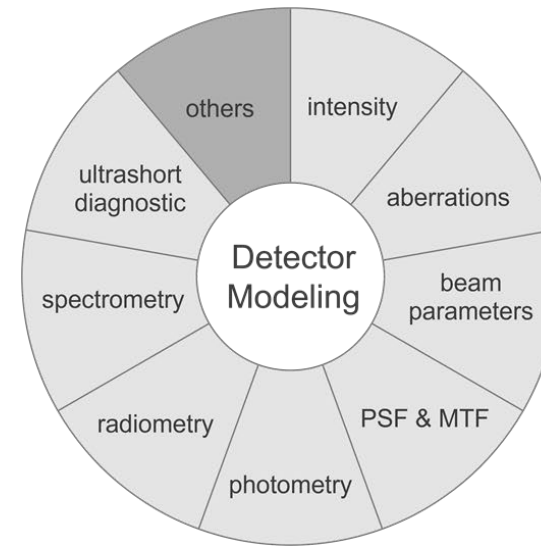
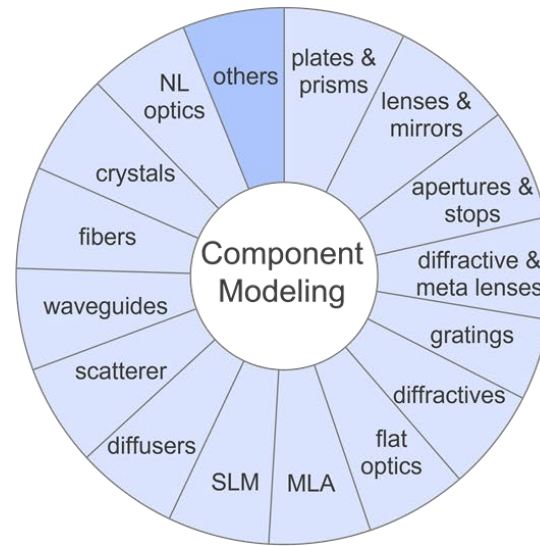
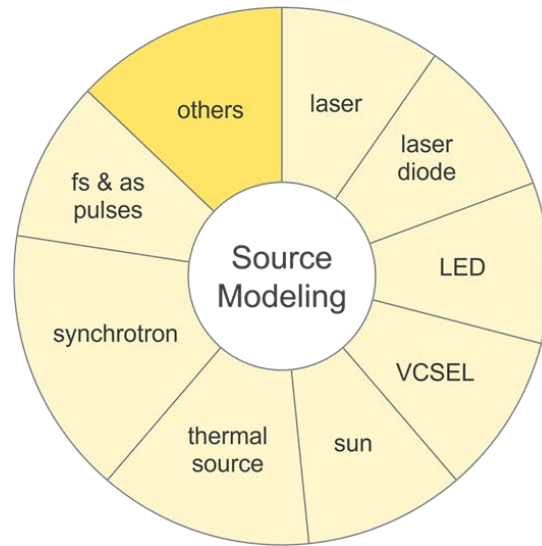


Optics as enabling technology requires maximum flexibility in source, component and detector modeling.

System Modeling and Design



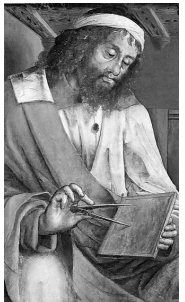
System Modeling and Design: Digital Twin (Optics & Photonics)



What theories and technologies can be used for modeling and design?

Geometrical and Physical Optics

- Geometrical (ray) optics is very powerful in optical modeling and design in a wide range of applications.
 - Comment: Special connection to physical optics is essential for PSF/MTF calculation in lens design.
- Geometrical optics dominates optical modeling and design in theory, practice, and software products.
- Physical optics provides solutions beyond geometrical optics, because ...



Euclid of Alexandria
(c. 325 BC – 265 BC)

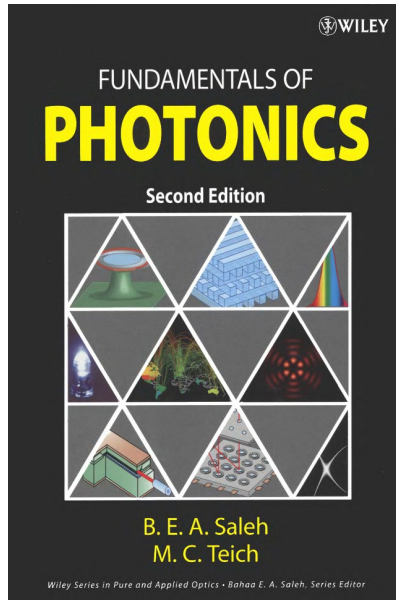
Pierre de Fermat
(1601 - 1665)



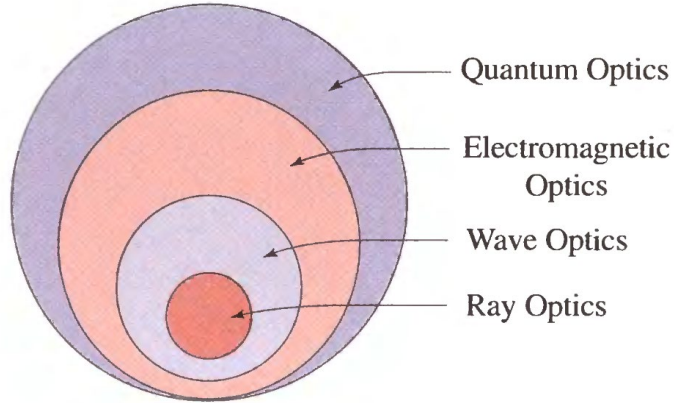
James Clerk Maxwell
(1831 – 1879)



... Physical Optics Includes Geometrical Optics



Page 2



Euclid of Alexandria
(c. 325 BC – 265 BC)

Pierre de Fermat
(1601 - 1665)

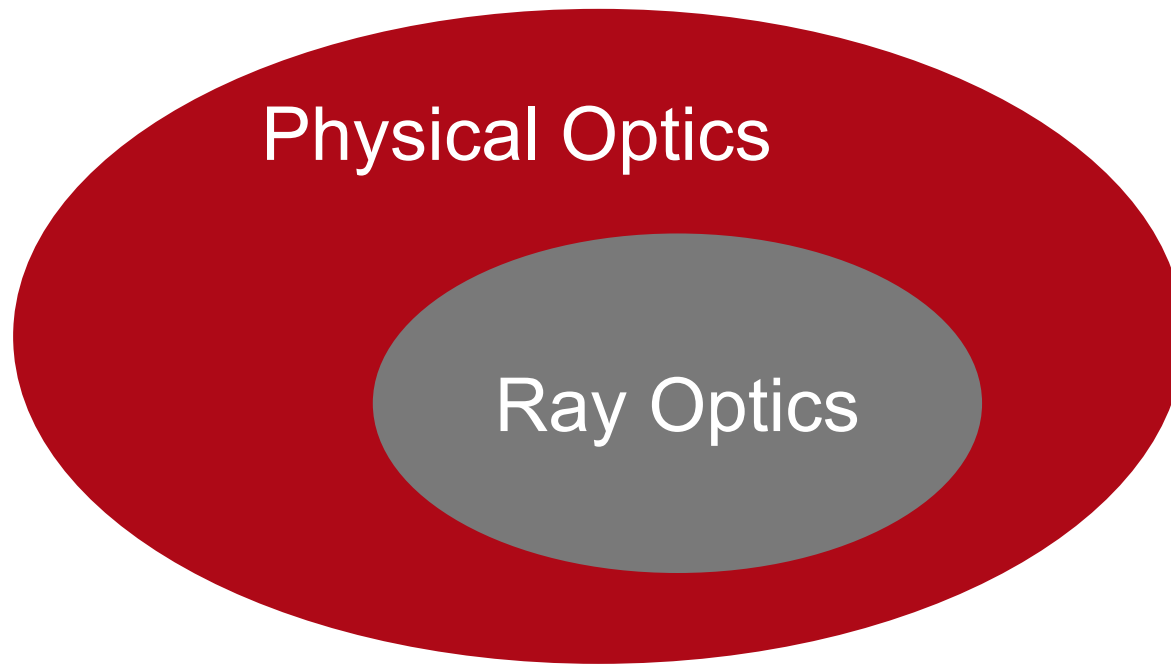


James Clerk Maxwell
(1831 – 1879)

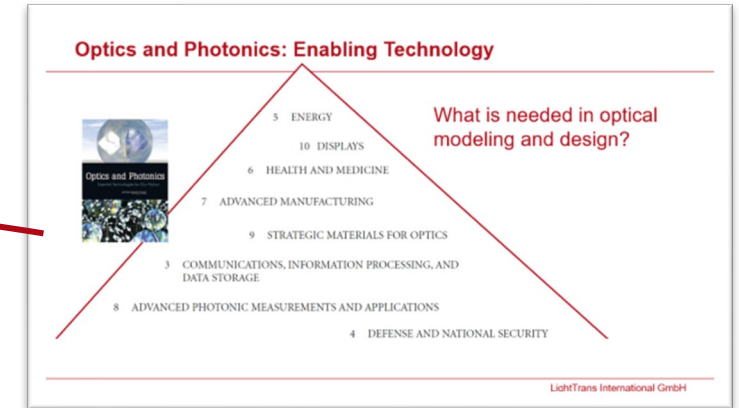
Physical Optics

Geometrical Optics

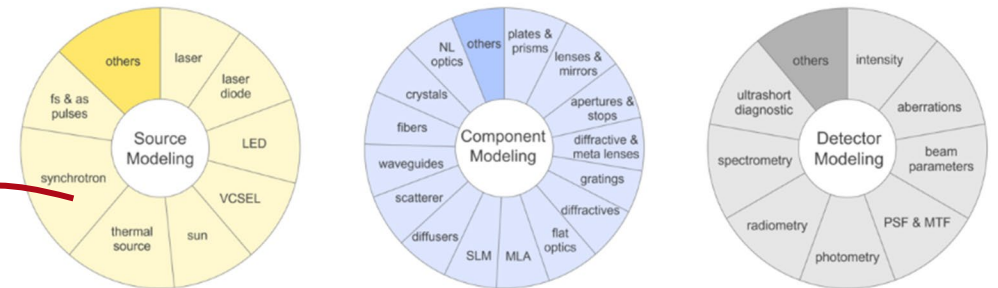
Physical Optics Includes Geometrical Optics



- Physical optics provides the needed flexibility in optical modeling and design.
- But this fact has no strong practical consequences yet.



Sources, Components, and Detectors



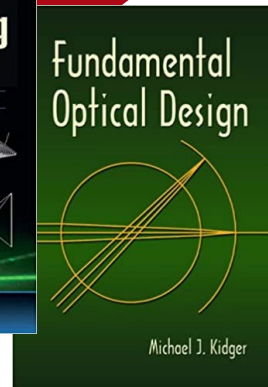
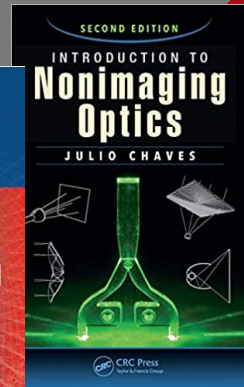
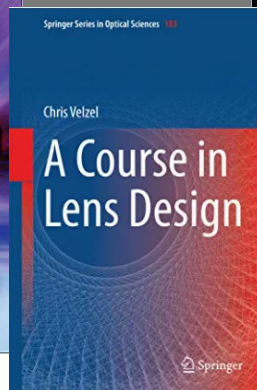
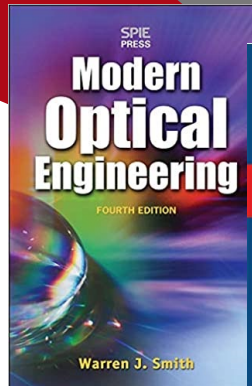
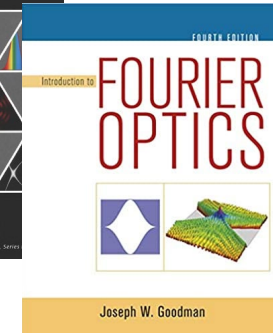
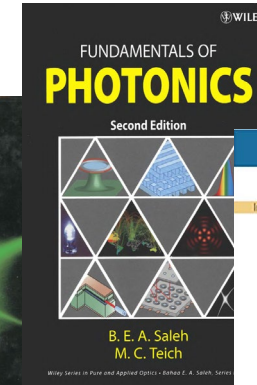
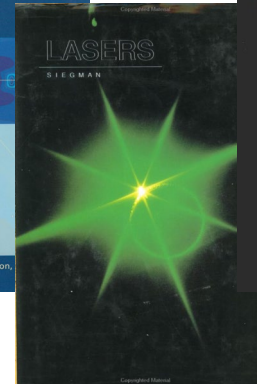
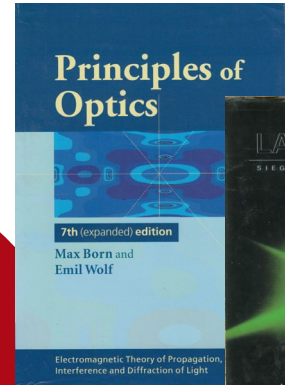
Optics as enabling technology requires maximum flexibility in source, component and detector modeling.

LightTrans International GmbH

Physical and Geometrical Optics: Theory

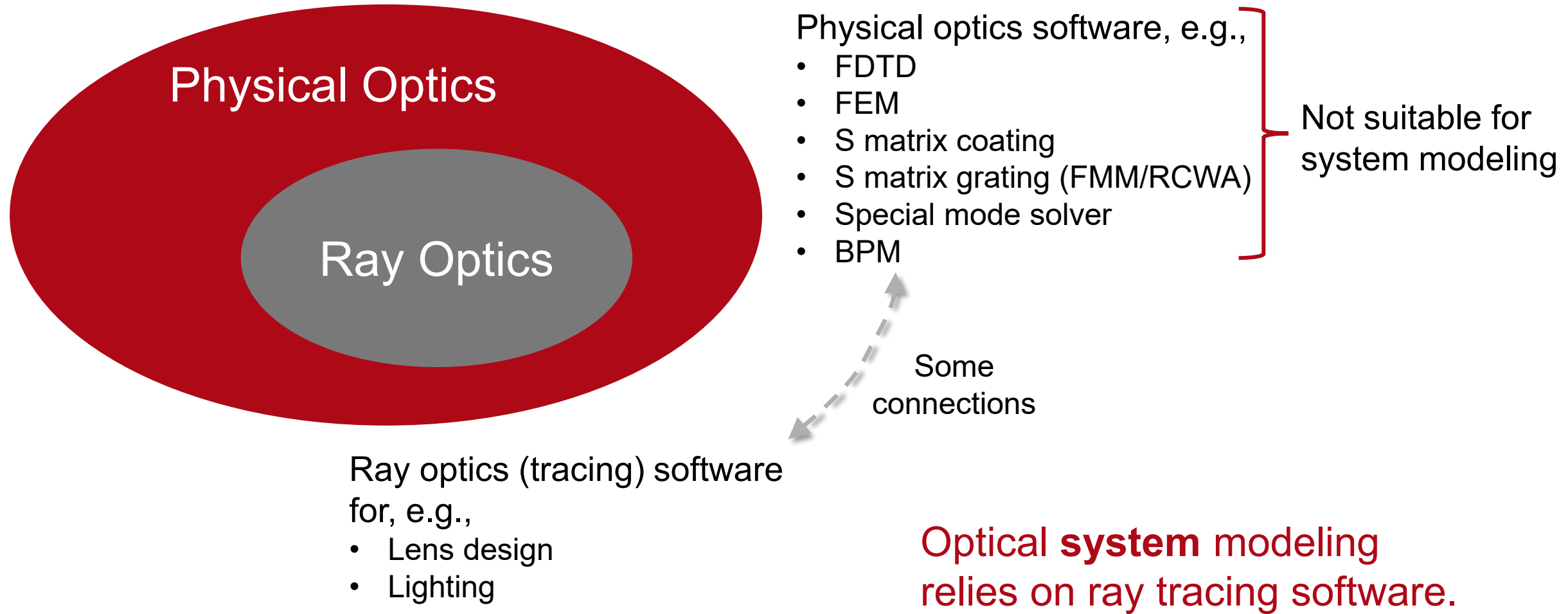
Physical Optics

Ray Optics

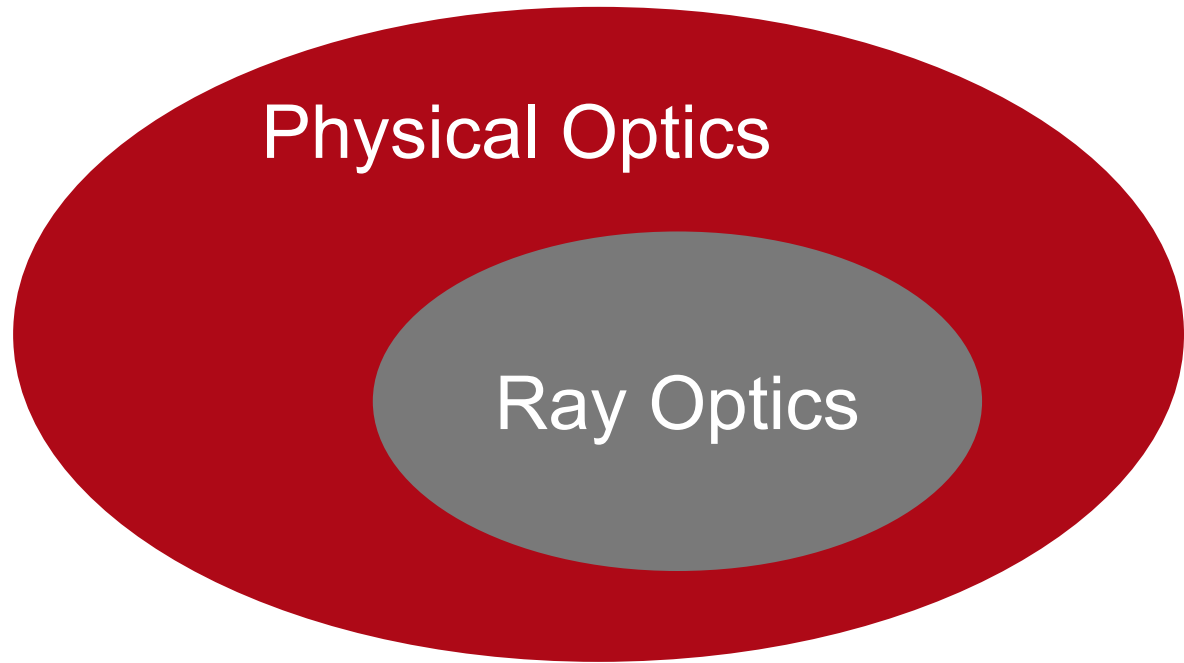


The connection between geometrical and physical optics is almost not visible.

Physical and Geometrical Optics: Practice



Physical and Geometrical Optics: Practice



Ray optics (tracing) software for, e.g.,

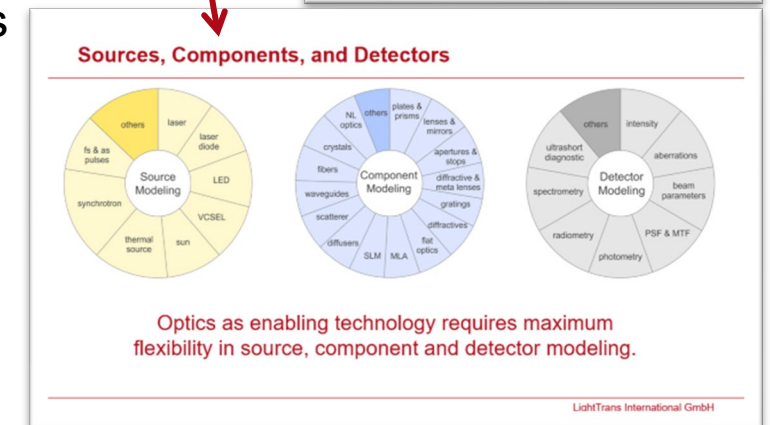
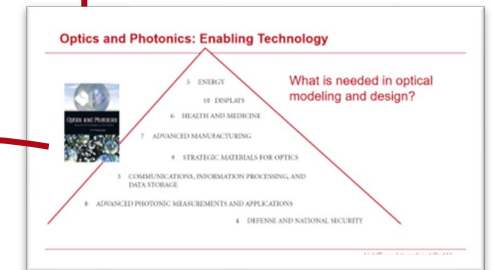
- Lens design
- Lighting

Physical optics software, e.g.,

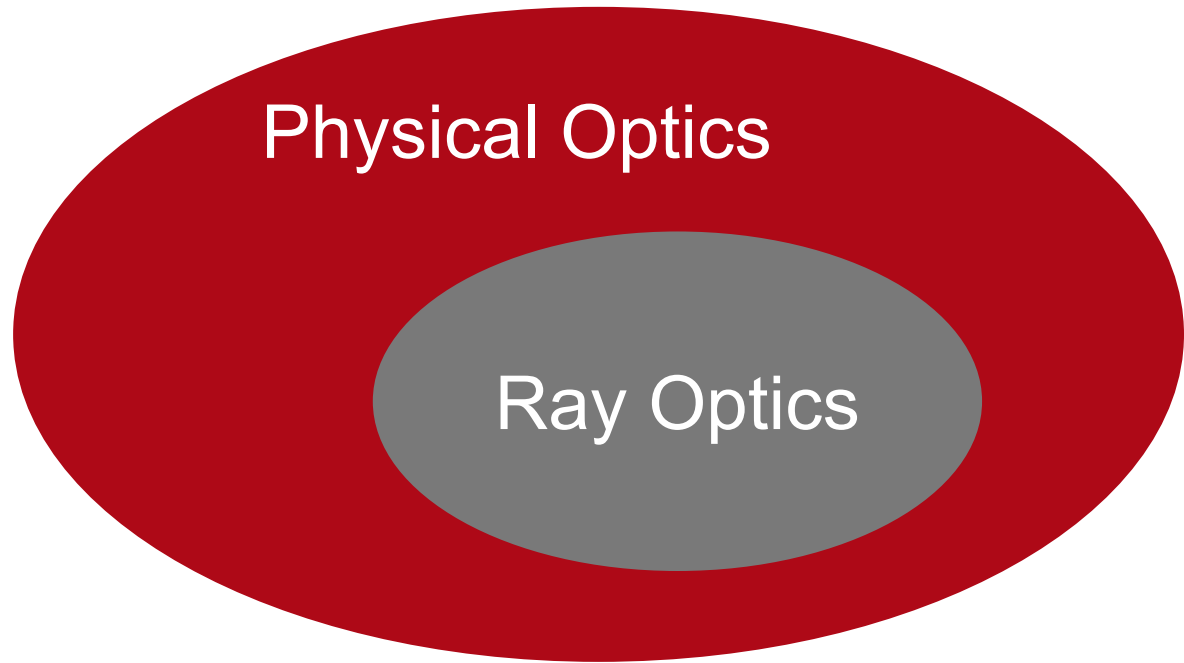
- FDTD
- FEM
- S matrix coating
- S matrix grating (FMM/RCWA)
- Special mode solver
- BPM

Not suitable for system modeling

Some connections



Physical and Geometrical Optics: Demand



Current situation:

- Geometrical and physical optics coexist without a powerful connection in theory and practice.
- Some design tasks apply specialized connections, e.g., PSF/MTF calculation in lens design.

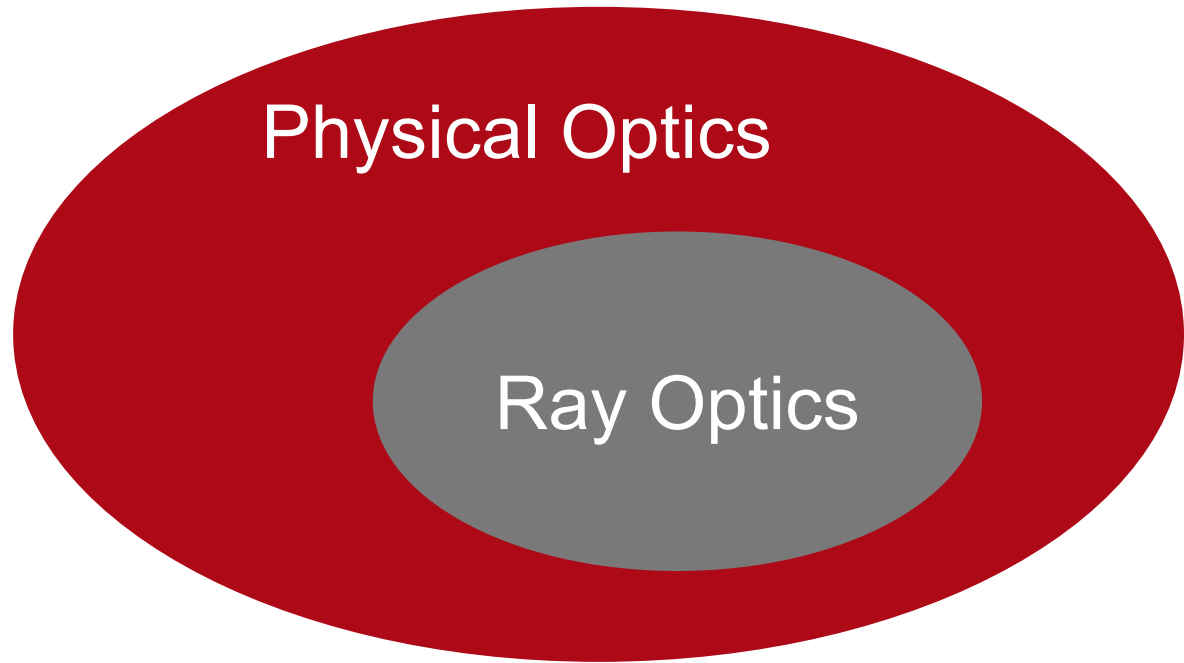


Demand:

- Seamless transition between geometrical and physical optics in theory and practice.

Is that a reasonable demand?

Physical and Geometrical Optics: Light Representation



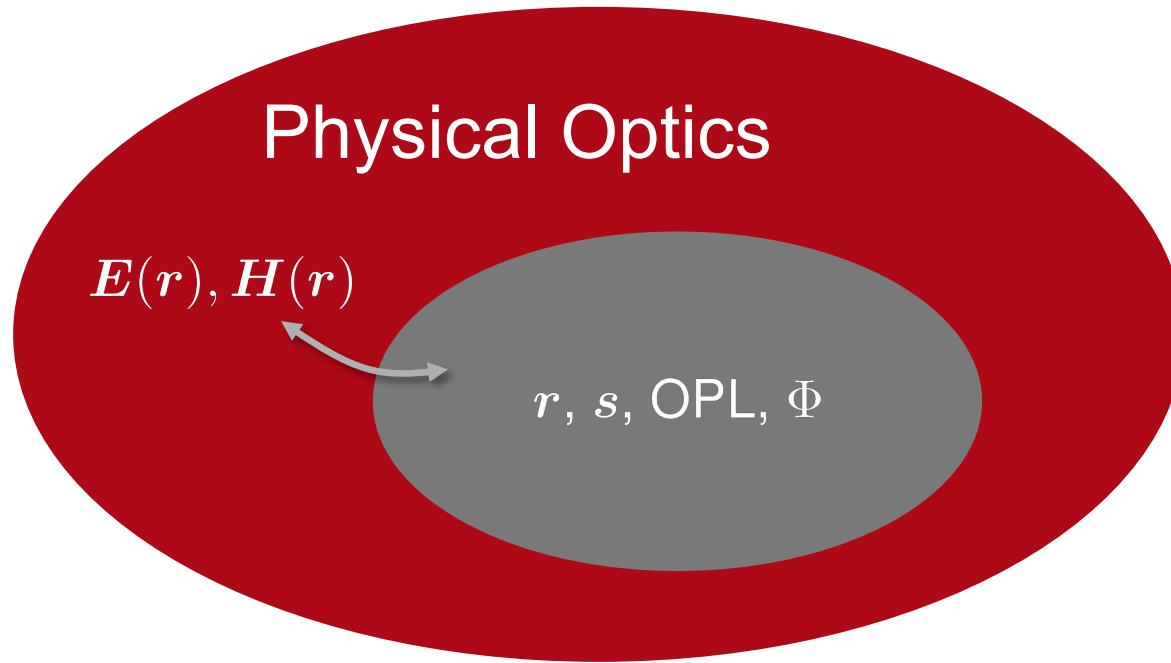
- Light representation in physical optics:
 $\mathbf{E}(\mathbf{r}) = (E_x(\mathbf{r}), E_y(\mathbf{r}), E_z(\mathbf{r}))$ and
 $\mathbf{H}(\mathbf{r}) = (H_x(\mathbf{r}), H_y(\mathbf{r}), H_z(\mathbf{r}))$
- Light representation in geometrical optics:
Ray position $\mathbf{r}$, direction $\mathbf{s}$, OPL, and flux Φ

Demand:

- Seamless transition between geometrical and physical optics in theory and practice.

Is that a reasonable demand?

Physical and Geometrical Optics: Light Representation



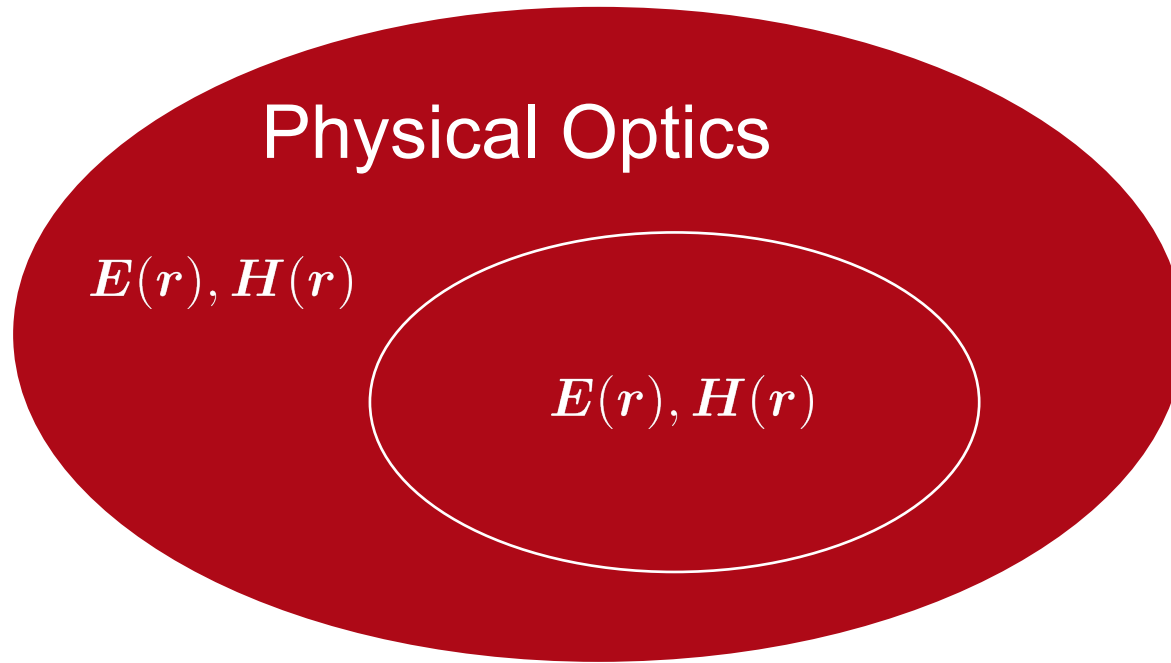
- Light representation in physical optics:
 $\mathbf{E}(\mathbf{r}) = (E_x(\mathbf{r}), E_y(\mathbf{r}), E_z(\mathbf{r}))$ and
 $\mathbf{H}(\mathbf{r}) = (H_x(\mathbf{r}), H_y(\mathbf{r}), H_z(\mathbf{r}))$
- Light representation in geometrical optics:
Ray position $\mathbf{r}$, direction $\mathbf{s}$, OPL, and flux Φ

Different light representations prevent a seamless transition between physical and geometrical optics!

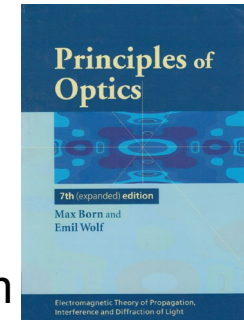


We must formulate our objective in a different way!

Physical and Geometrical Optics: Light Representation



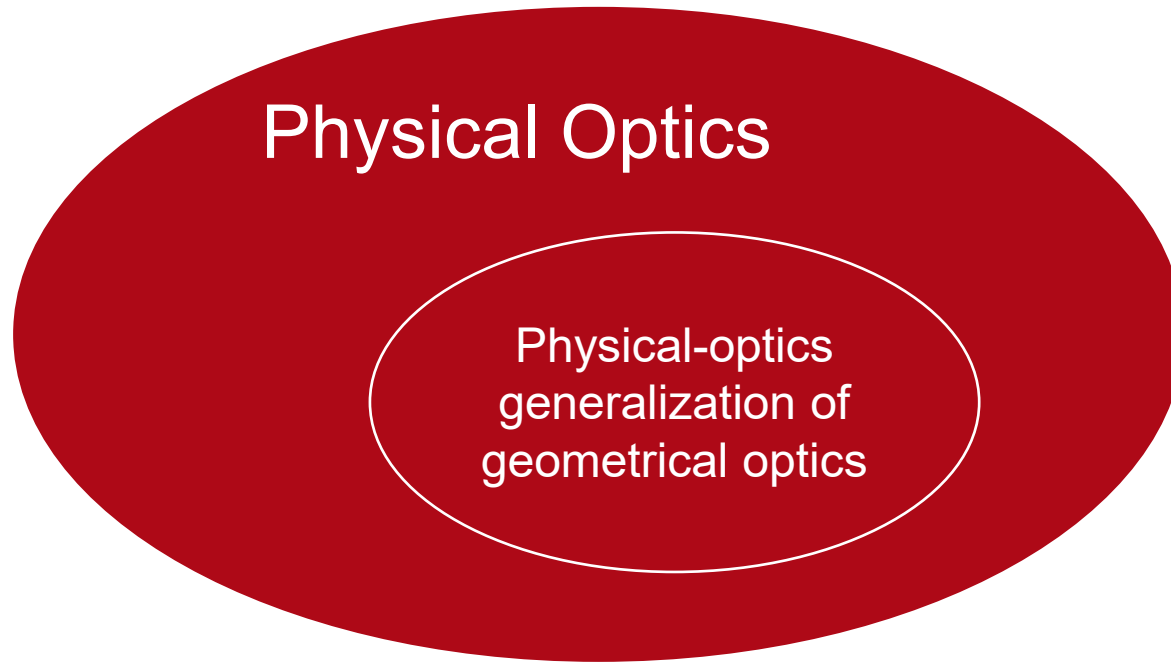
We need to identify that part of physical optics, which deals with the “***geometrical laws relating to the propagation of the 'amplitude vectors' E and H .***”



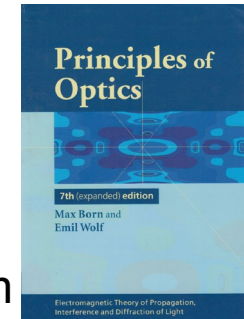
Citation from

page 125

Geometric Branch of Physical Optics

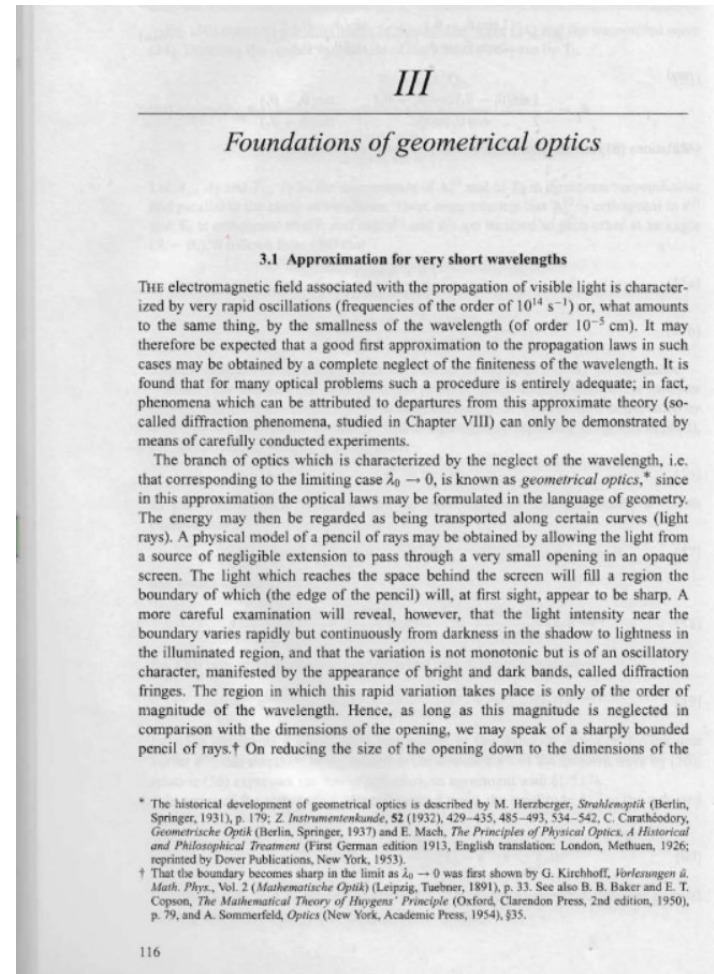
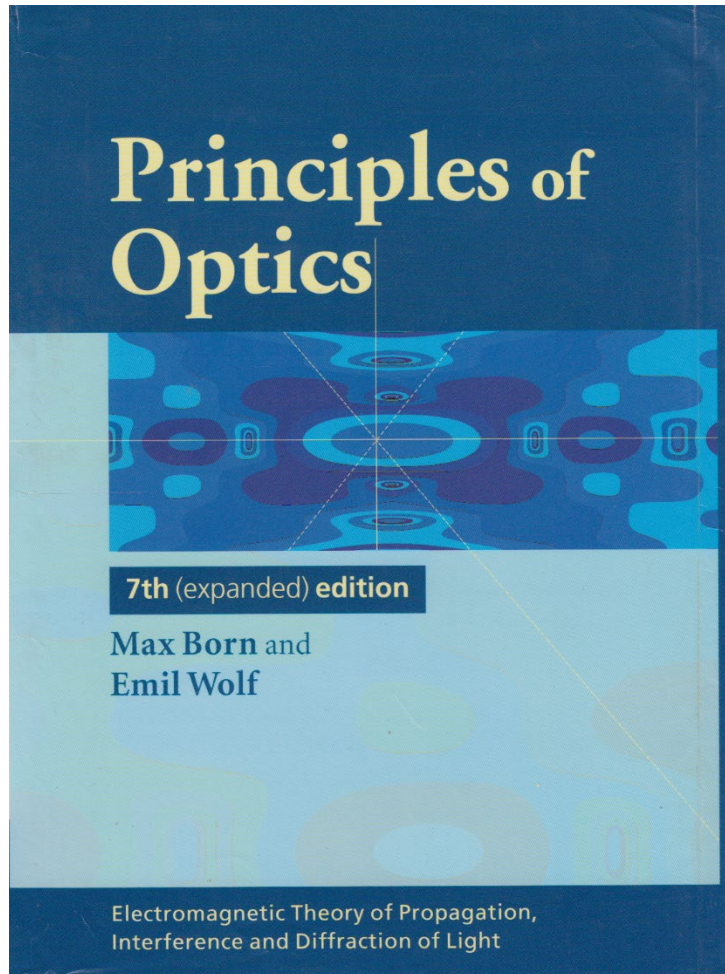


We need to identify that part of physical optics, which deals with the “***geometrical laws relating to the propagation of the 'amplitude vectors' E and H .***”

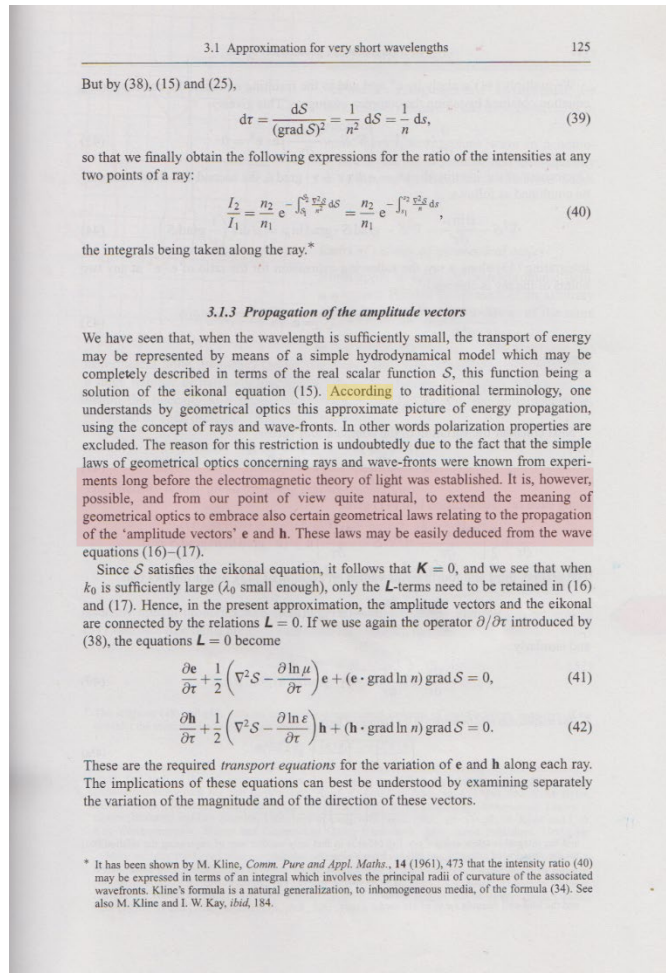


Citation from page 125

Geometric Branch of Physical Optics



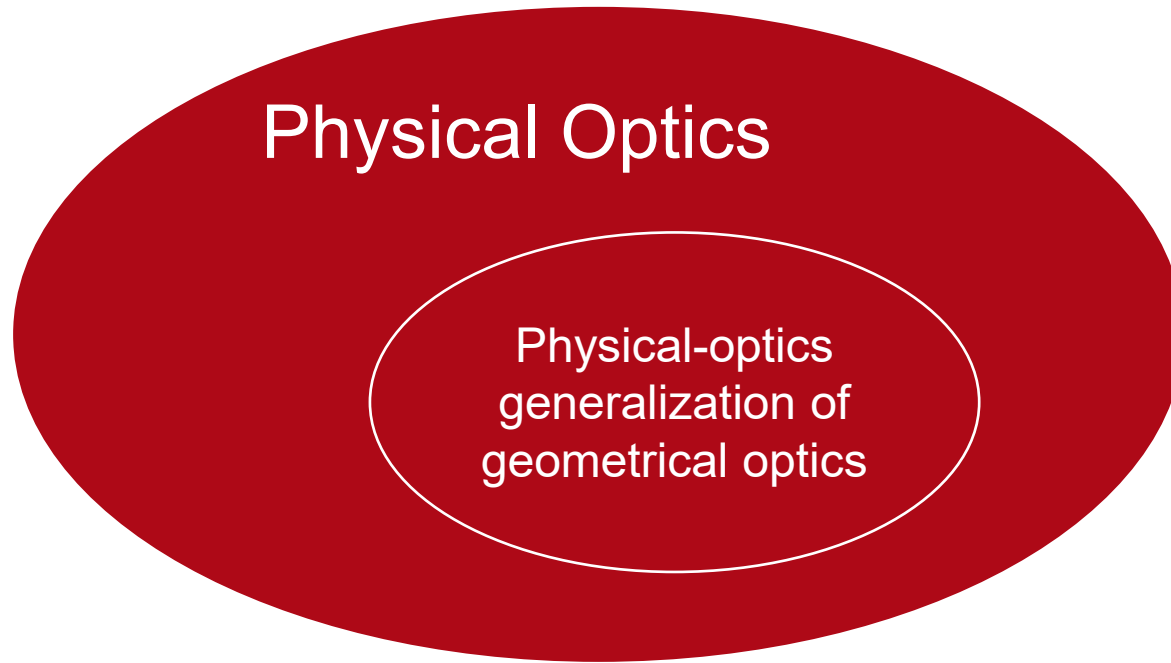
Geometric Branch of Physical Optics



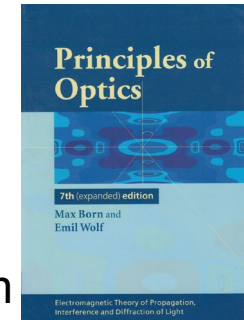
page 125

“According to traditional terminology, one understands by geometrical optics this approximate picture of energy propagation, using the concept of rays and wave-fronts. In other words polarization properties are excluded. The reason for this restriction is undoubtedly due to the fact that the simple laws of geometrical optics concerning rays and wave-fronts were known from experiments long before the electromagnetic theory of light was established. **It is, however, possible, and from our point of view quite natural, to extend the meaning of geometrical optics to embrace also certain geometrical laws relating to the propagation of the 'amplitude vectors' $\mathbf{E}$ and $\mathbf{H}$.**”

Geometric Branch of Physical Optics



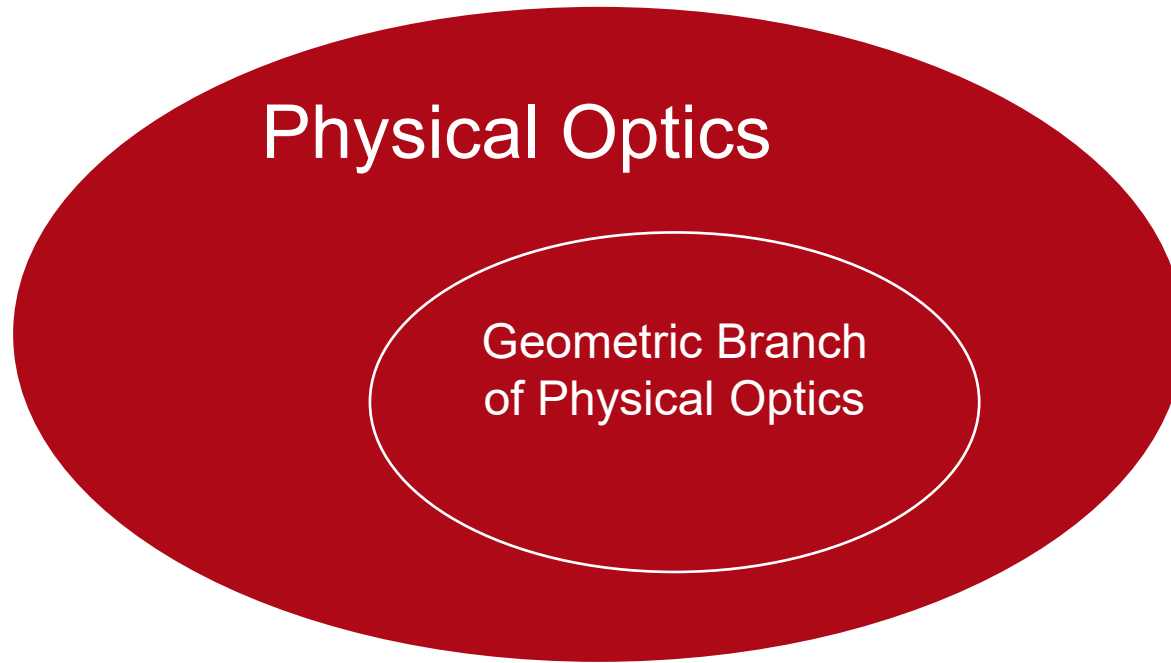
We need to identify that part of physical optics, which deals with the “***geometrical laws relating to the propagation of the 'amplitude vectors' E and H .***”



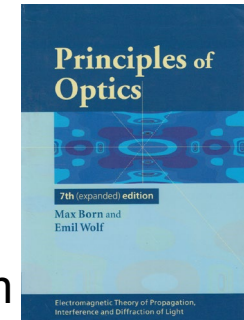
Citation from page 125

We follow Max Born's and Emil Wolf's advice!

Geometric Branch of Physical Optics



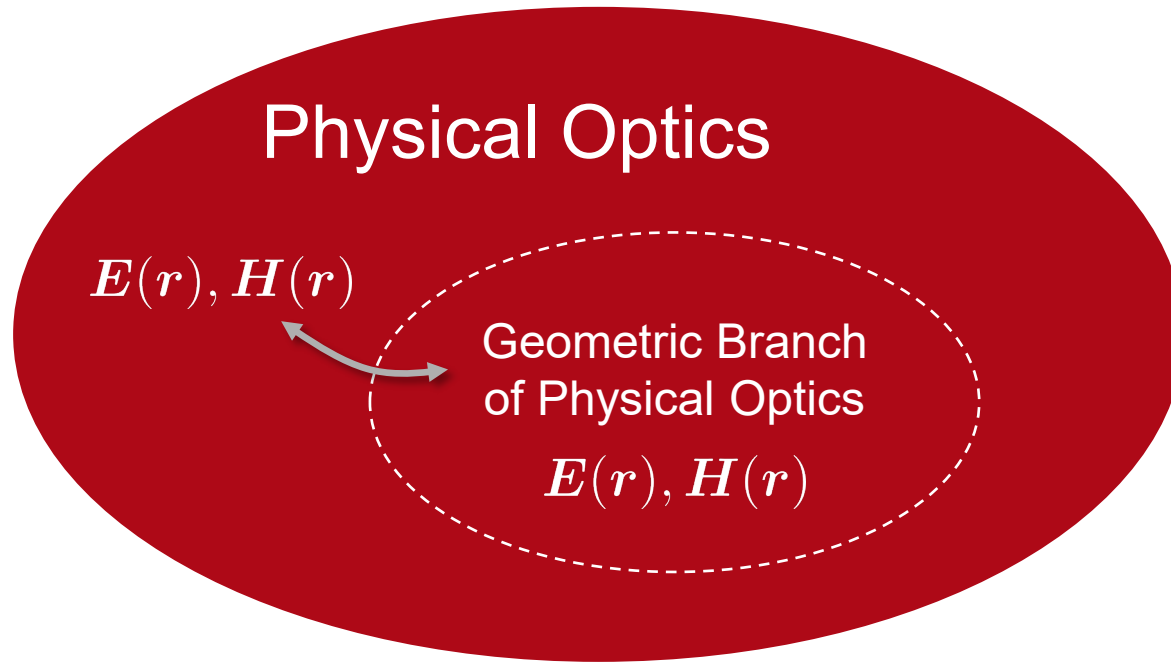
We need to identify that part of physical optics, which deals with the “***geometrical laws relating to the propagation of the 'amplitude vectors' E and H .***”



Citation from page 125

We follow Max Born's and Emil Wolf's advice!

Physical and Geometrical Optics: The Objective



Search for a seamless transition reasonable!

Current situation:

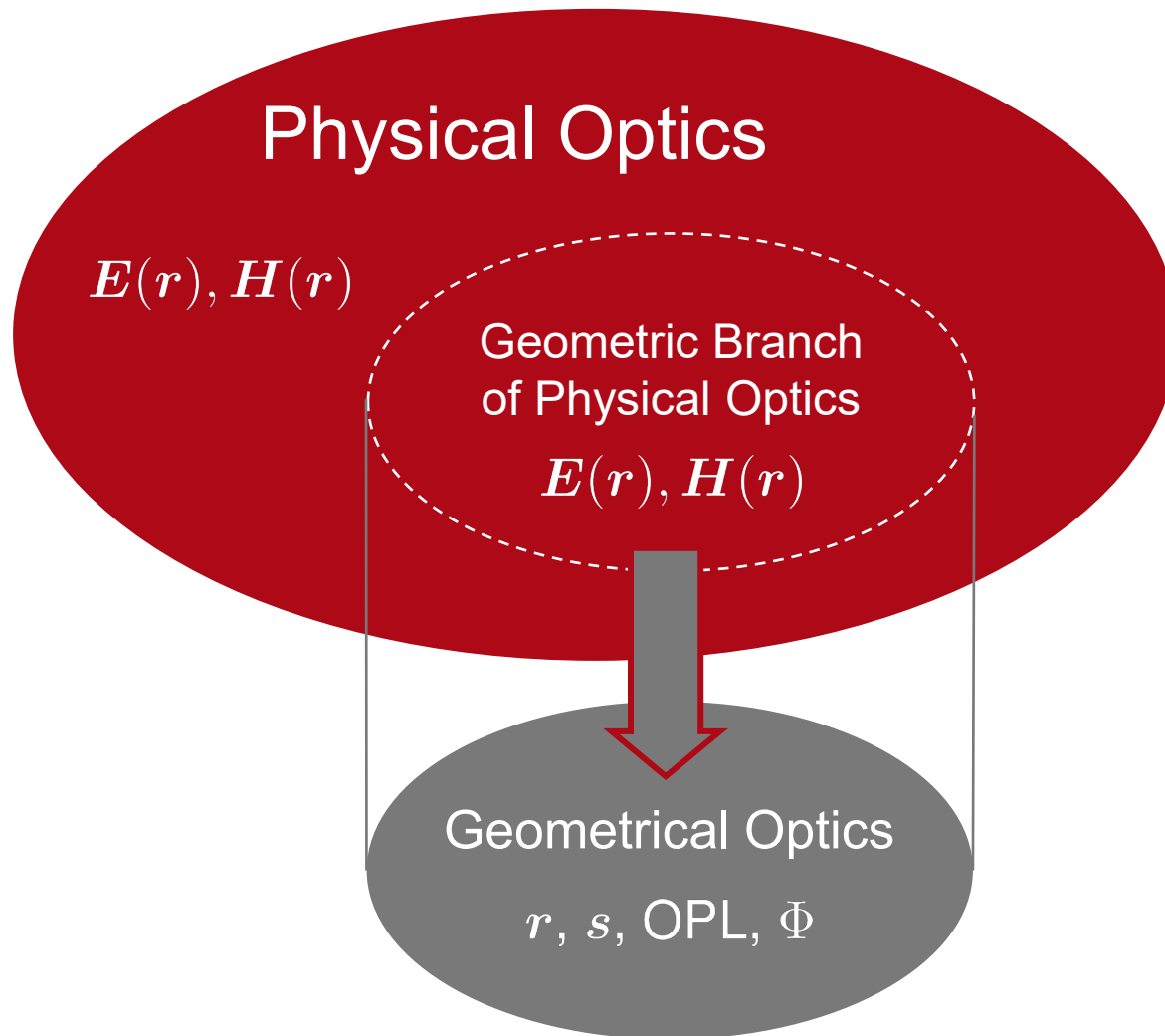
- Geometrical and physical optics coexist without a powerful connection in theory and practice.
- Some design tasks apply specialized connections, e.g., PSF/MTF calculation in lens design.



Our objective:

- Seamless transition between physical optics and its *geometric branch* in theory and practice.

Physical and Geometrical Optics: The Objective



Current situation:

- Geometrical and physical optics coexist without a powerful connection in theory and practice.
- Some design tasks apply specialized connections, e.g., PSF/MTF calculation in lens design.



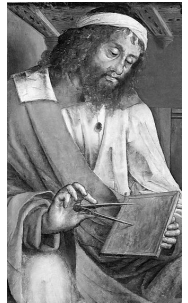
Our objective:

- Seamless transition between physical optics and its *geometric branch* in theory and practice.
- Geometrical optics follows from the geometric branch by restricting to a ray-optical light representation.

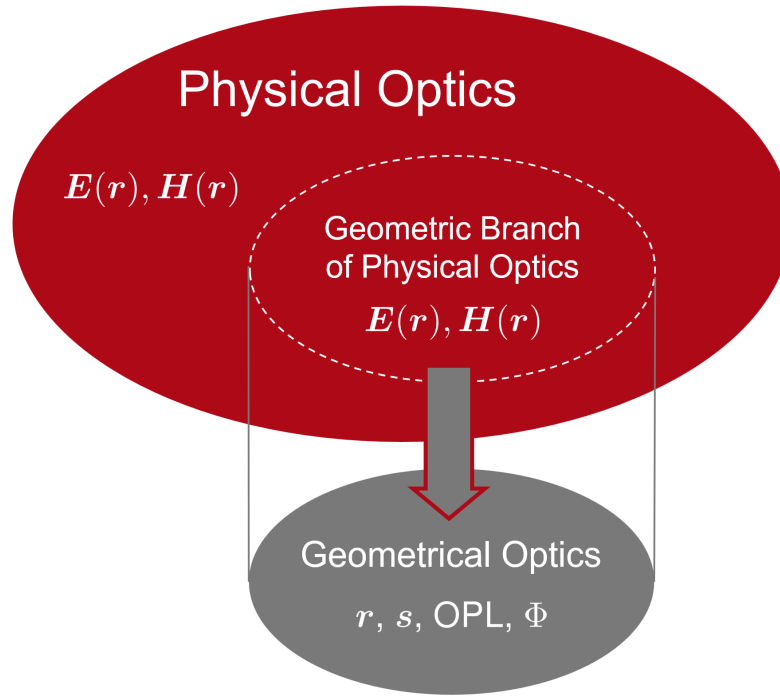
Unified Modeling: The Major Trend

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Euclid of Alexandria
(c. 325 BC – 265 BC)



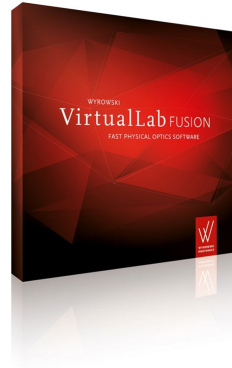
Pierre de Fermat
(1601 - 1665)



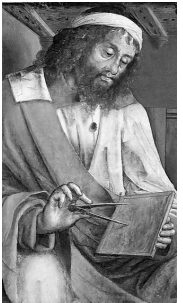
James Clerk Maxwell
(1831 – 1879)



Unified Modeling: The Major Trend



Unified modeling provides the foundation and the direction of the software development!



Euclid of Alexandria
(c. 325 BC – 265 BC)

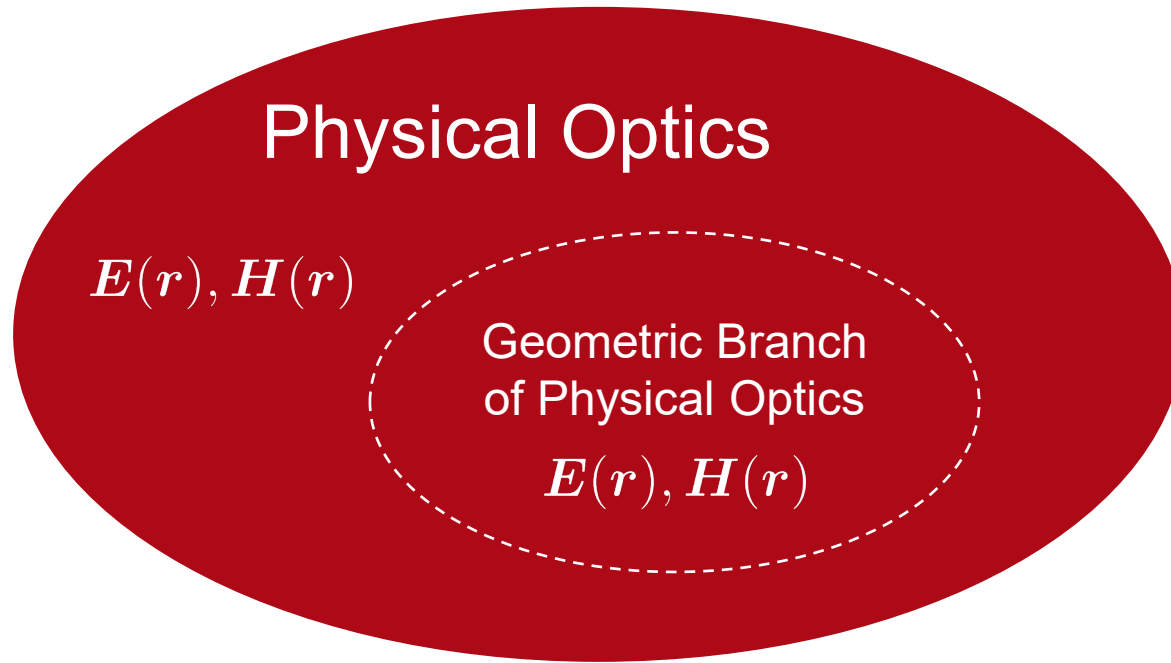
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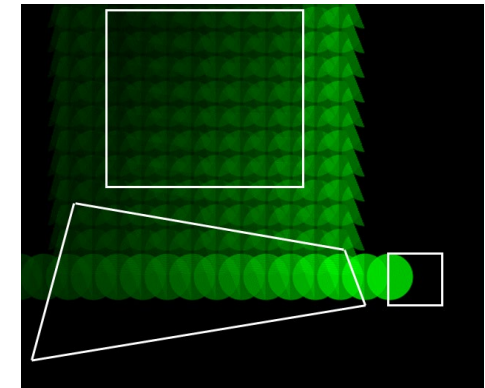
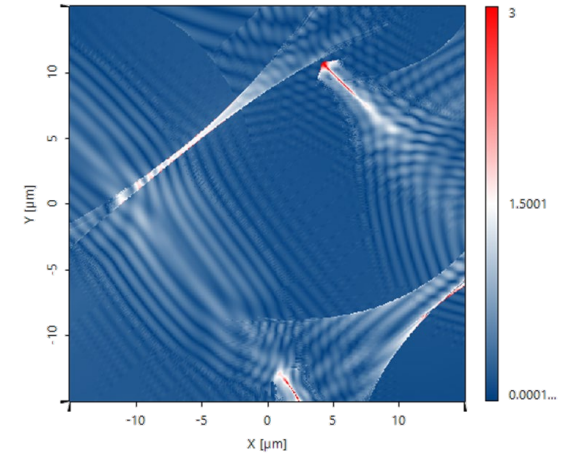
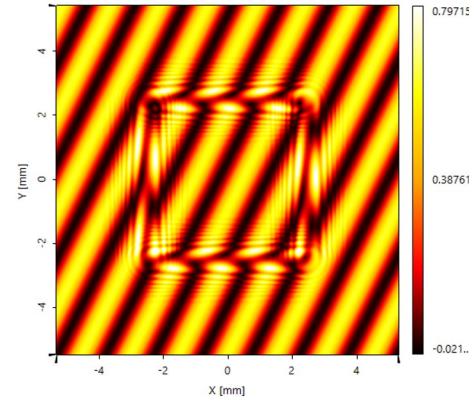
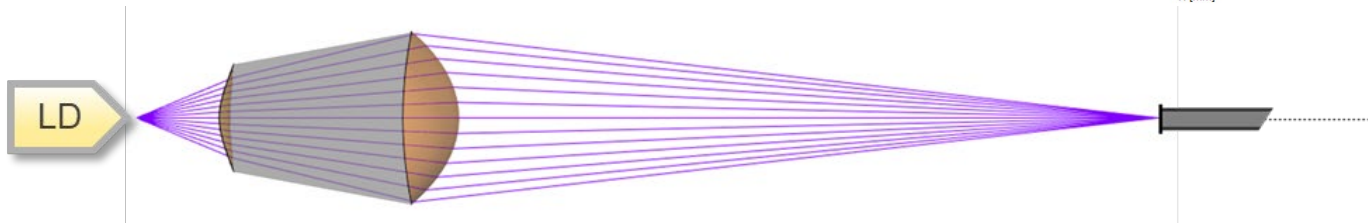
Geometric Branch of Physical Optics



How to define the
geometric branch of
physical optics?

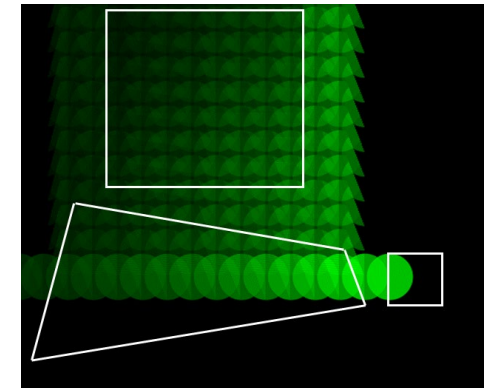
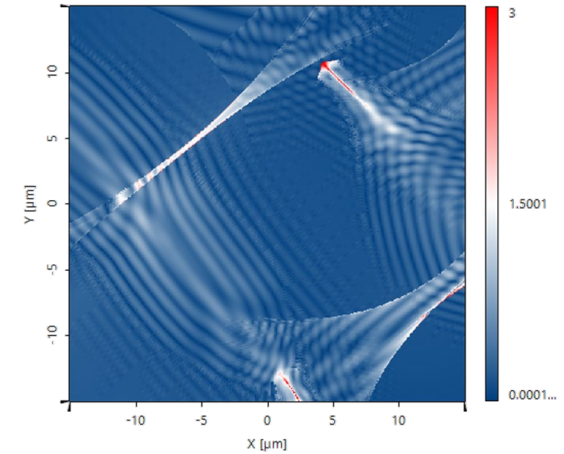
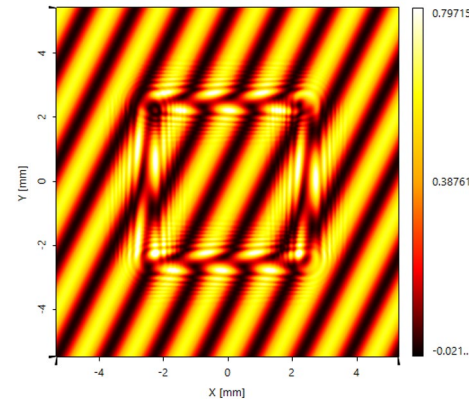
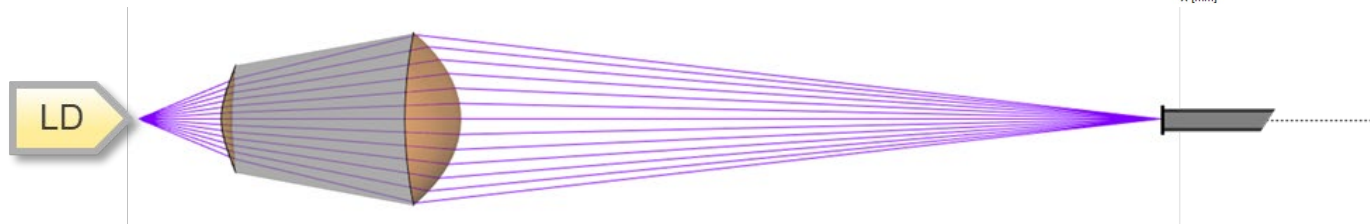
Content Overview

- **Introduction to a unified approach in optical modeling**
- Theoretical considerations on physical optics modeling
- Modeling examples
 - Talk
 - Follow-up material

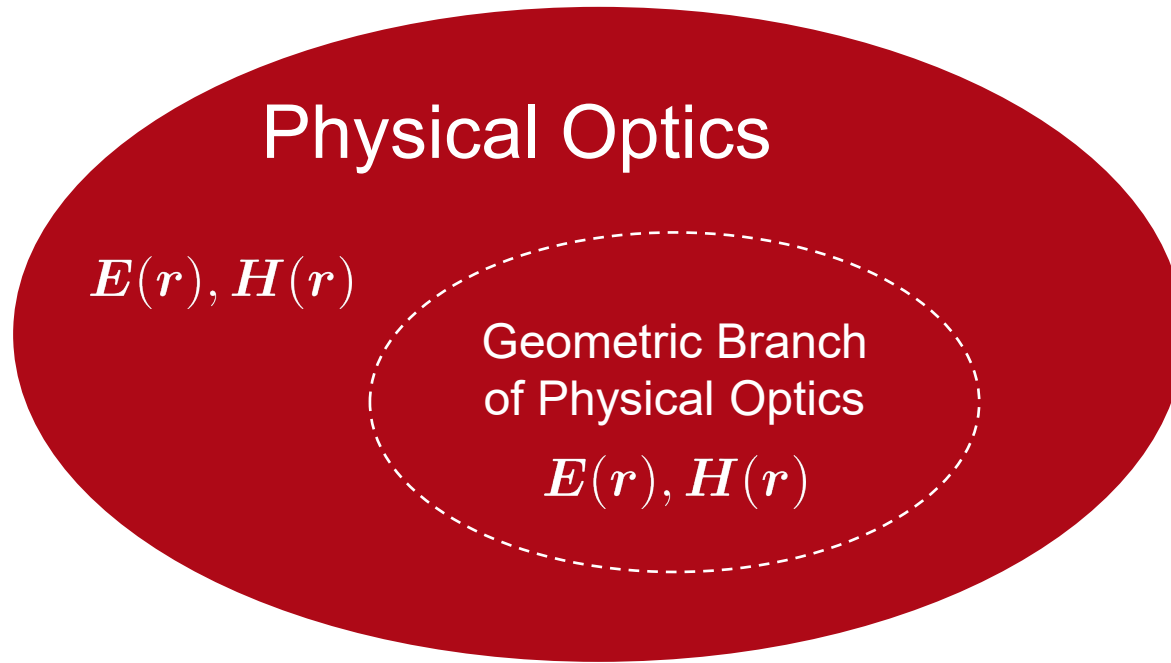


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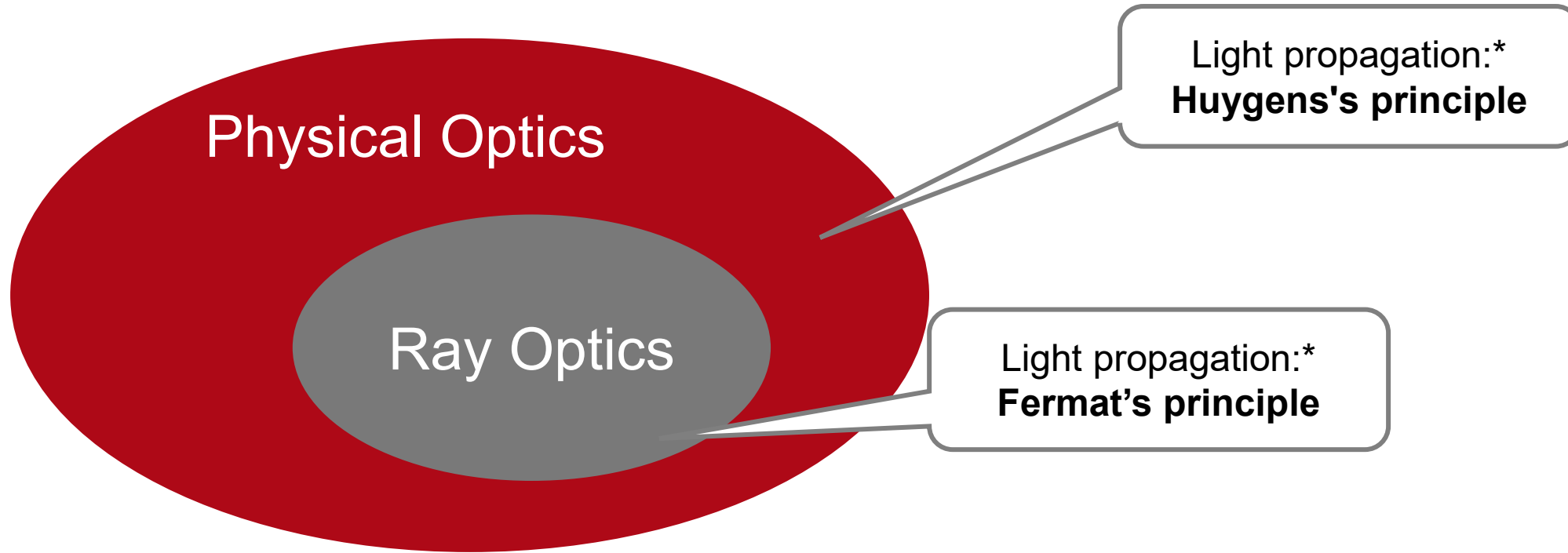


Geometric Branch of Physical Optics



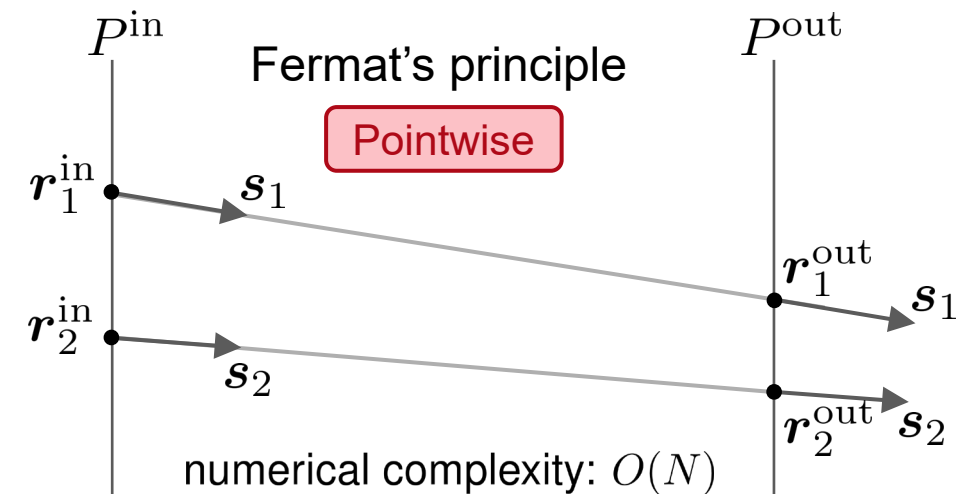
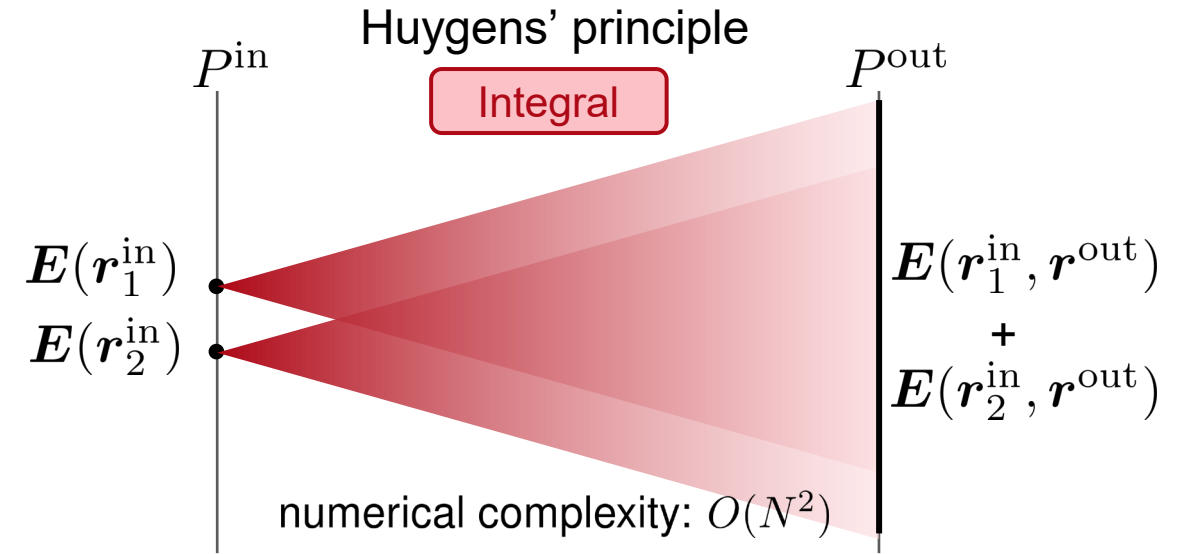
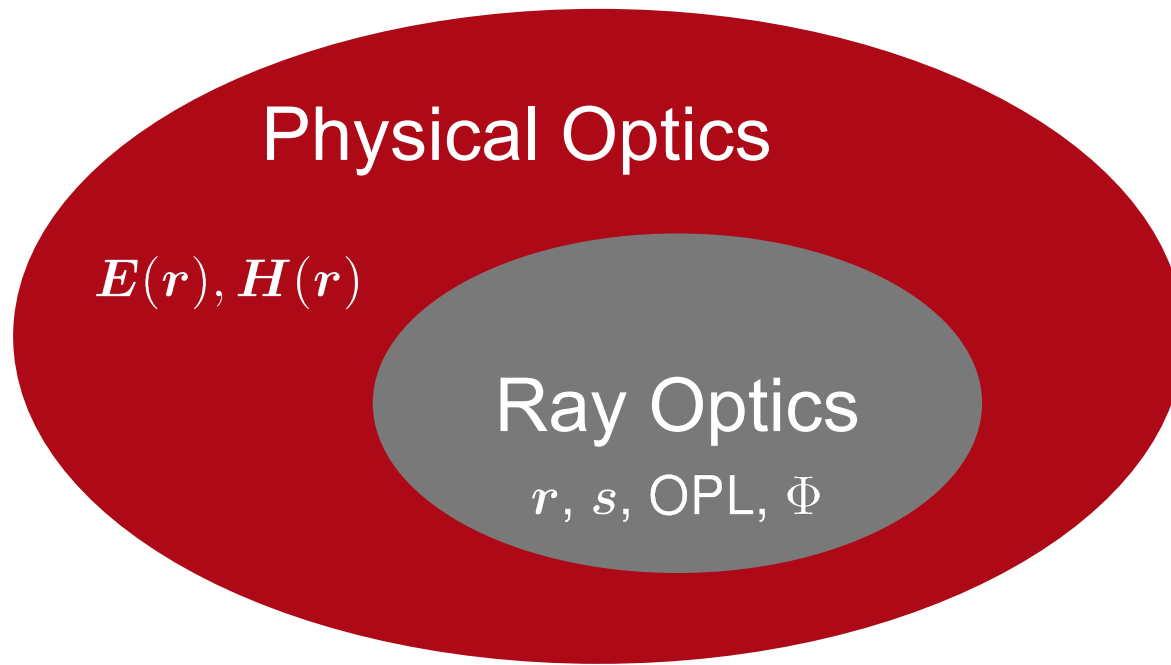
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Physical and Geometrical Optics: Light Propagation

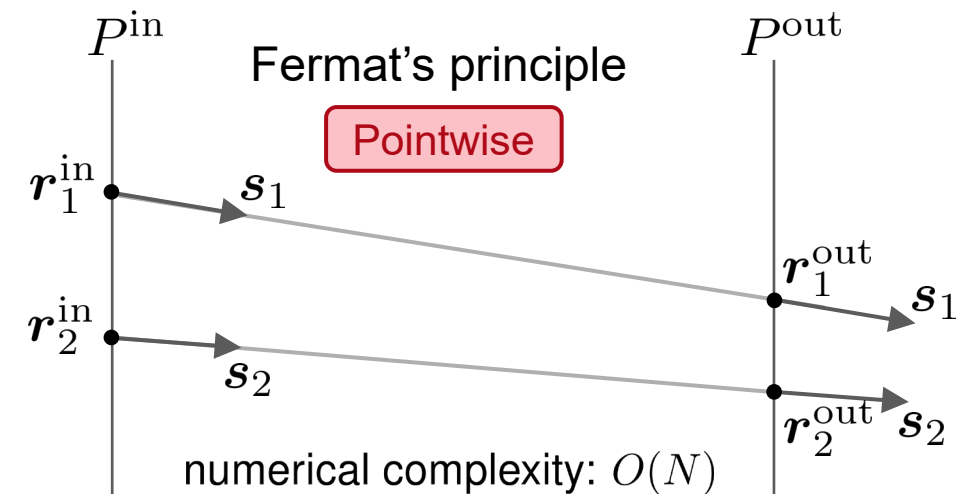
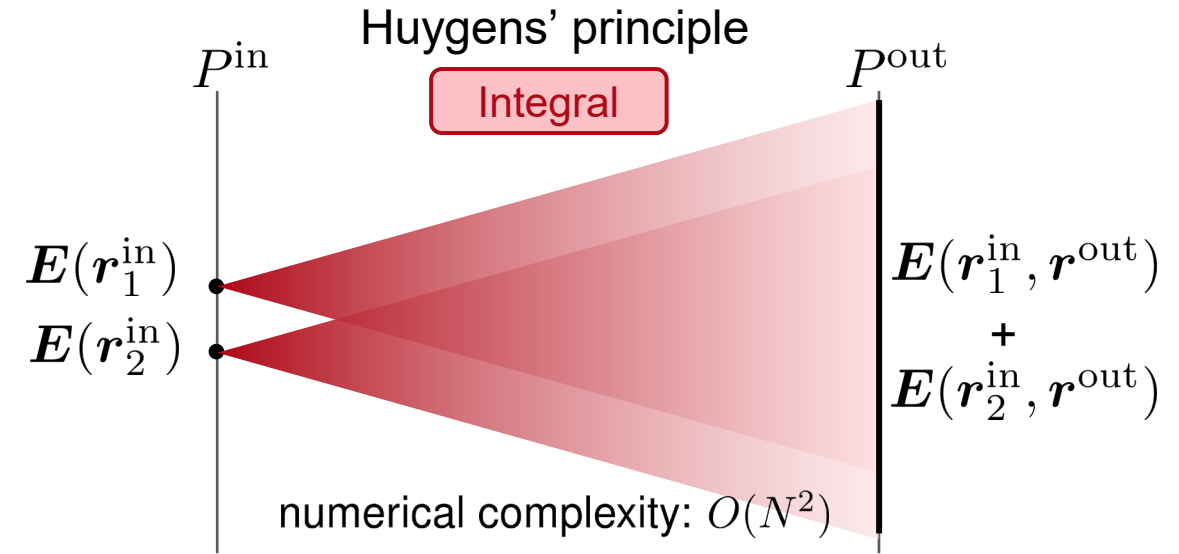
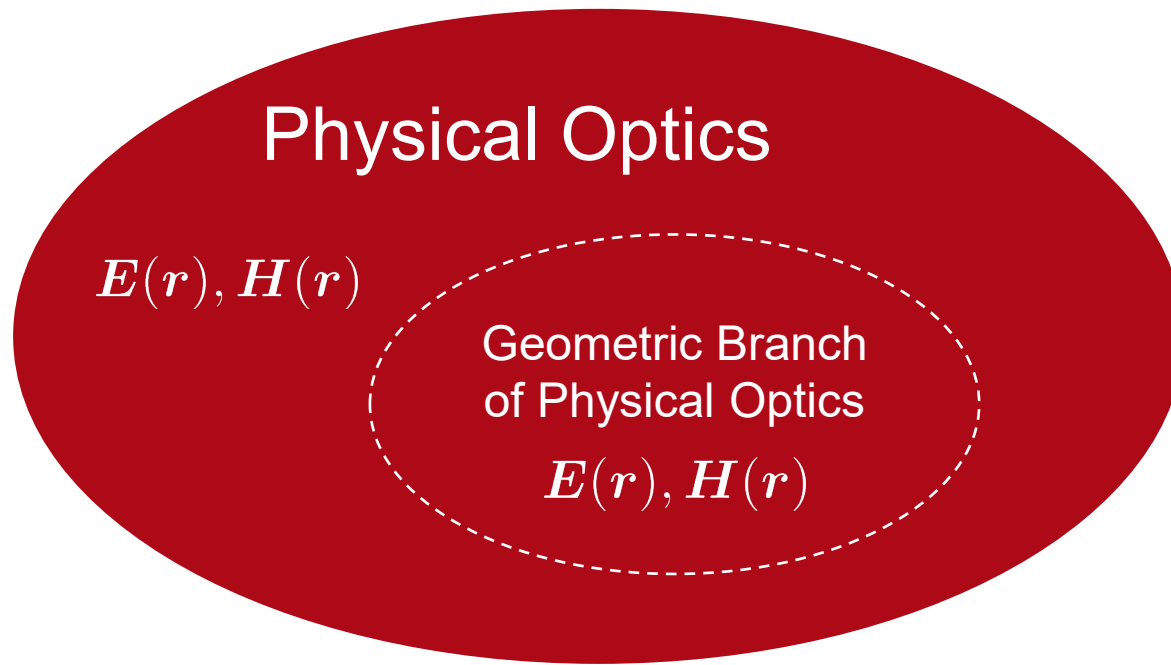


*Here: Propagation in homogeneous media

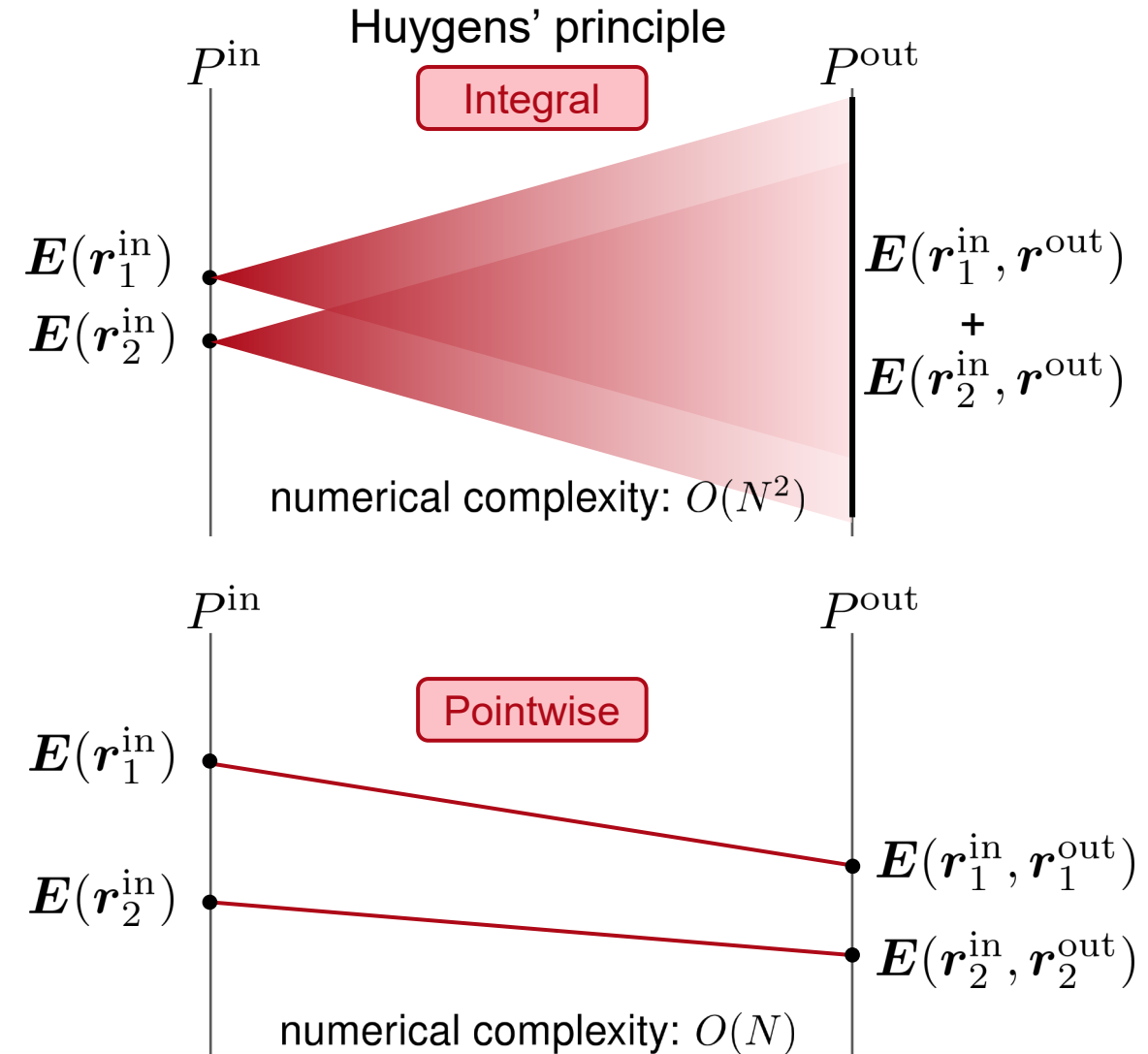
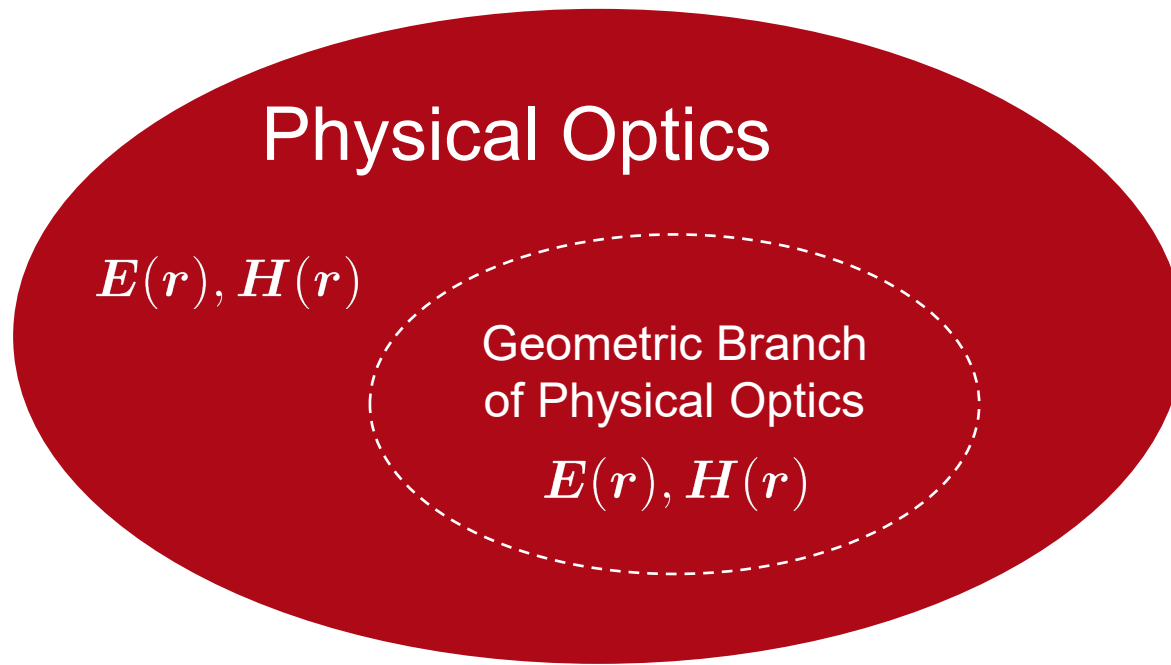
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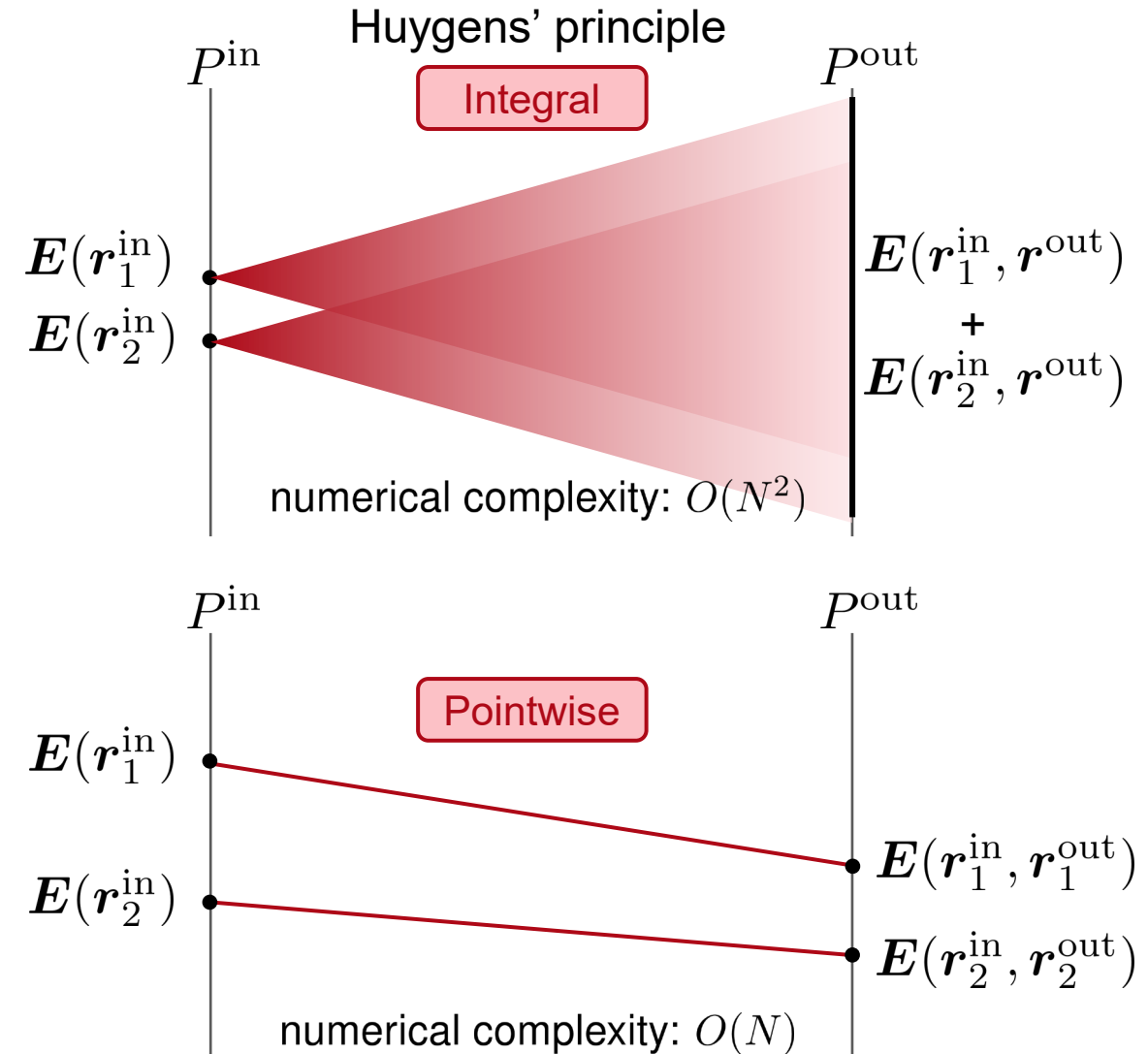
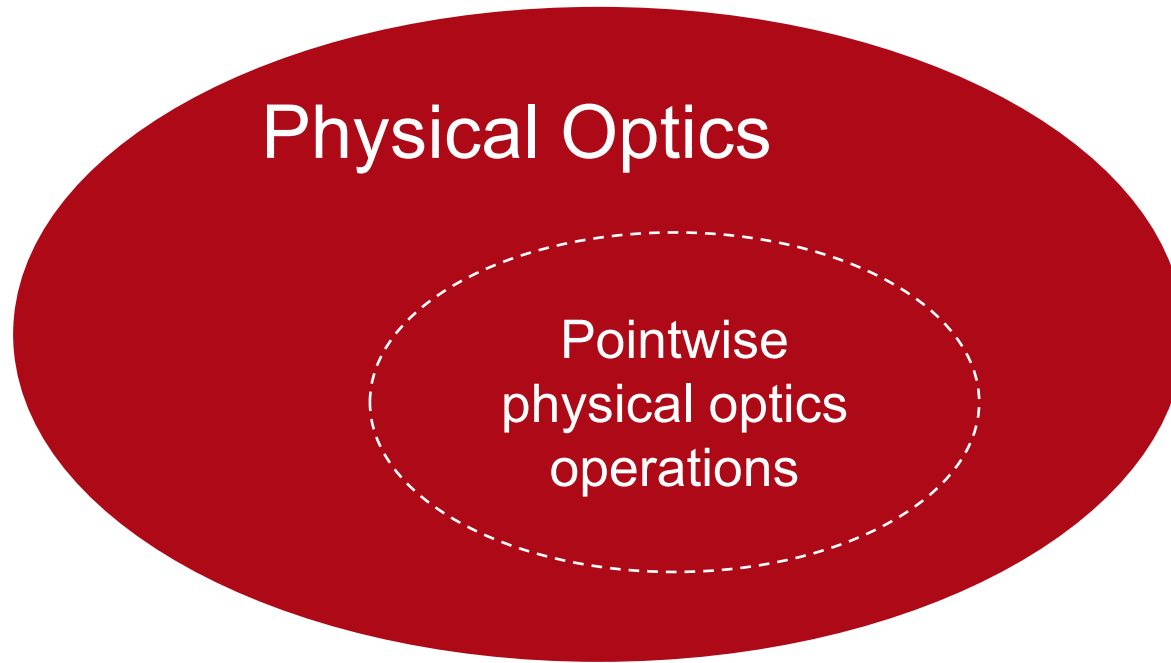
Geometric Branch of Physical Optics: Pointwise Operations



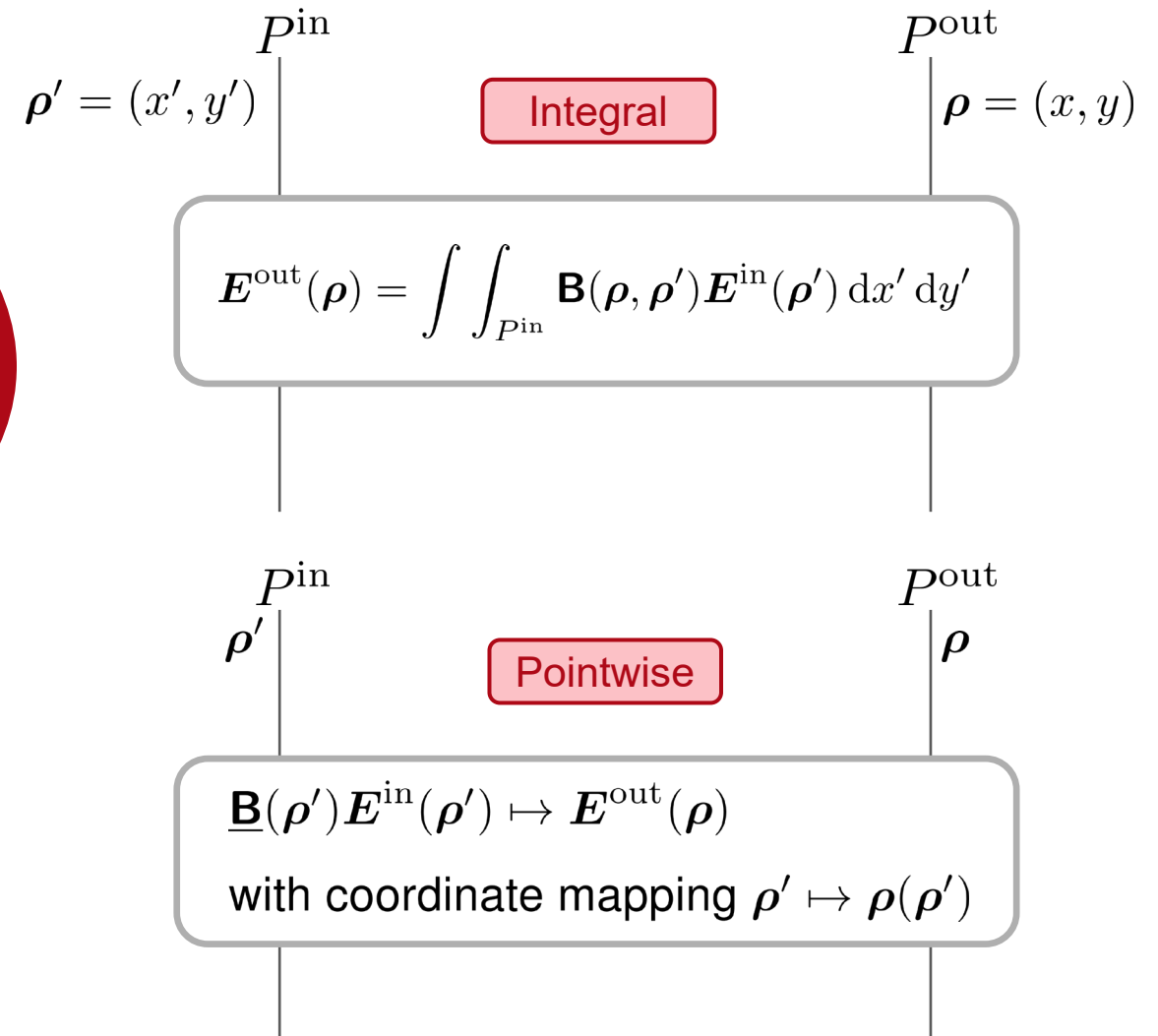
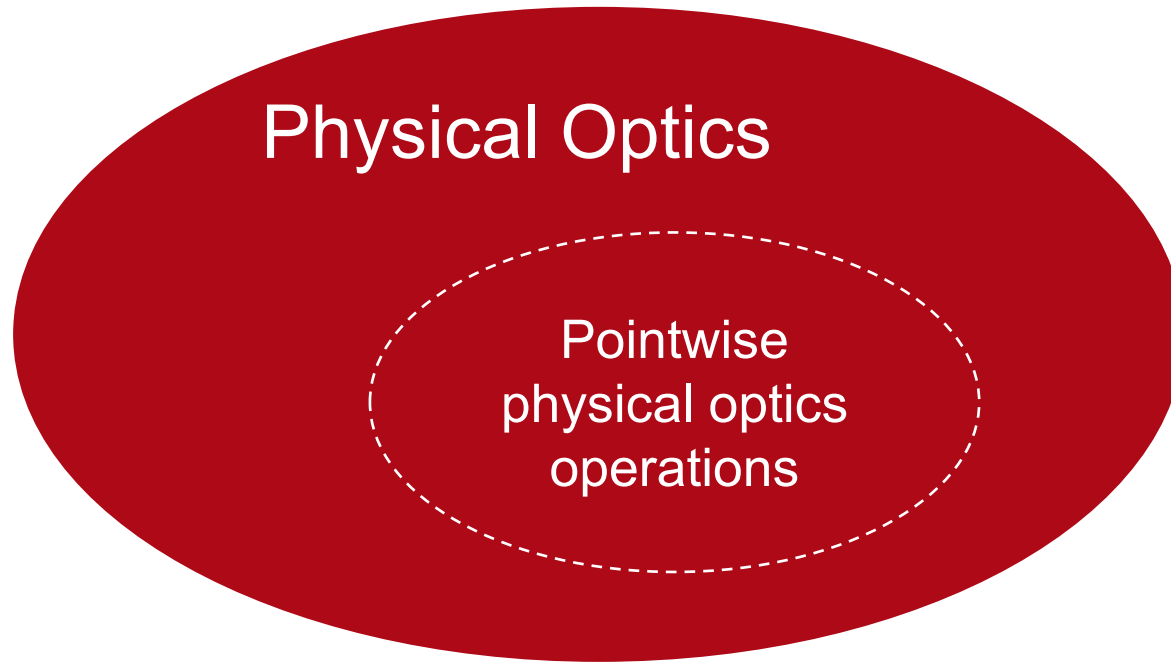
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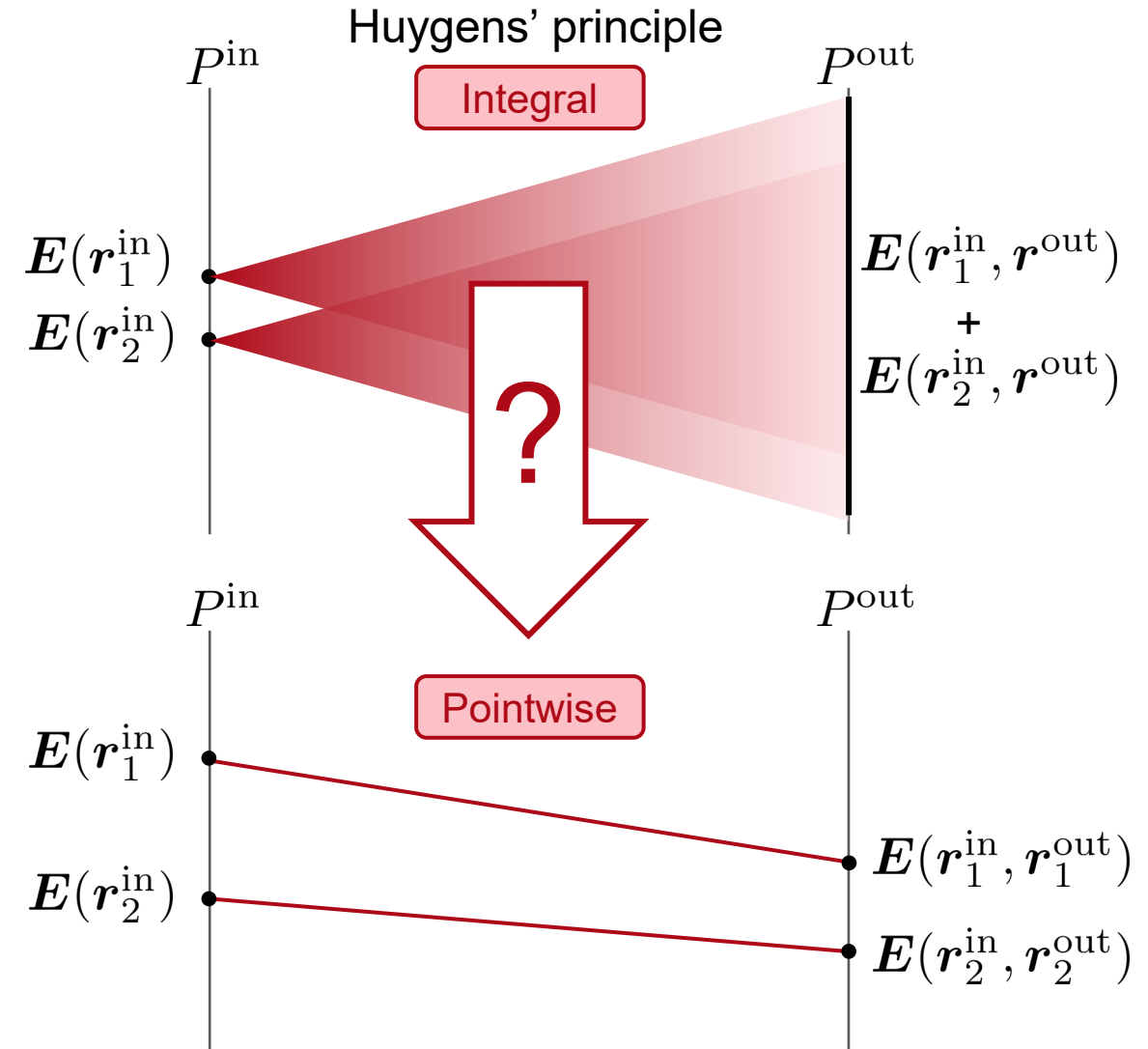
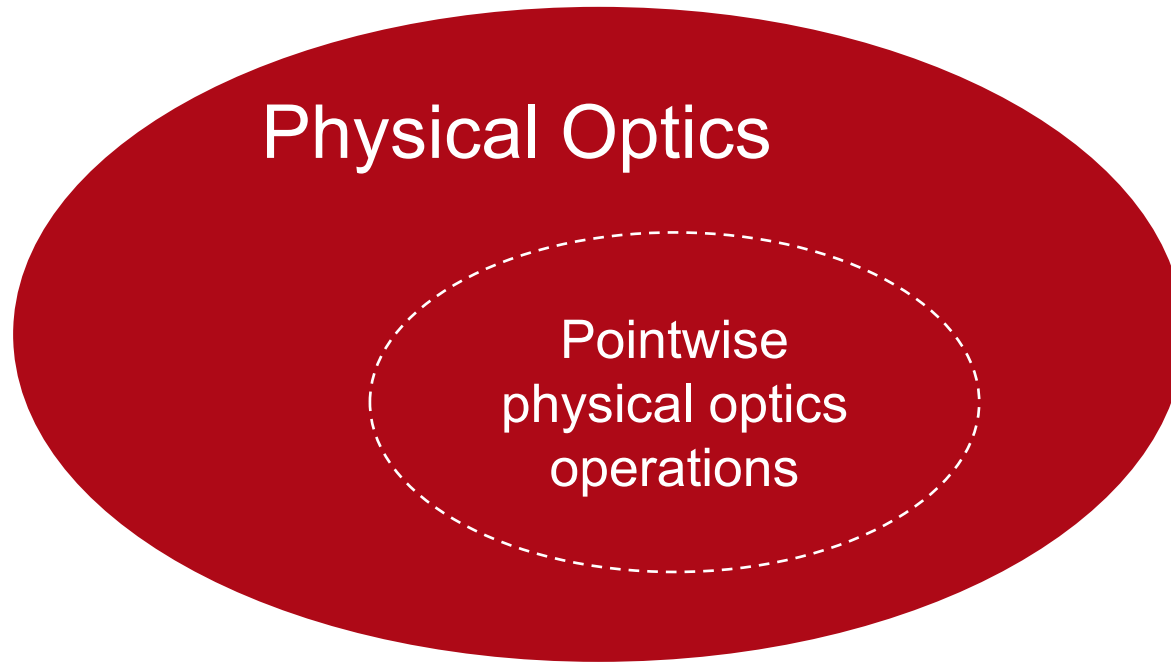
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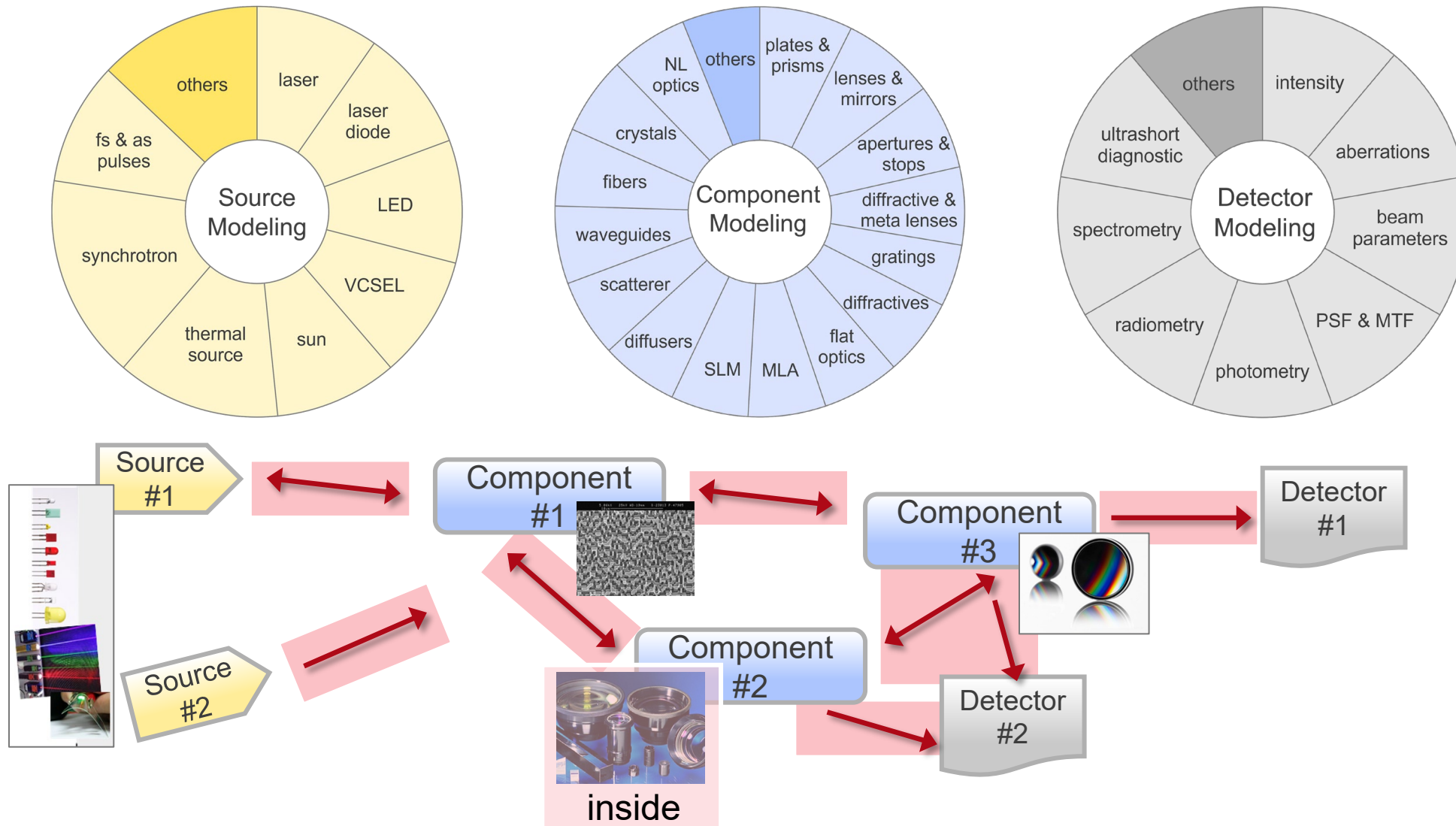
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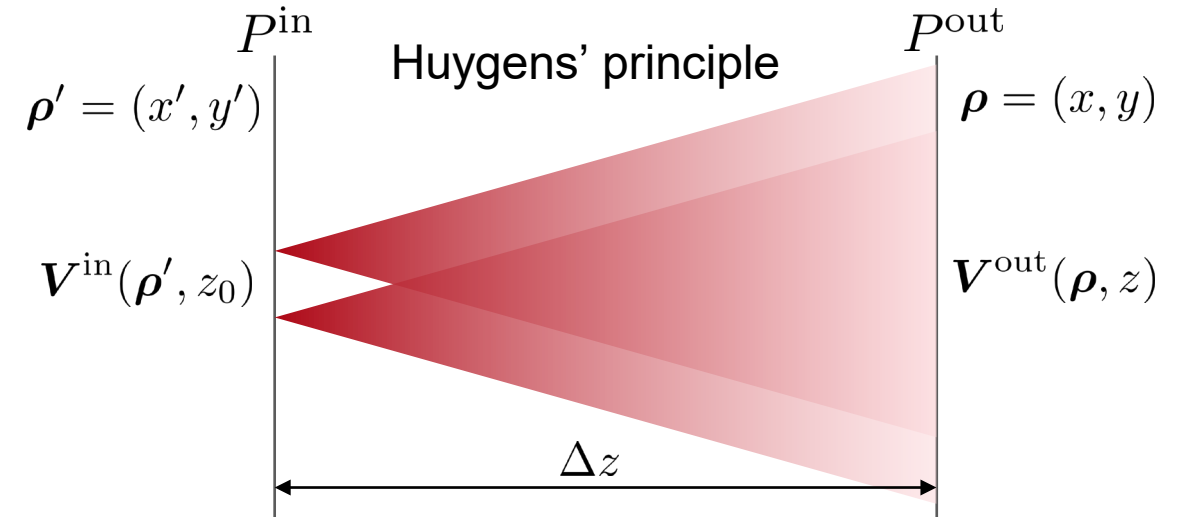
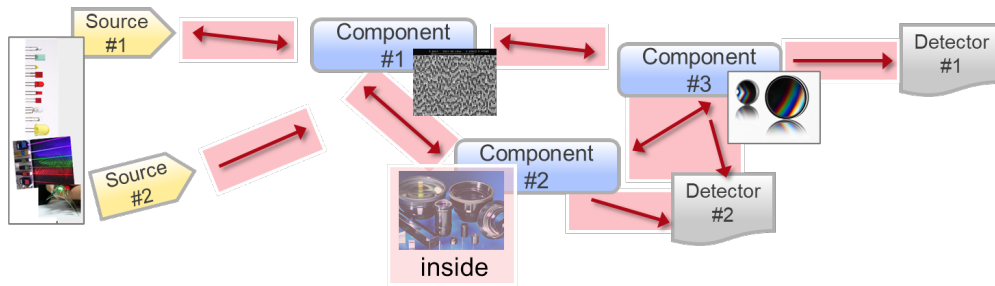


Propagation in Homogeneous Isotropic Media*



*Homogeneous media examples: vacuum, glasses, plastic, water, oil

Propagation in Homogeneous Isotropic Media*



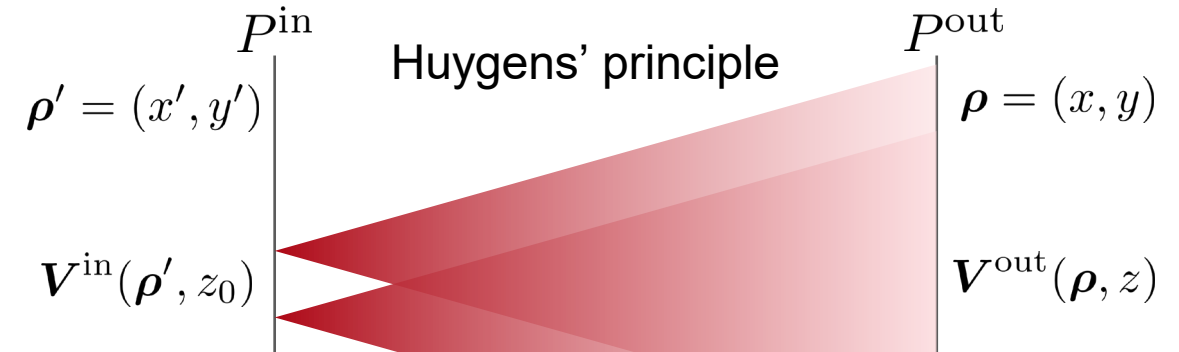
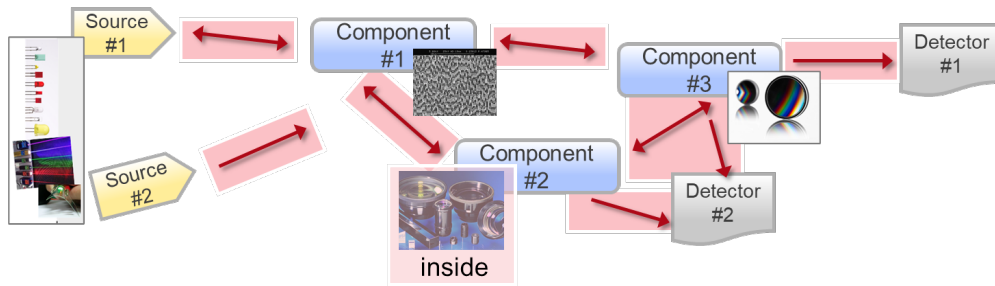
- Propagating an electromagnetic field

$$V := \left(E_x, E_y, E_z, H_x, H_y, H_z \right)^T$$

between planes of arbitrary orientation or surfaces constitutes a **key technology in physical optics modeling**.

*Homogeneous media examples: vacuum, glasses, plastic, water, oil

Propagation in Homogeneous Isotropic Media*



$$V(\rho, z) = -\frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} V(\rho', z_0) \frac{\partial}{\partial z} \frac{e^{ik_0 \tilde{n} R}}{R} dx' dy'$$

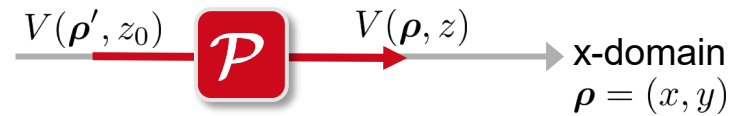
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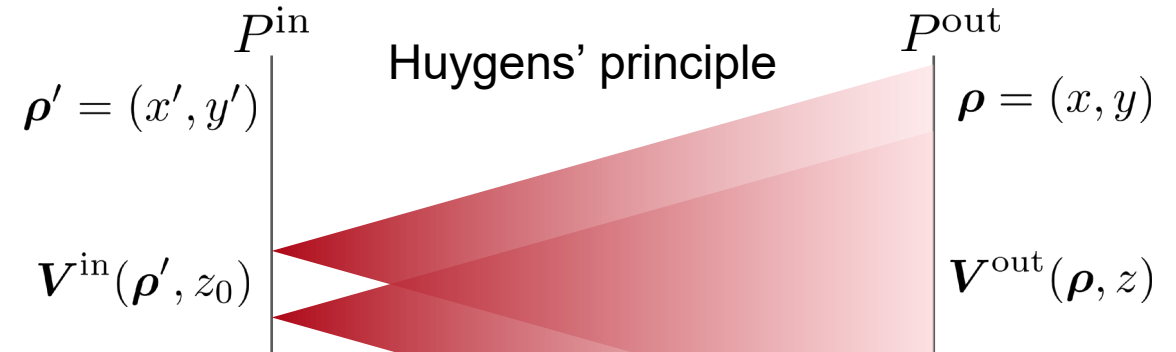
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Propagation in Homogeneous Isotropic Media*



- In x-domain propagation is expressed by the Rayleigh-Sommerfeld **integral**

$$\mathcal{P} V(\boldsymbol{\rho}, z) = -\frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} V(\boldsymbol{\rho}', z_0) \frac{\partial}{\partial z} \frac{e^{ik_0 \tilde{n} R}}{R} dx' dy'.$$



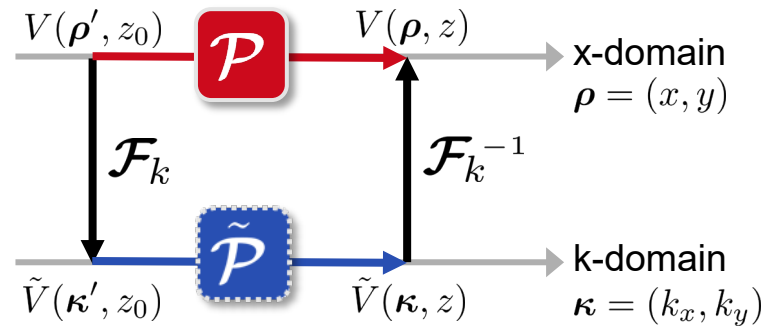
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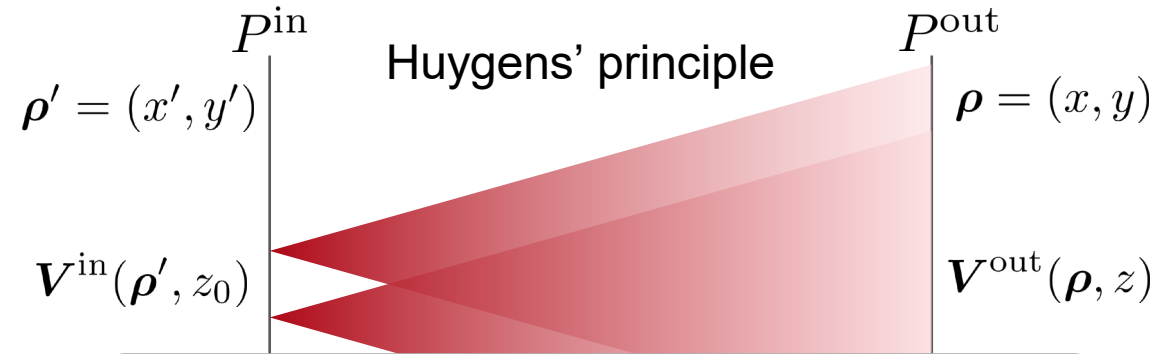
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- In k-domain we apply the **pointwise operation**

$$\tilde{\mathcal{P}} \quad \tilde{\mathcal{P}} : \tilde{V} \mapsto \tilde{V} \times e^{i\tilde{k}_z(\kappa)\Delta z}.$$

- The Fourier transform $\mathcal{F}_k$ is an integral operator:

$$\tilde{V}(\kappa, z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} V(\rho, z) \exp(-i\kappa \cdot \rho) dx dy$$



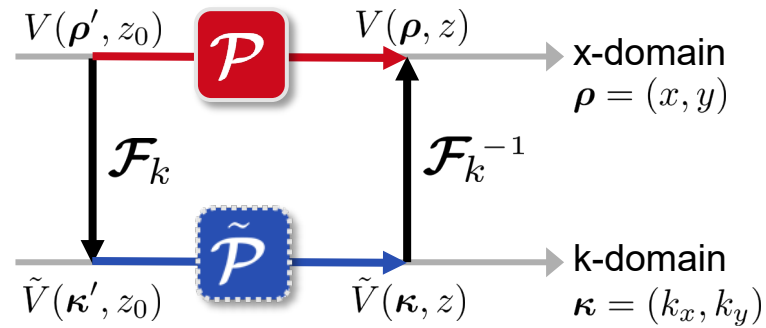
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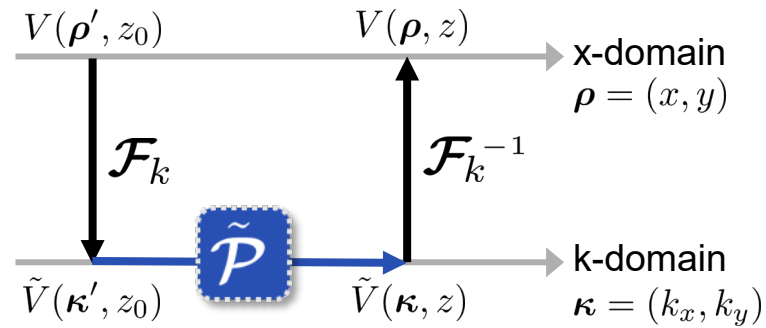
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Numerical complexity: $O(N^2)$

Numerical complexity
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Propagation in Homogeneous Isotropic Media



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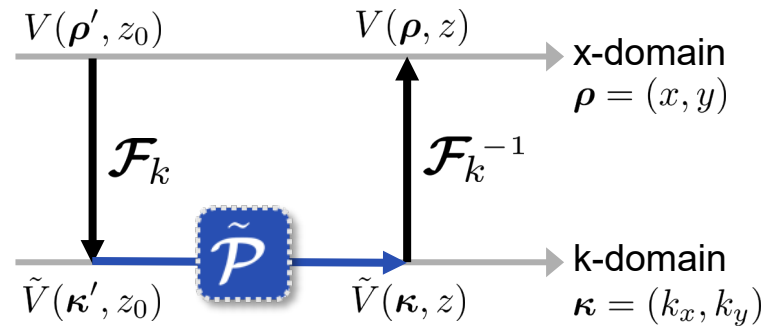
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A pointwise physical-optics propagation in homogeneous media can only be obtained, if both **Fourier transforms become (approximately) pointwise.**

Propagation in Homogeneous Isotropic Media



- In k-domain we apply the **pointwise operation**



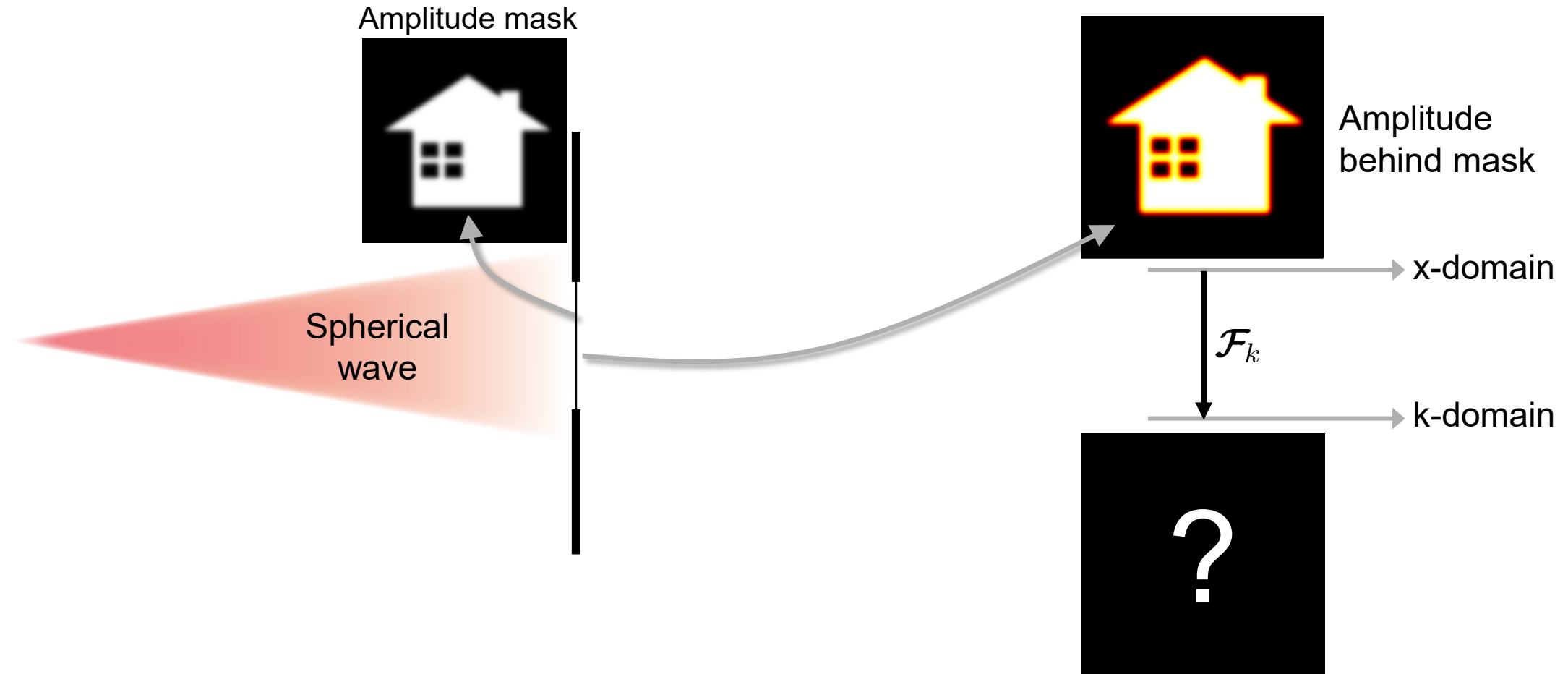
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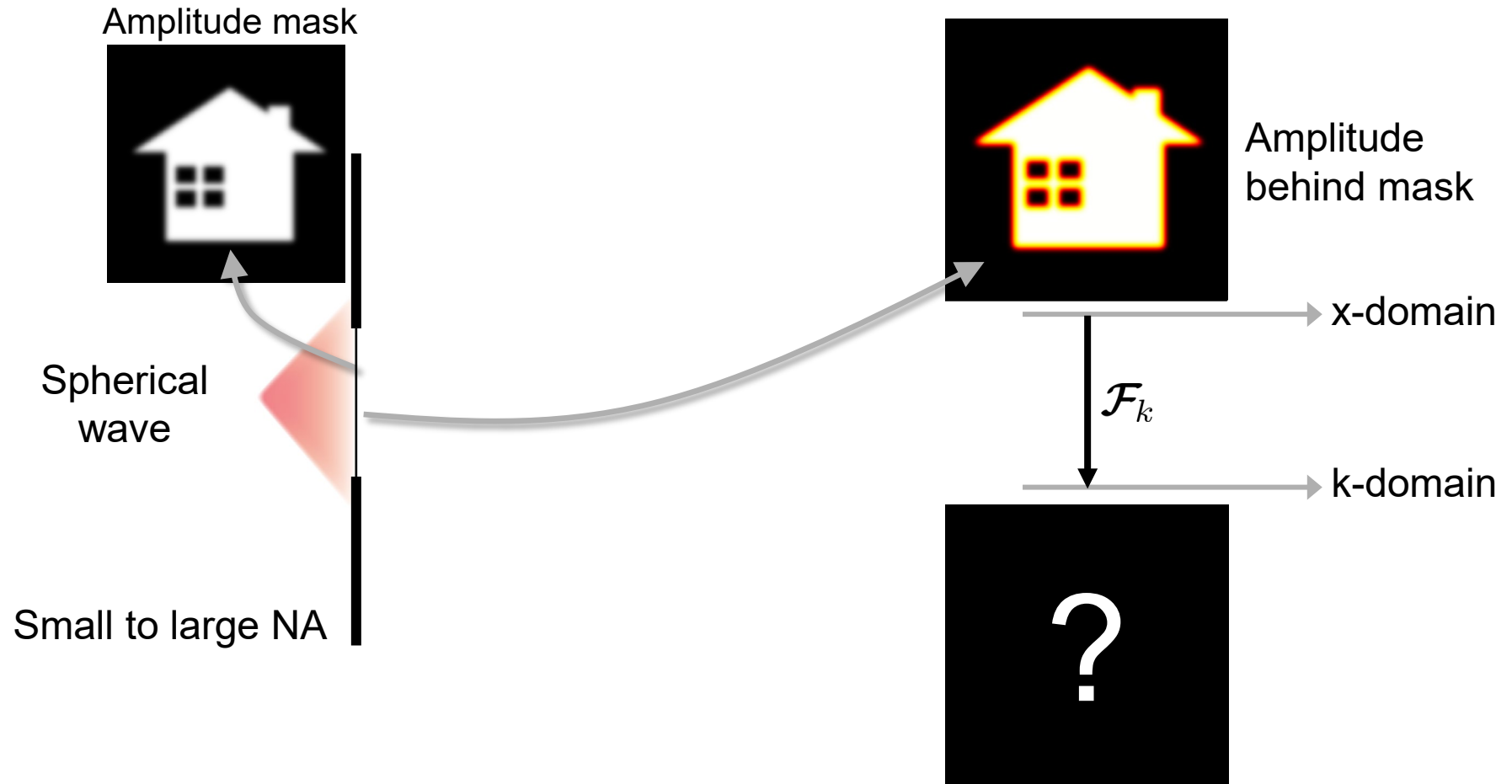
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Pointwise Fourier transform
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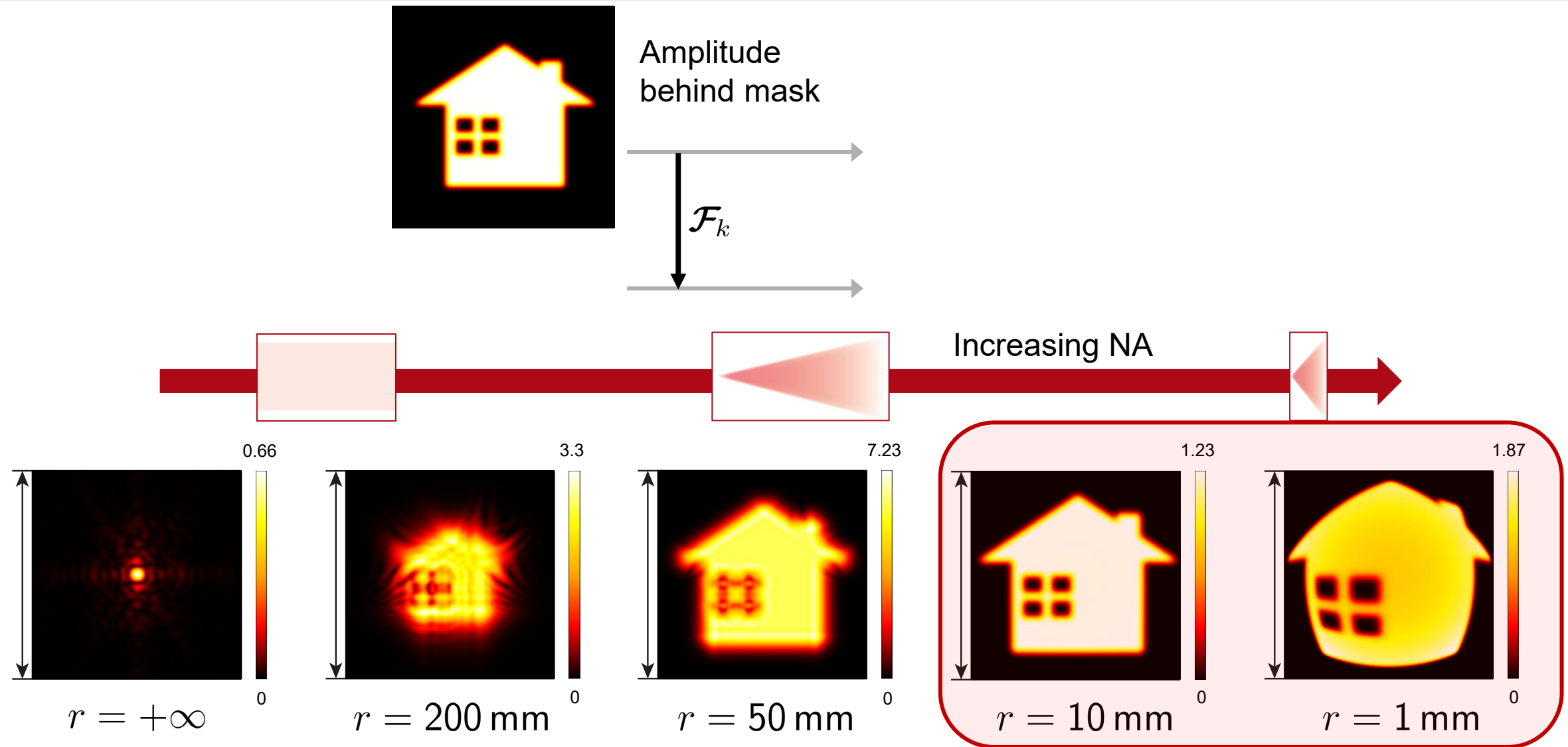
Pointwise Fourier Transform: Demonstration



Pointwise Fourier Transform: Demonstration



Results of Fourier Transform



Pointwise vs. Integral Fourier Transform @ NA = 0

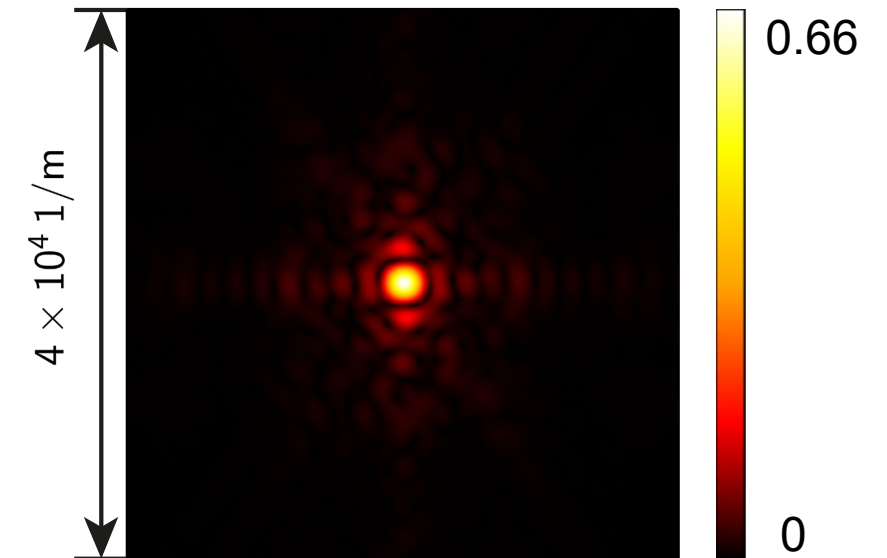
Sampling Points for Different Fourier Transform Techniques

	PFT	FFT
NA = 0	73 x 59	(73 x 59)

$$\tilde{V}(\boldsymbol{\kappa}) = (\mathcal{F}_k^{1:1} V)(\boldsymbol{\kappa}) = (f(\boldsymbol{\rho})V(\boldsymbol{\rho}))[\boldsymbol{\rho} \leftarrow \boldsymbol{\rho}(\boldsymbol{\kappa})]$$



$$\tilde{V}(\boldsymbol{\kappa}, z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} V(\boldsymbol{\rho}, z) \exp(-i\boldsymbol{\kappa} \cdot \boldsymbol{\rho}) \, dx \, dy$$



Pointwise vs. Integral Fourier Transform @ NA = 0.027

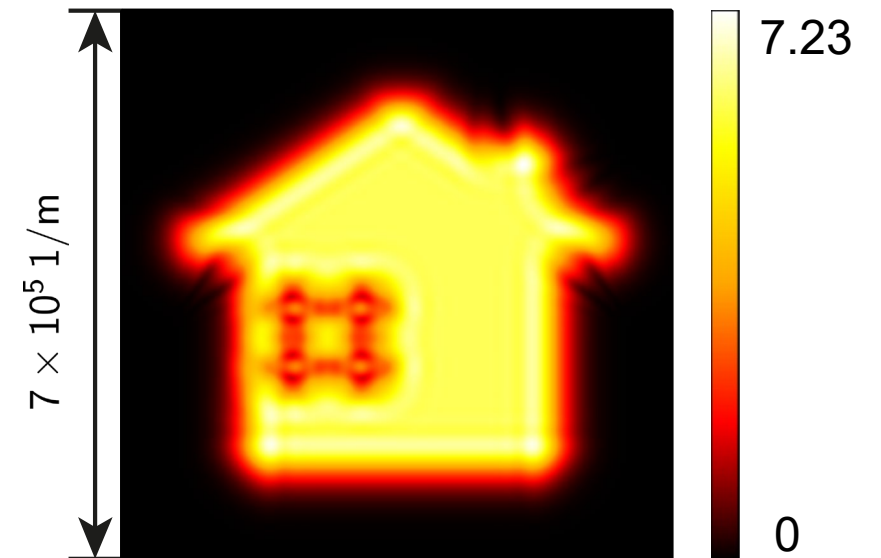
Sampling Points for Different Fourier Transform Techniques

	PFT	FFT
NA = 0.027	(73 x 59)	(315 x 262)

$$\tilde{V}(\boldsymbol{\kappa}) = (\mathcal{F}_k^{1:1} V)(\boldsymbol{\kappa}) = (f(\boldsymbol{\rho})V(\boldsymbol{\rho}))[\boldsymbol{\rho} \leftarrow \boldsymbol{\rho}(\boldsymbol{\kappa})]$$



$$\tilde{V}(\boldsymbol{\kappa}, z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} V(\boldsymbol{\rho}, z) \exp(-i\boldsymbol{\kappa} \cdot \boldsymbol{\rho}) \, dx \, dy$$



Pointwise vs. Integral Fourier Transform @ NA = 0.134

Sampling Points for Different Fourier Transform Techniques

	PFT	FFT
NA = 0.134	(73 x 59)	(1333 x 925)

$$\tilde{V}(\boldsymbol{\kappa}) = (\mathcal{F}_k^{1:1} V)(\boldsymbol{\kappa}) = (f(\boldsymbol{\rho})V(\boldsymbol{\rho}))[\boldsymbol{\rho} \leftarrow \boldsymbol{\rho}(\boldsymbol{\kappa})]$$

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Pointwise vs. Integral Fourier Transform @ NA = 0.804

Sampling Points for Different Fourier Transform Techniques

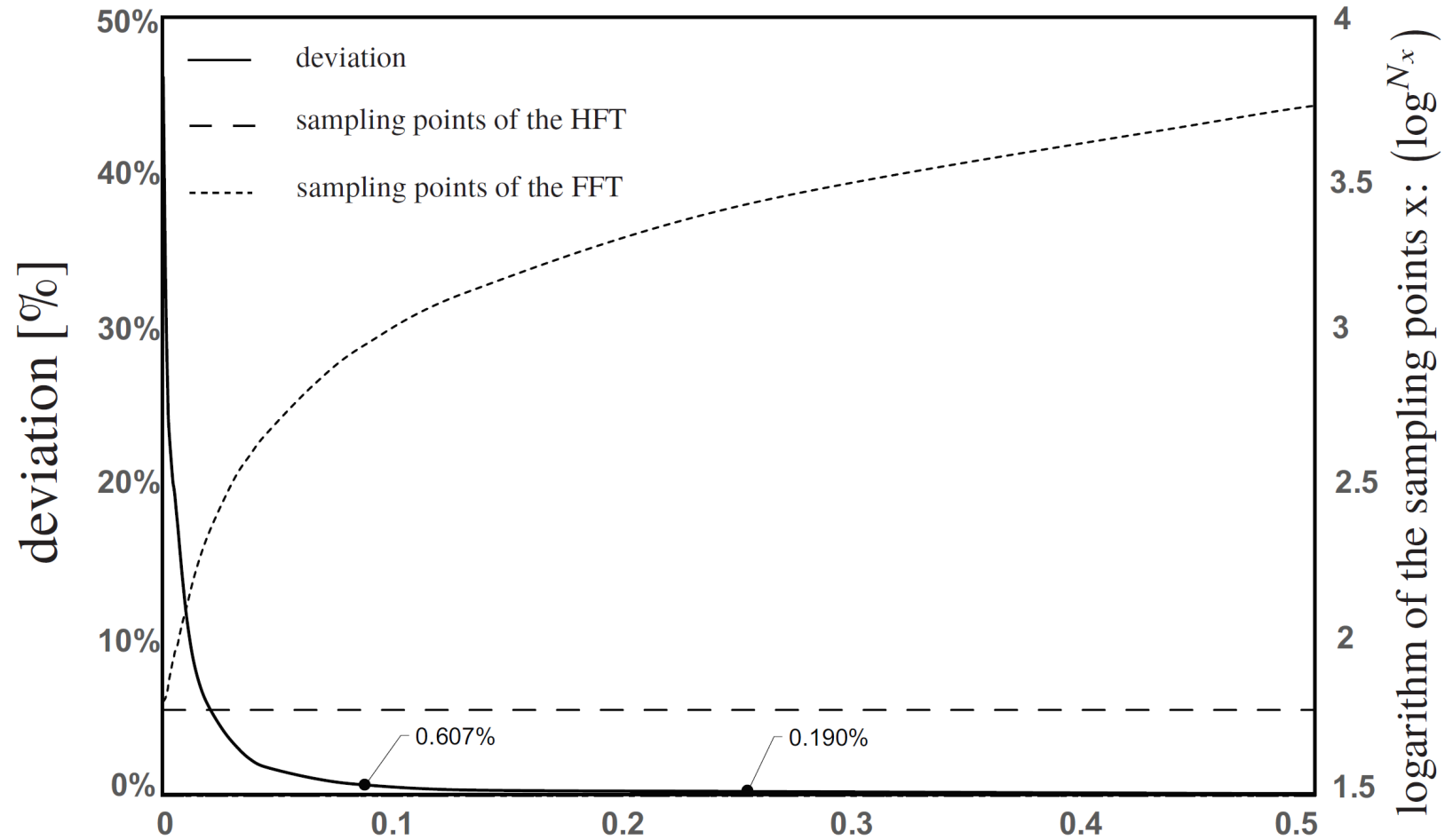
	PFT	FFT
NA = 0.804	(73 x 59)	(7947 x 6225)

$$\tilde{V}(\boldsymbol{\kappa}) = (\mathcal{F}_k^{1:1} V)(\boldsymbol{\kappa}) = (f(\boldsymbol{\rho})V(\boldsymbol{\rho}))[\boldsymbol{\rho} \leftarrow \boldsymbol{\rho}(\boldsymbol{\kappa})]$$

$$\tilde{V}(\boldsymbol{\kappa}, z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} V(\boldsymbol{\rho}, z) \exp(-i\boldsymbol{\kappa} \cdot \boldsymbol{\rho}) \, dx \, dy$$

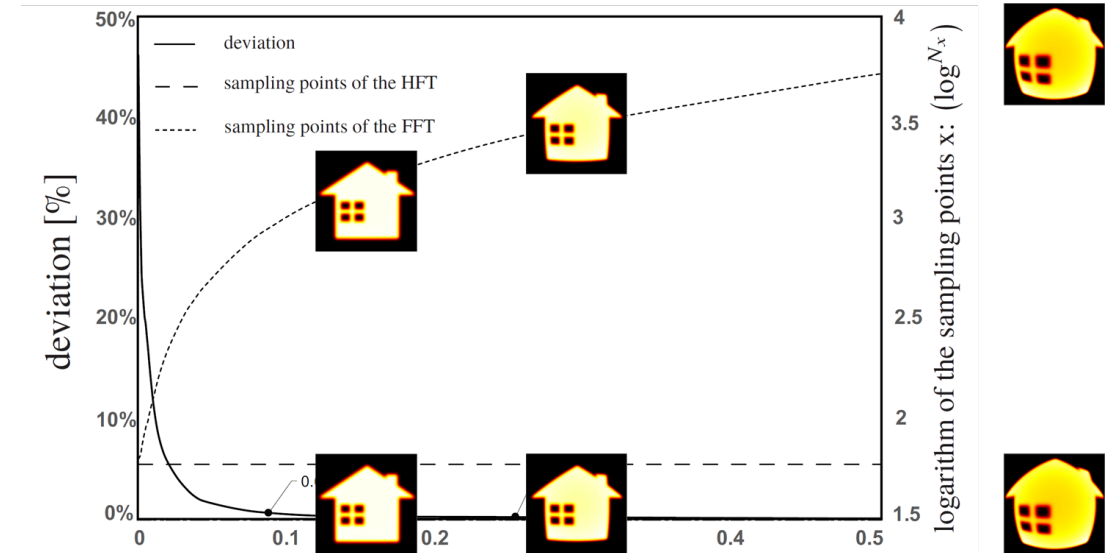


Comparison of the Numerical Effort and Accuracy



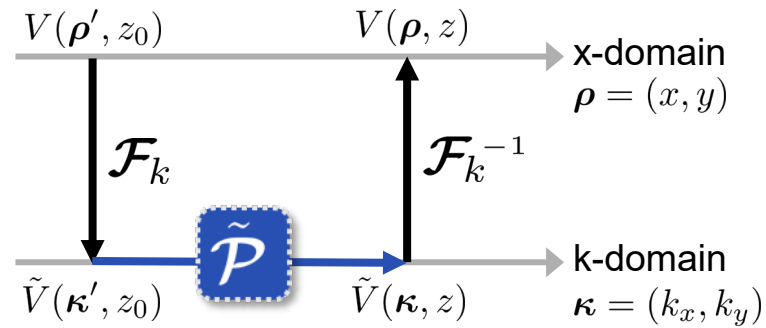
Facts About Pointwise Fourier Transform

- The pointwise Fourier transform (PFT) is valid for field components with sufficiently **strong spherical and aberrated wavefront phases**.
- The validity can be estimated for any field component by a pointwise transformation index.
- That enables a **seamless transition between integral and pointwise Fourier transform** in physical optics modeling algorithms by pure mathematical arguments.
- PFT and FFT have a numerical complexity of $O(N)$. However, the number of sampling points N for PFT is significantly smaller: $N^{\text{PFT}} \ll N^{\text{FFT}}$
- Typical numbers:
 $N^{\text{FFT}} = 10^6 - 10^8$ and $N^{\text{PFT}} = 10^2 - 10^3$



Z. Wang, O. Baladron-Zorita, C. Hellmann, and F. Wyrowski, "Theory and algorithm of the homeomorphic Fourier transform for optical simulations," Opt Express **28**, 10552–10571 (2020).

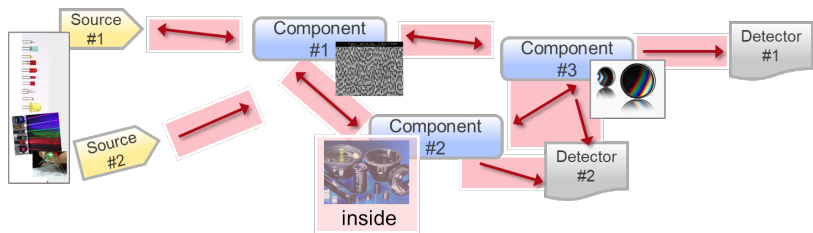
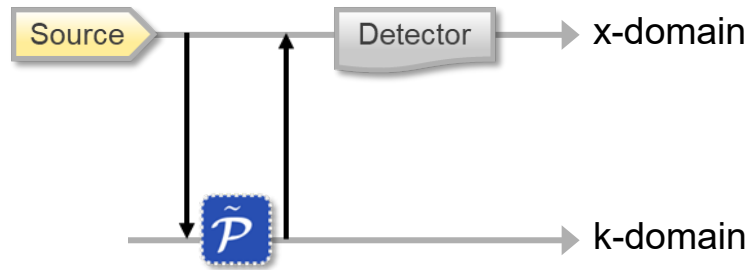
Consequences for Physical Optics Modeling



Physical Optics

Pointwise
physical optics
operations

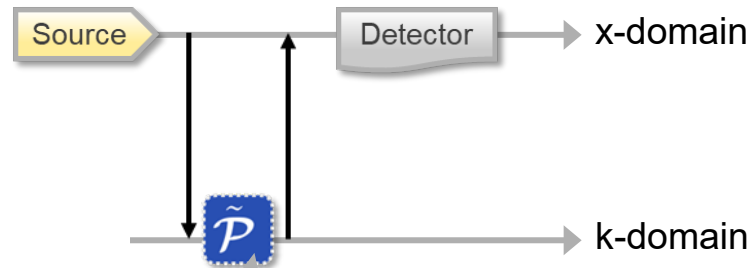
Consequences for Physical Optics Modeling



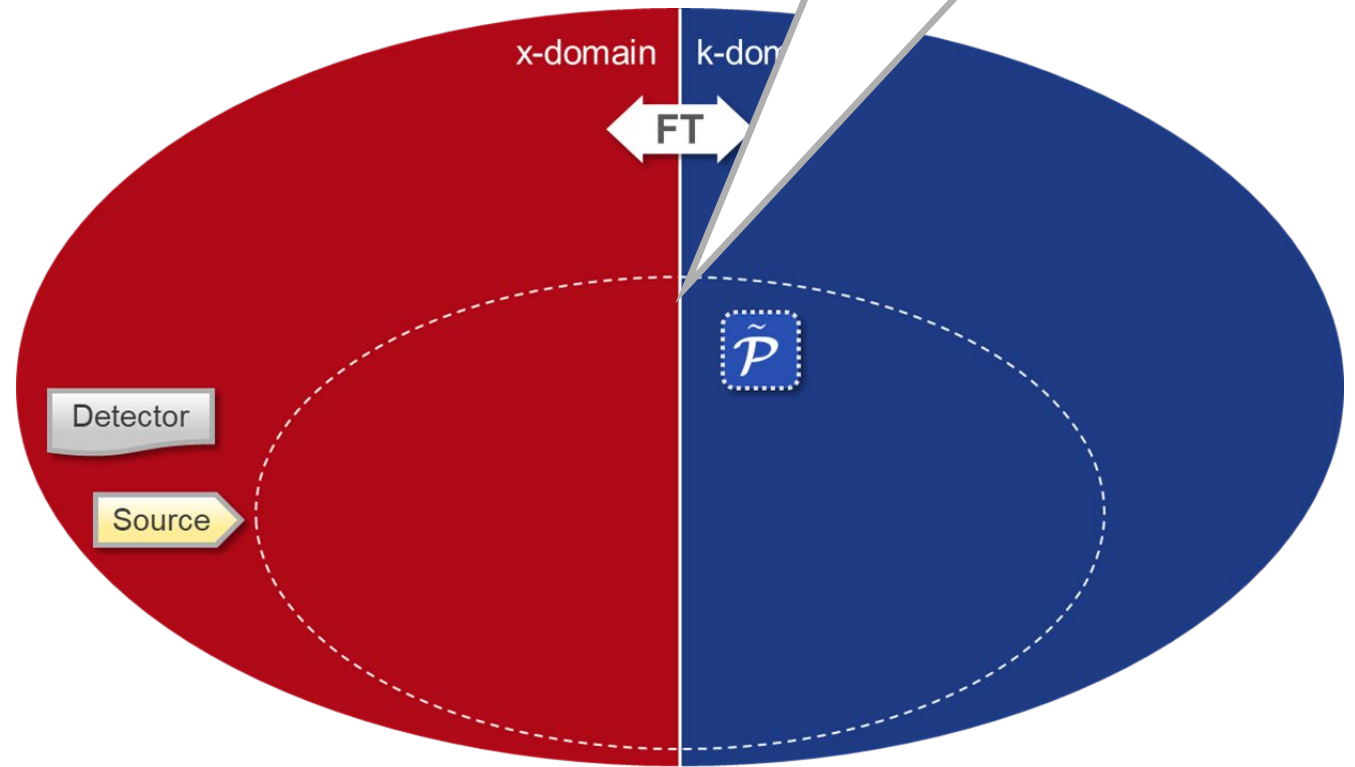
Physical Optics

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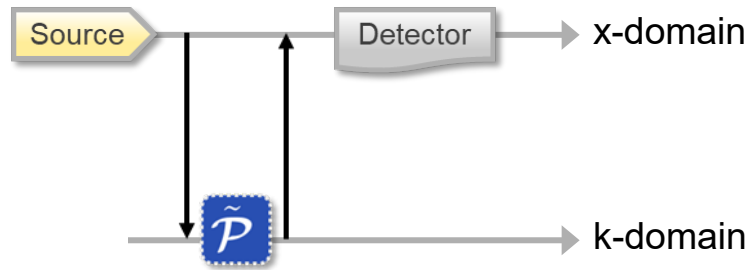
Consequences for Physical Optics Modeling



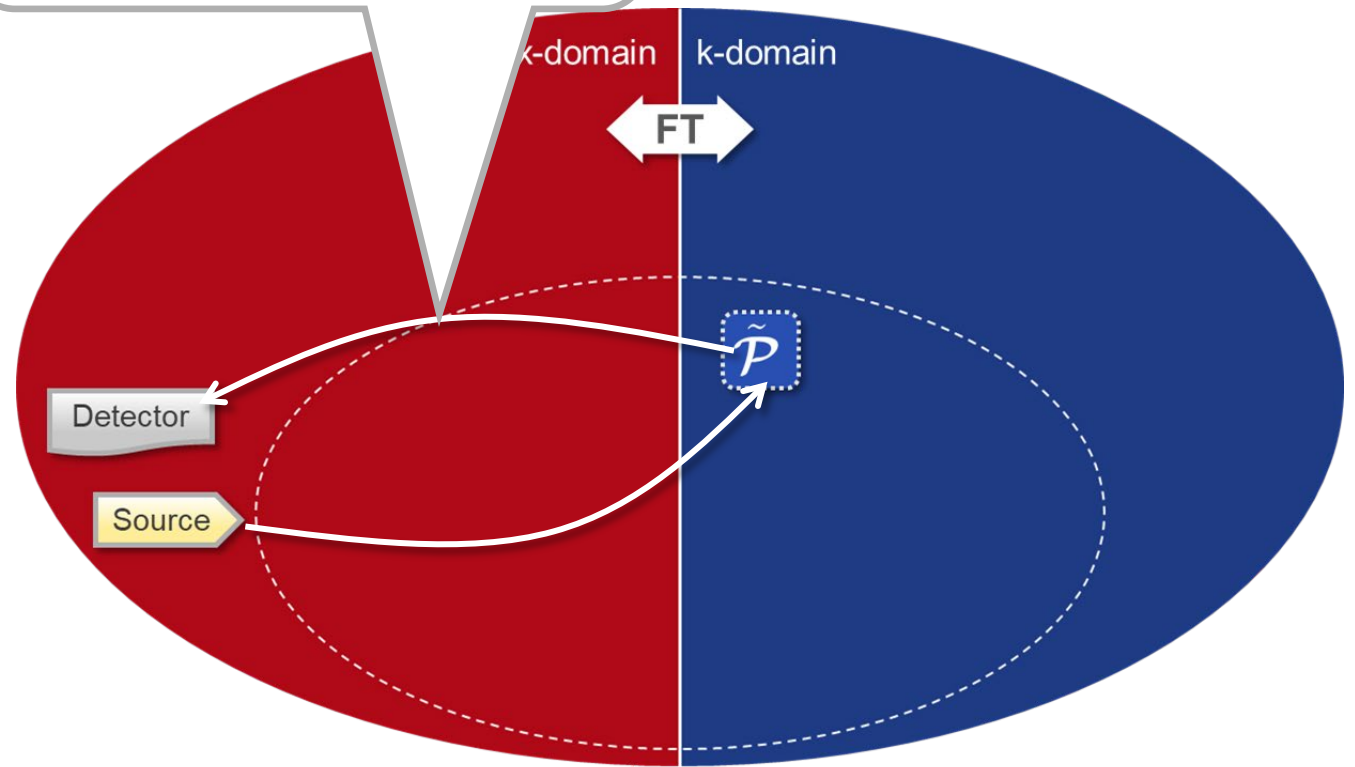
Blue with dashed line indicates pointwise operation in k-domain.



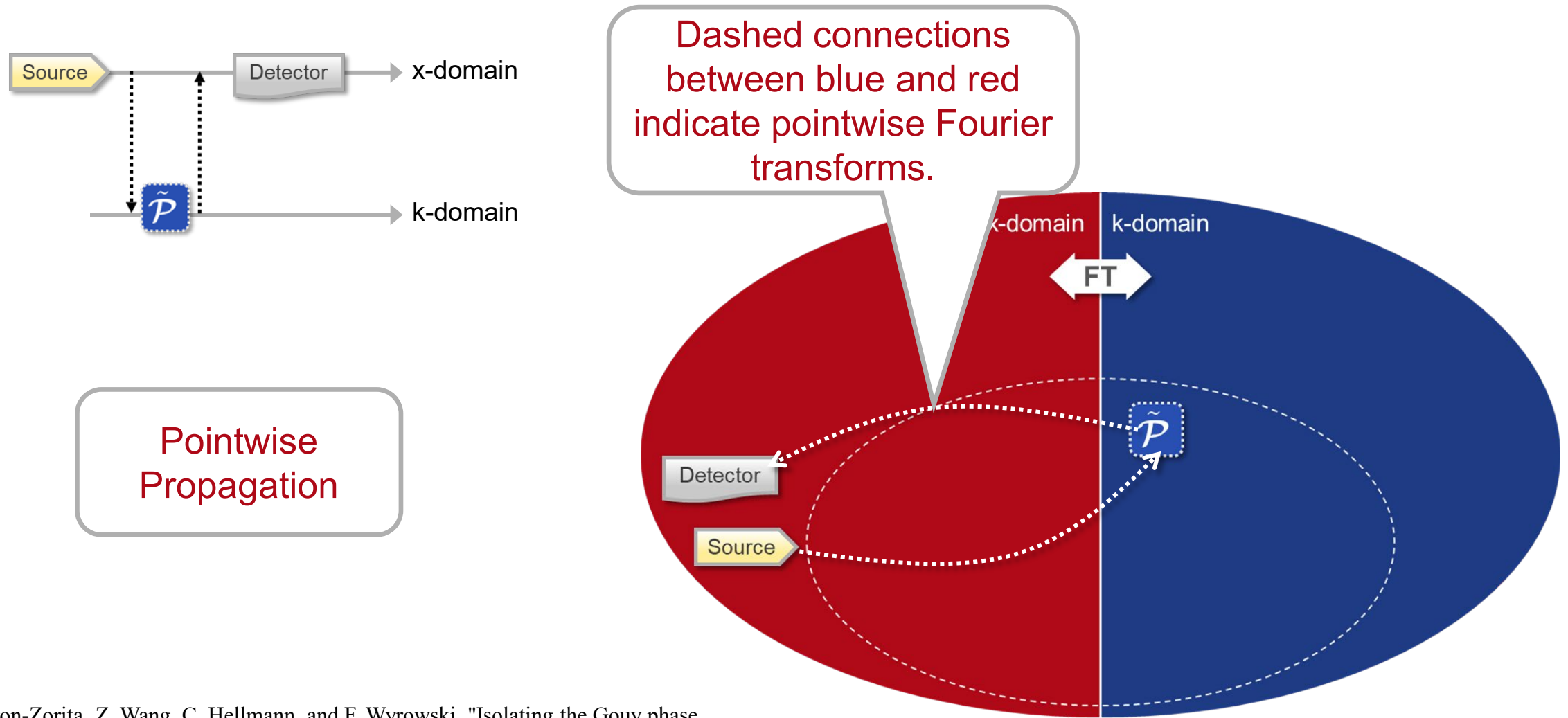
Consequences for Physical Optics Modeling



Connections between blue and red indicate Fourier transforms.

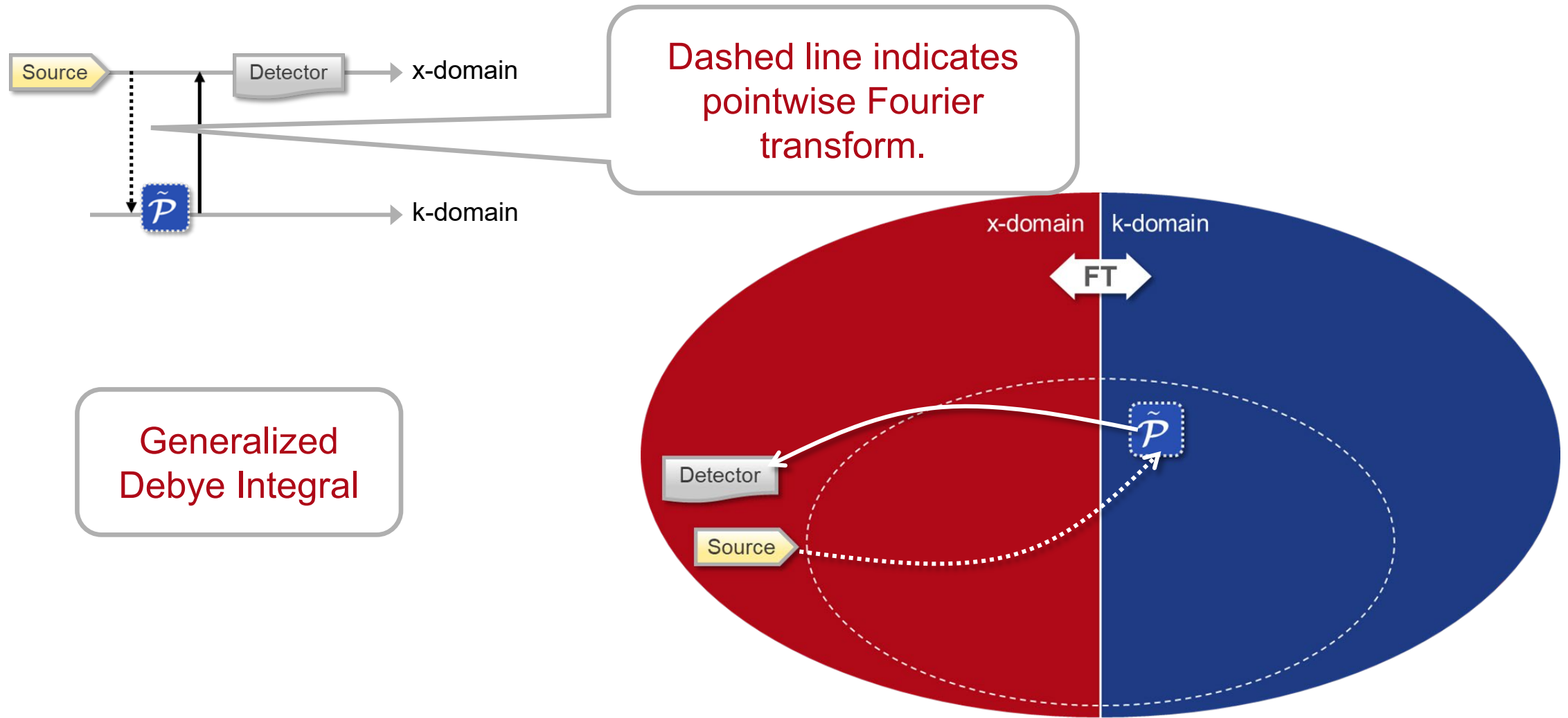


Consequences for Physical Optics Modeling



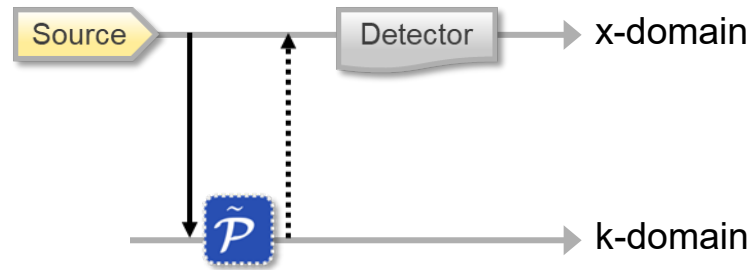
O. Baladron-Zorita, Z. Wang, C. Hellmann, and F. Wyrowski, "Isolating the Gouy phase shift in a full physical-optics solution to the propagation problem," J. Opt. Soc. Am. A **36**, 1551–1558 (2019).

Consequences for Physical Optics Modeling

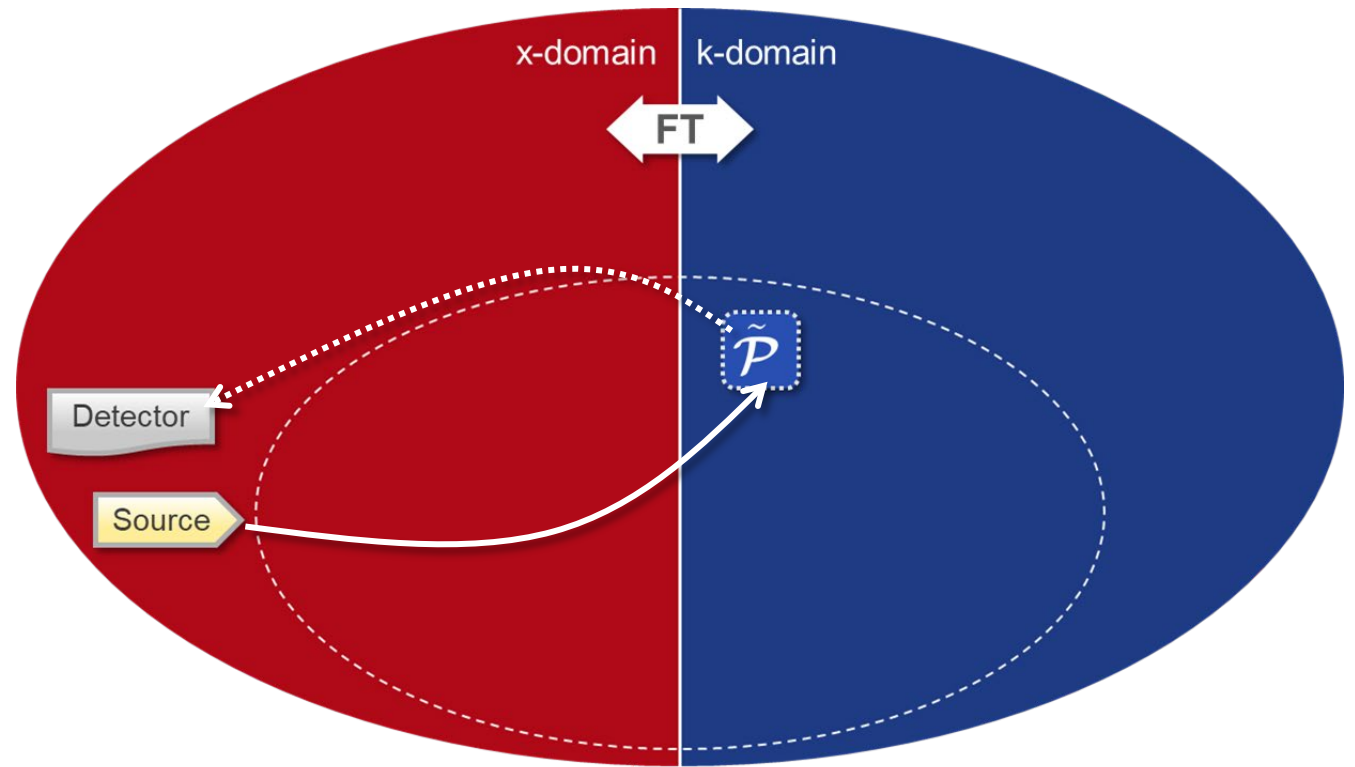


Z. Wang, O. Baladron-Zorita, C. Hellmann, and F. Wyrowski, "Generalized Debye integral," Opt. Express **28**, 24459–24470 (2020).

Consequences for Physical Optics Modeling

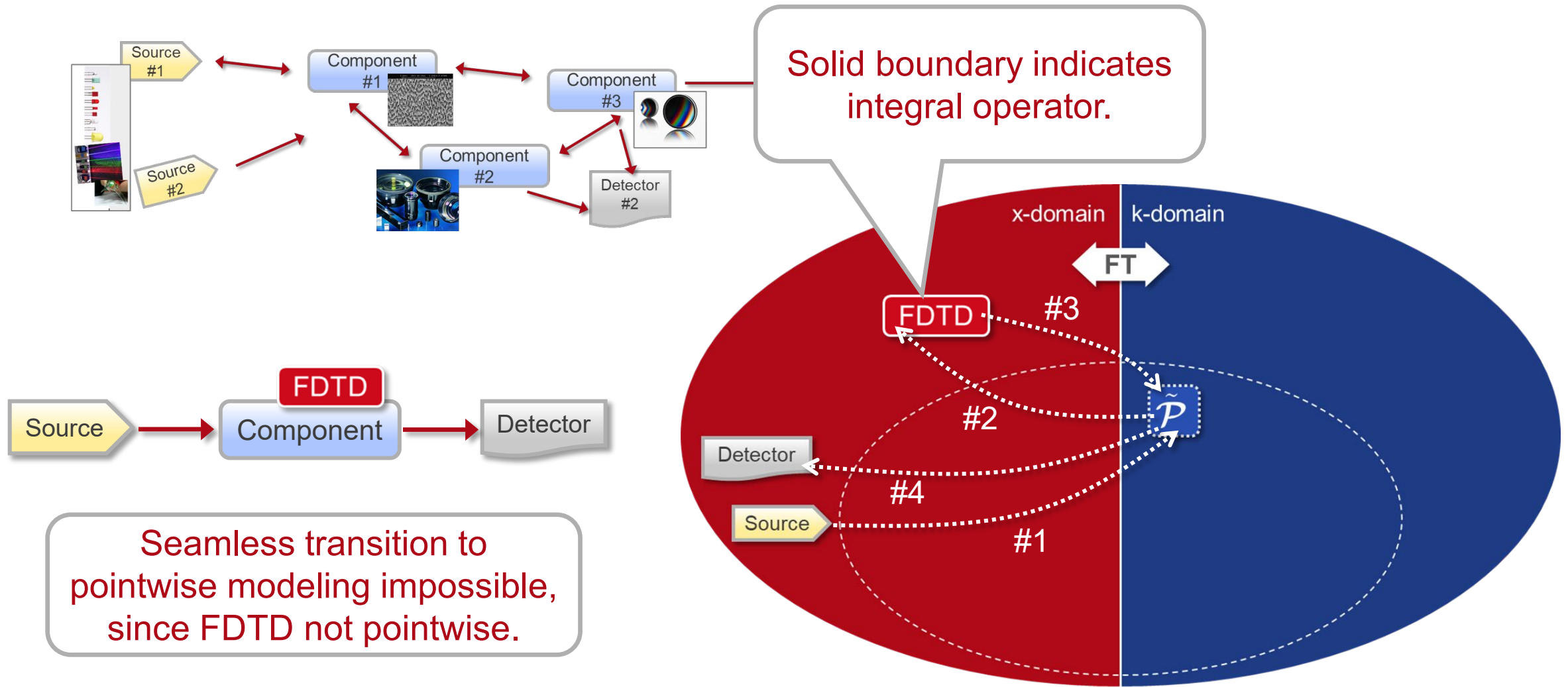


Generalized Far
Field Integral

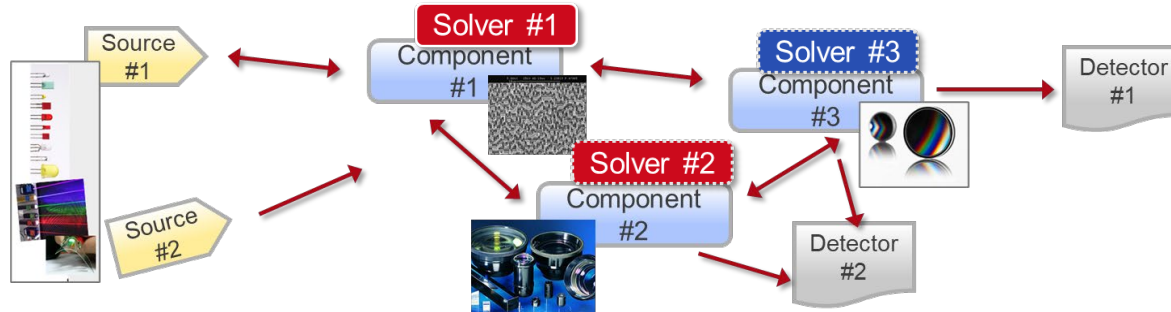


Z. Wang, O. Baladron-Zorita, C. Hellmann, and F. Wyrowski, "Generalized far-field integral," Opt. Express **29**, 1774–1787 (2021).

Consequences for Physical Optics System Modeling

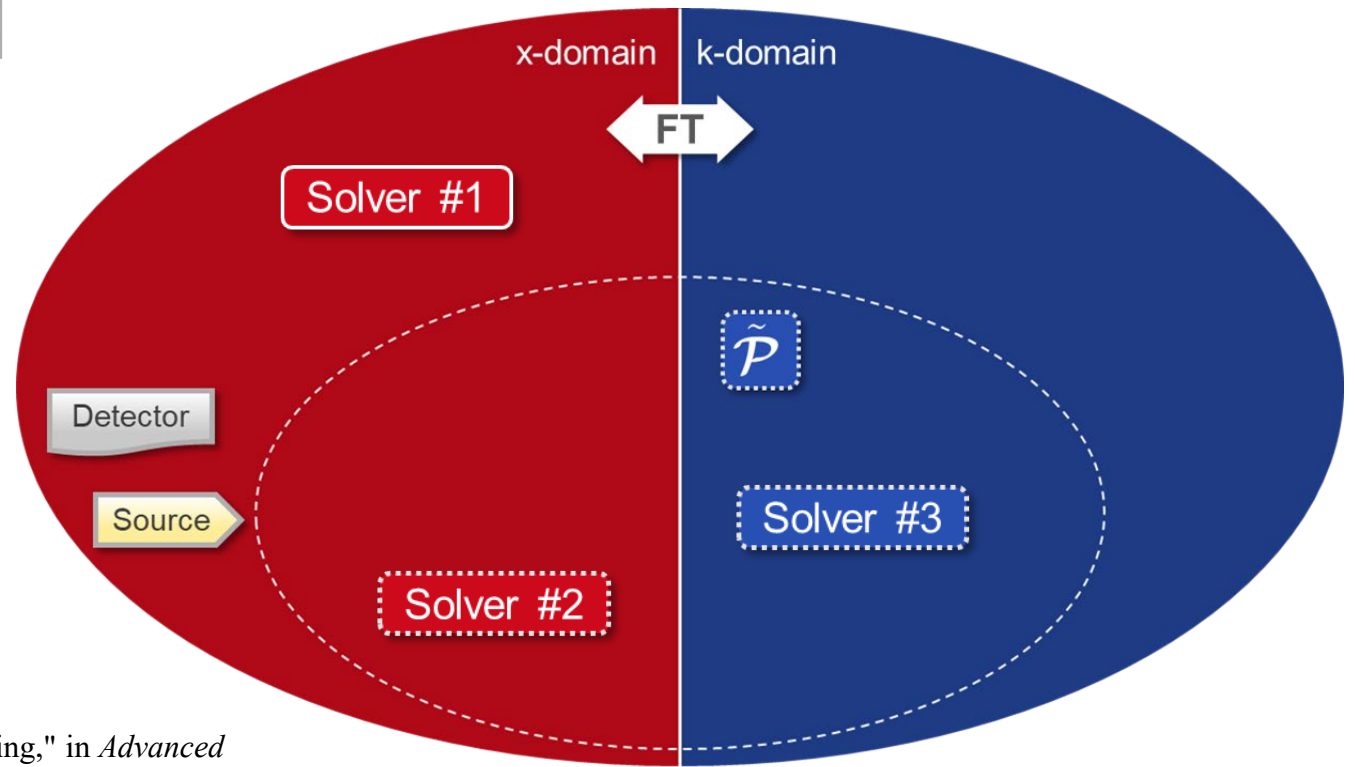


Consequences for Physical Optics System Modeling



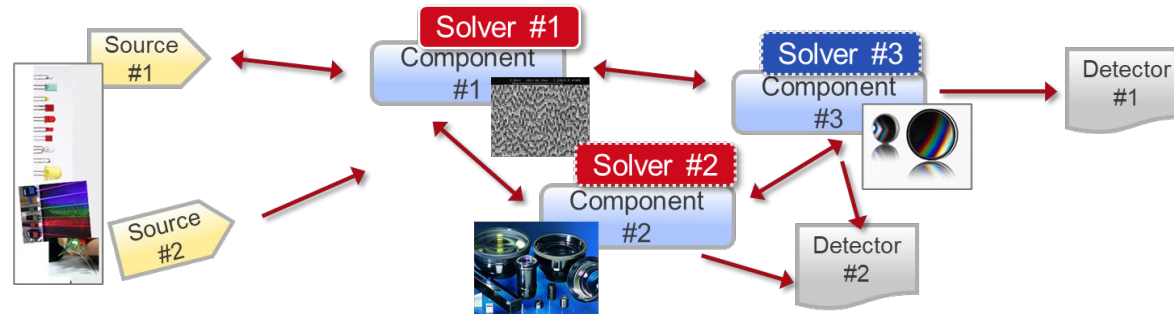
Instead of using one solver only ...

Connecting solvers is a key technology for physical-optics system modeling!

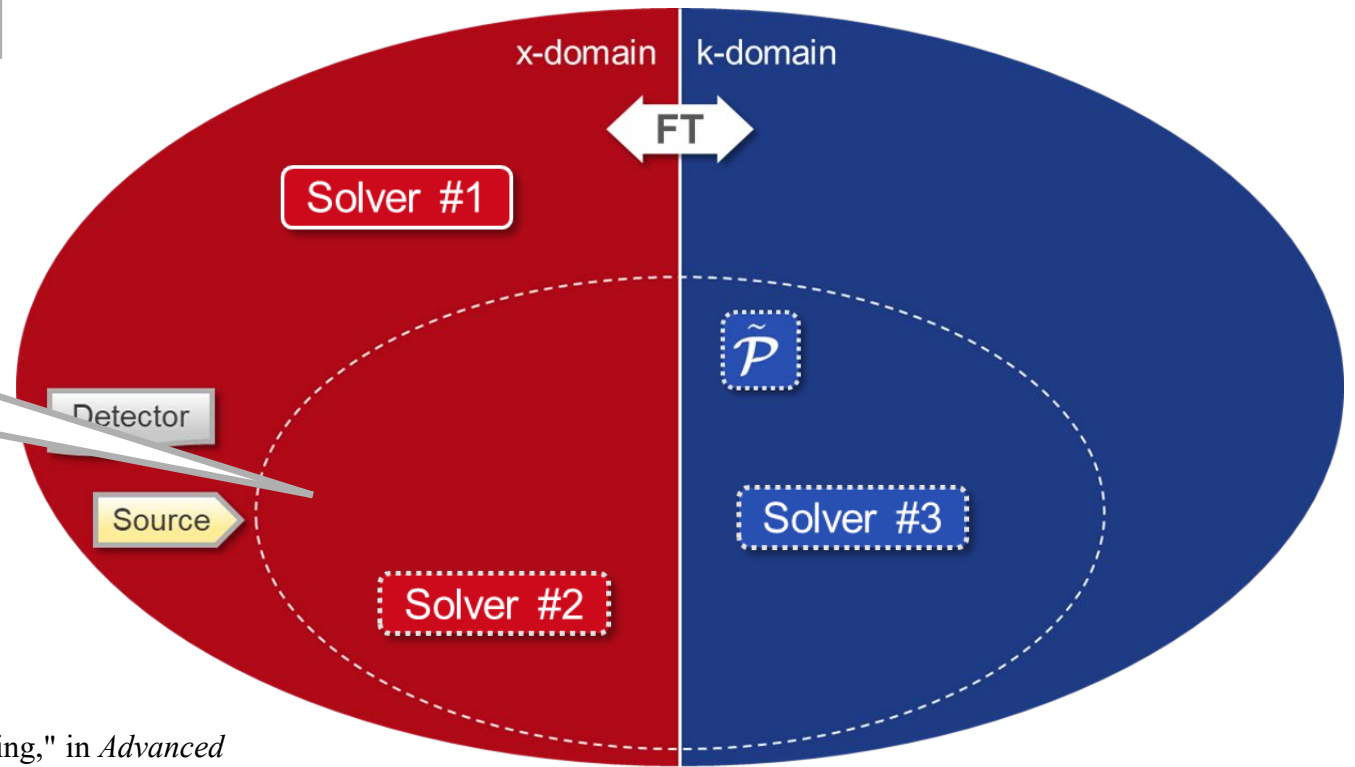


M. Kuhn, F. Wyrowski, and C. Hellmann, "Non-sequential Optical Field Tracing," in *Advanced Finite Element Methods and Applications*, T. Apel and O. Steinbach, eds., Lecture Notes in Applied and Computational Mechanics (Springer Berlin Heidelberg, 2013), Vol. 66, pp. 257–273.

Consequences for Physical Optics System Modeling

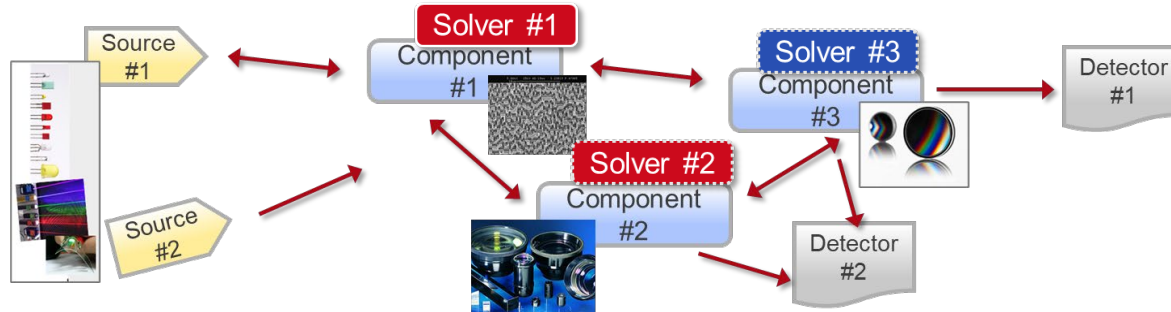


Include rigorous and approximated pointwise solver.

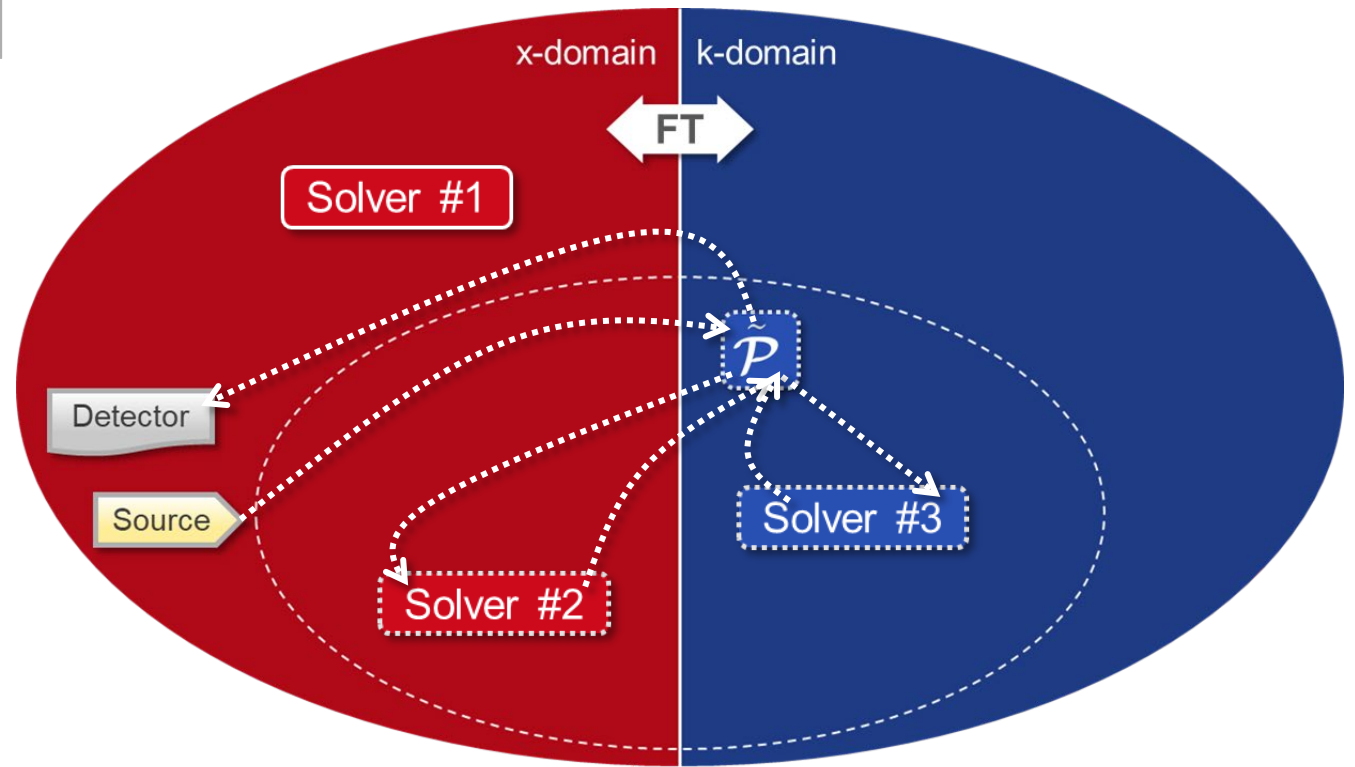


M. Kuhn, F. Wyrowski, and C. Hellmann, "Non-sequential Optical Field Tracing," in *Advanced Finite Element Methods and Applications*, T. Apel and O. Steinbach, eds., Lecture Notes in Applied and Computational Mechanics (Springer Berlin Heidelberg, 2013), Vol. 66, pp. 257–273.

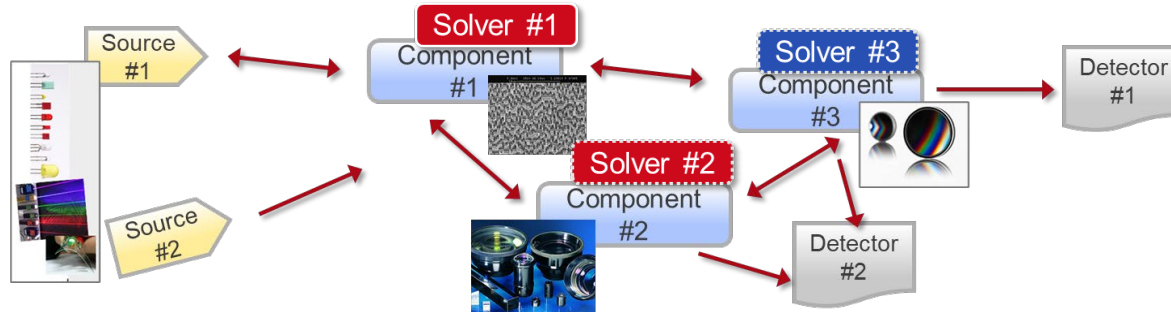
Consequences for Physical Optics System Modeling



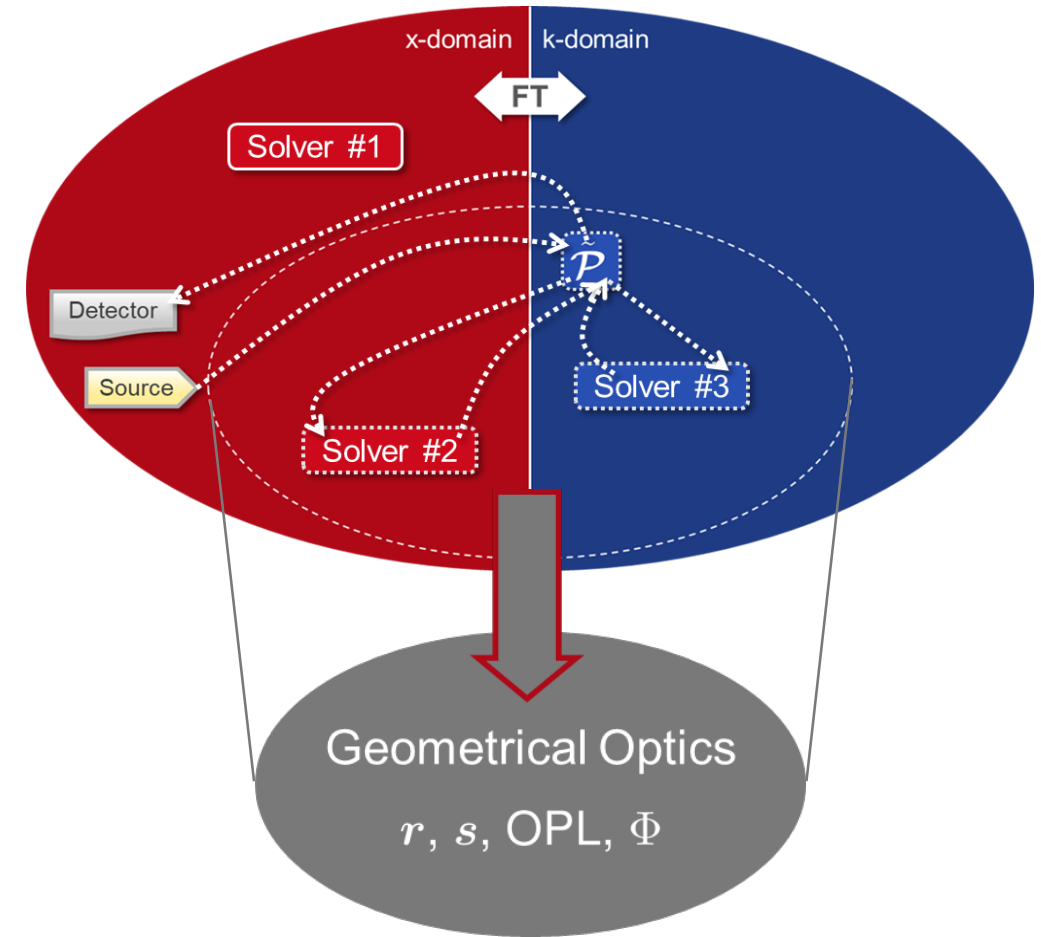
**Pointwise physical-optics
system modeling feasible.**



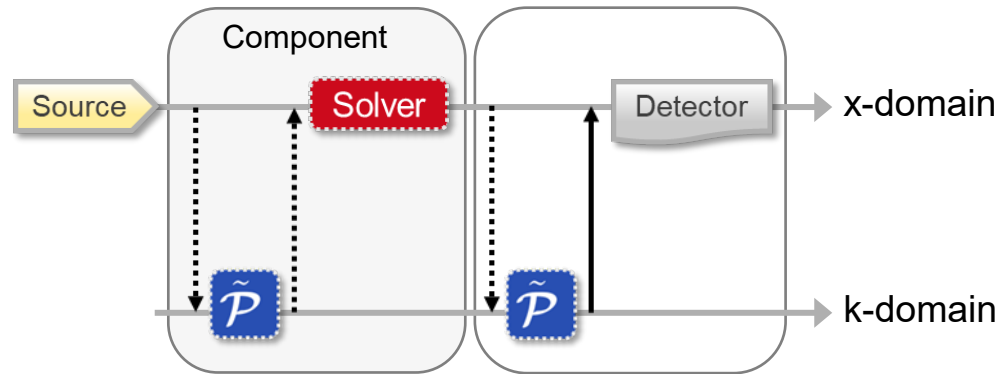
Consequences for Physical Optics System Modeling



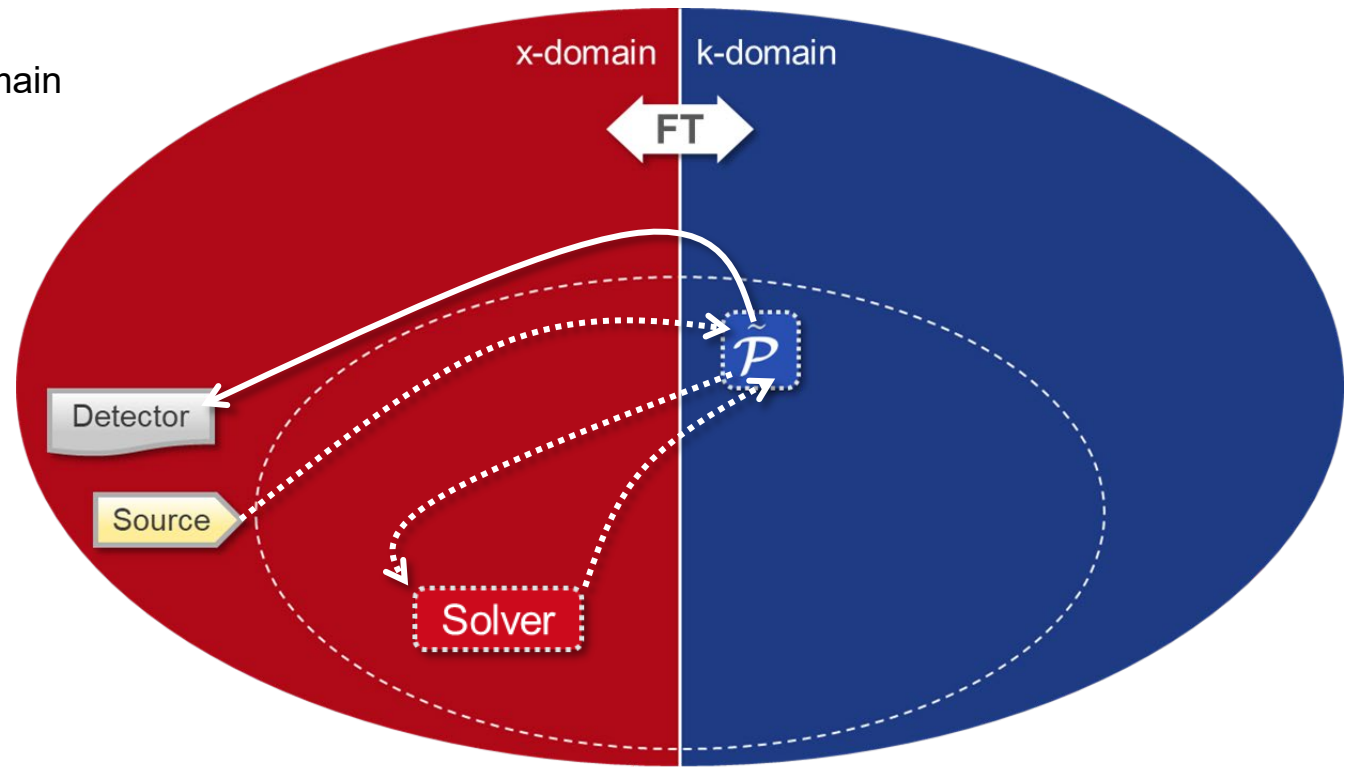
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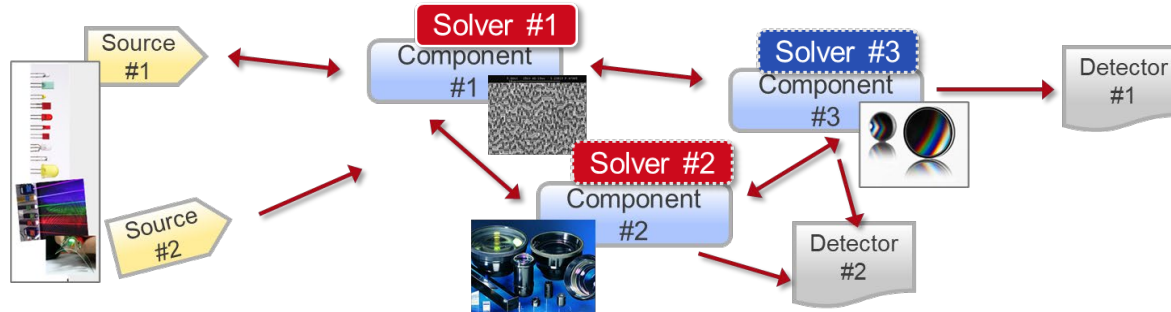
Modeling Diagrams



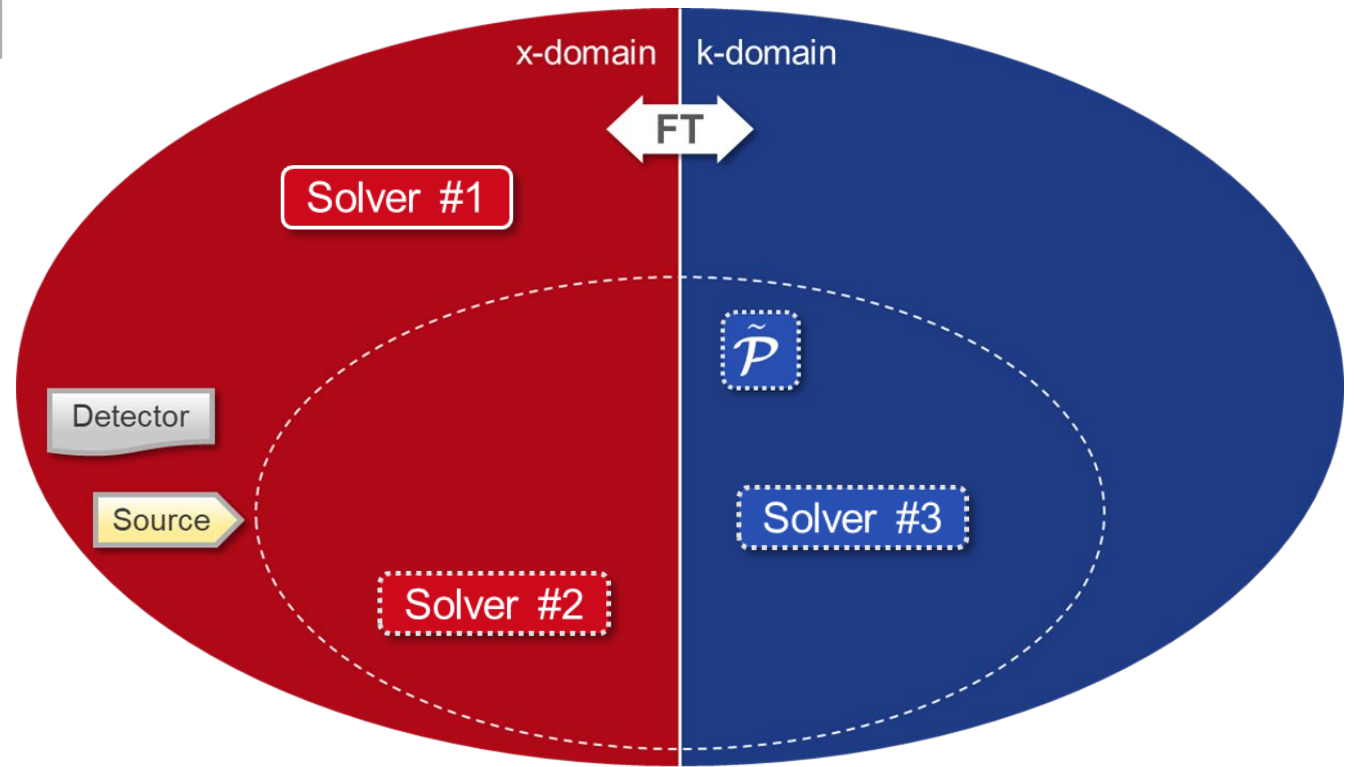
Types of illustrations of the connecting solvers technology.



Consequences for Physical Optics System Modeling



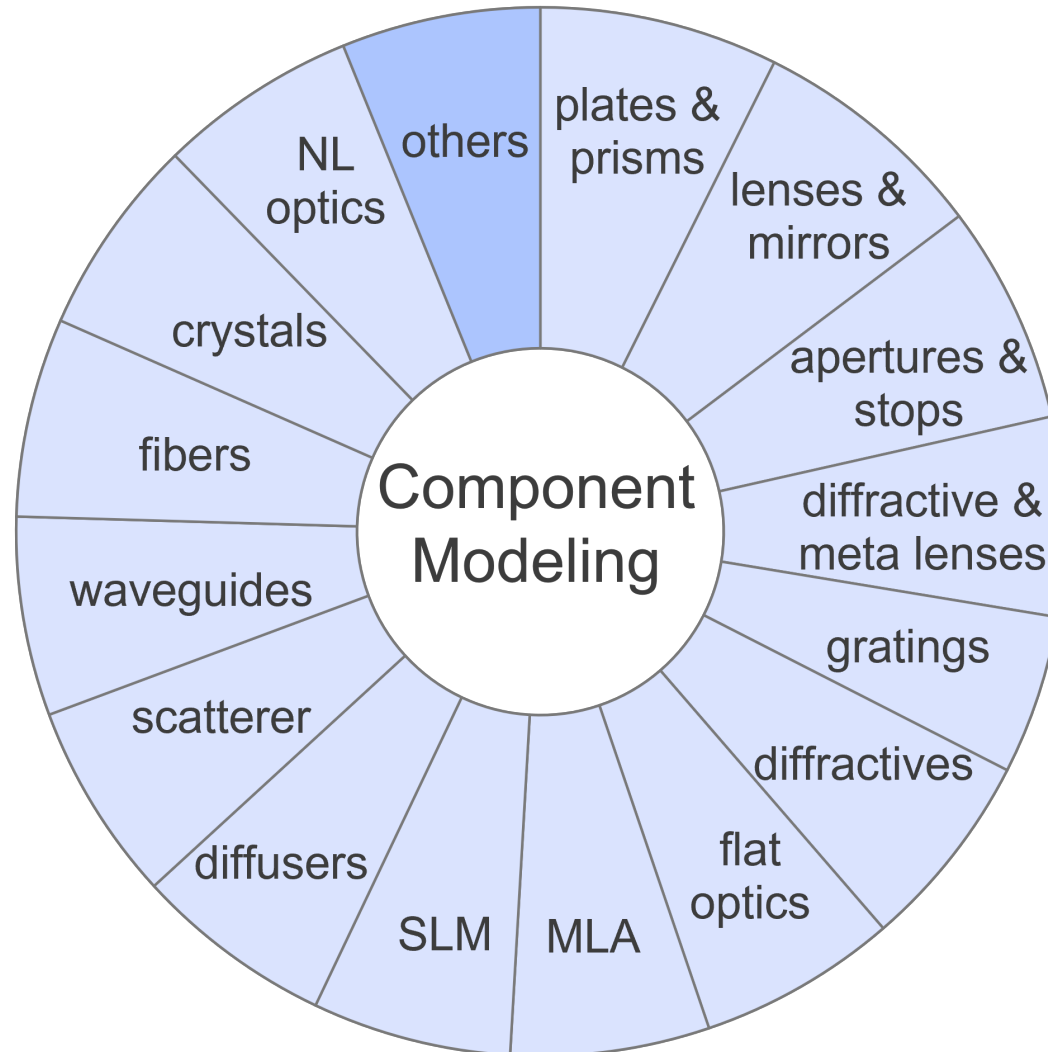
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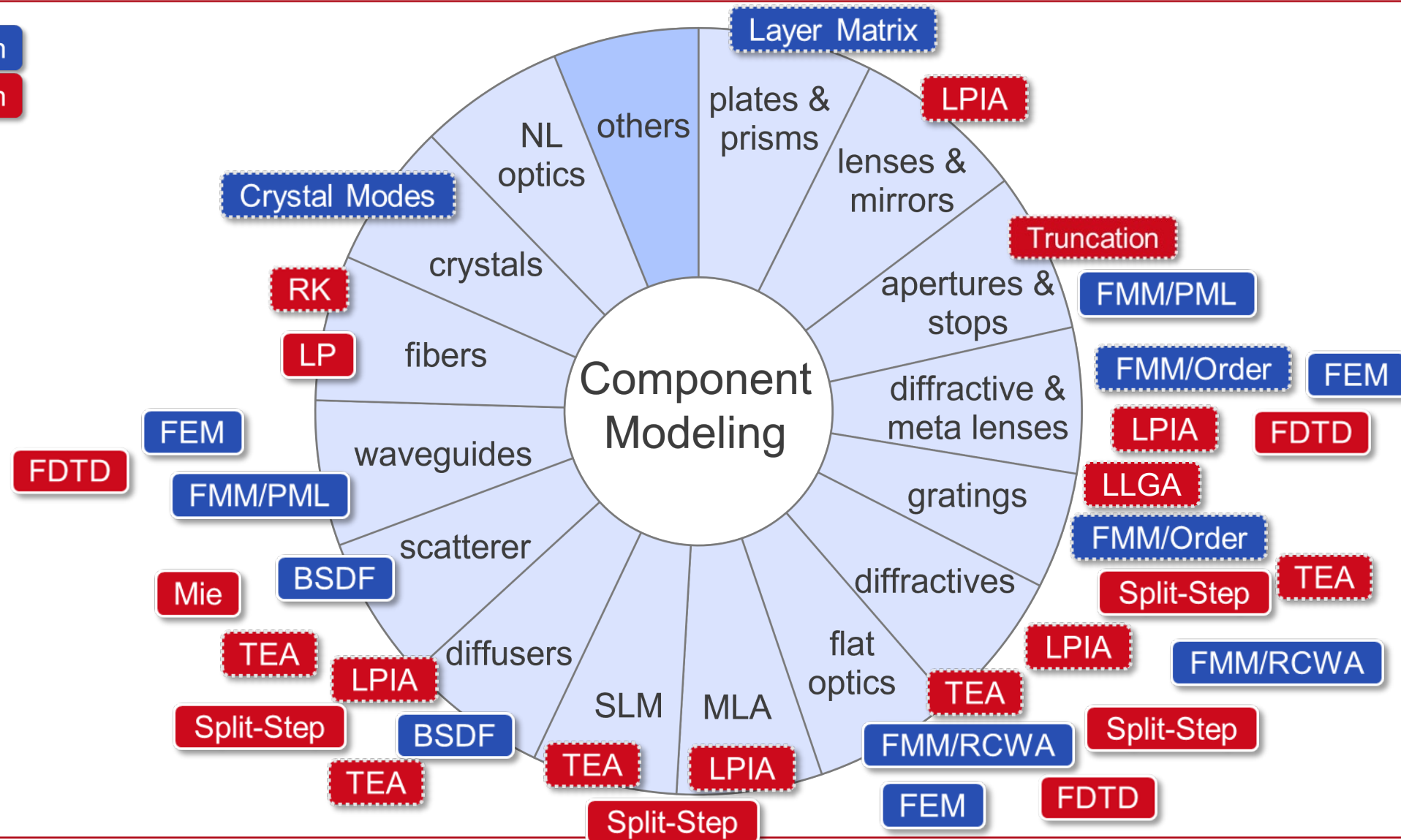
Suitable Solvers per Component

k-domain

x-domain



Solvers per Component



Solvers per Component

BSDF Bidirectional Scattering Distribution Function

FDTD Finite Different Time Domain

FEM Finite Element Method

FMM Fourier Modal Method

FMM/Order FMM with mode decomposition

FMM/PML FMM with Perfect Matched Layer

LLGA Local Linear Grating Approximation

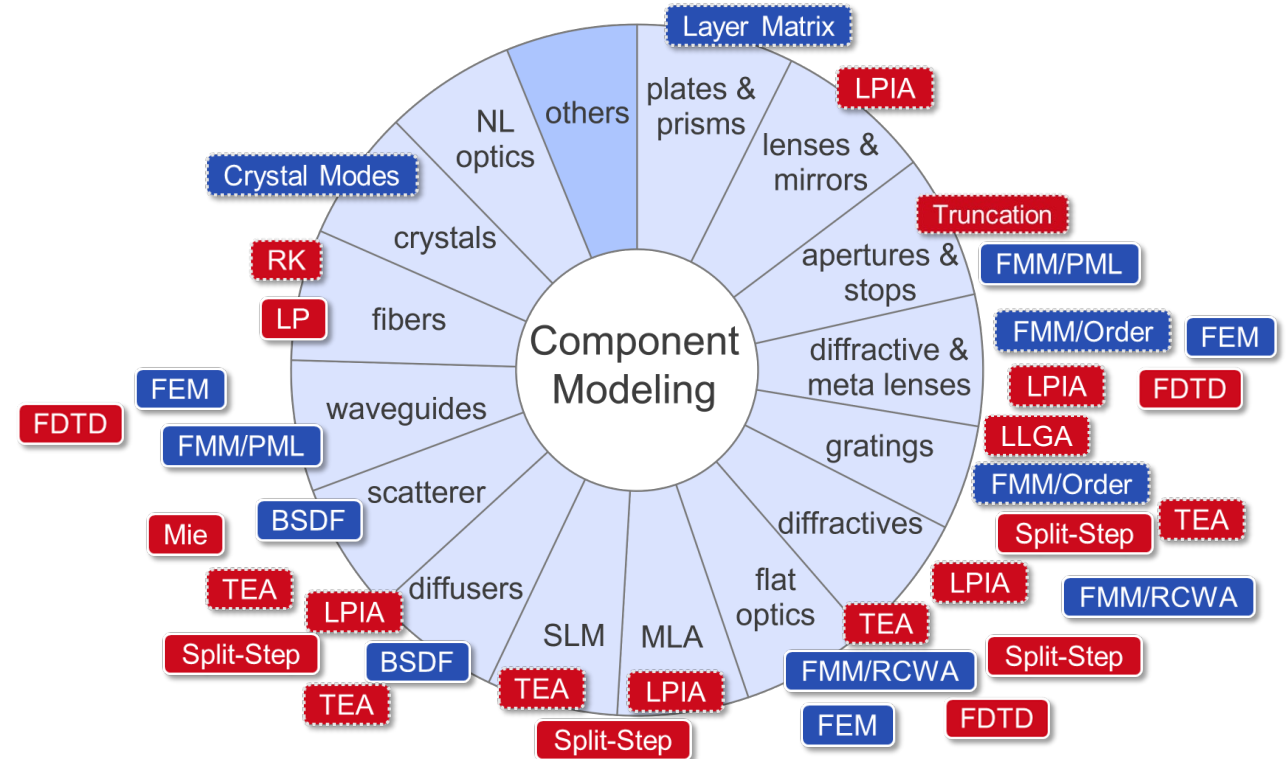
LP Linearly Polarized mode solver

LPIA Local Plane Interface Approximation

RCWA Rigorous Coupled Wave Approach

RK Runge-Kutta solver for GRIN media

TEA Thin Element Approximation



A. V. Pfeil and F. Wyrowski, "Wave-optical structure design with the local plane-interface approximation," *J. Mod. Optics* **47**, 2335–2350 (2000).

A. v Pfeil, F. Wyrowski, A. Drauschke, and H. Aagedal, "Analysis of optical elements with the local plane-interface approximation," *Appl. Opt.* **39**, 3304–3313 (2000).

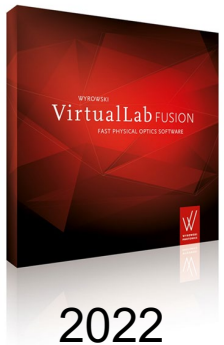
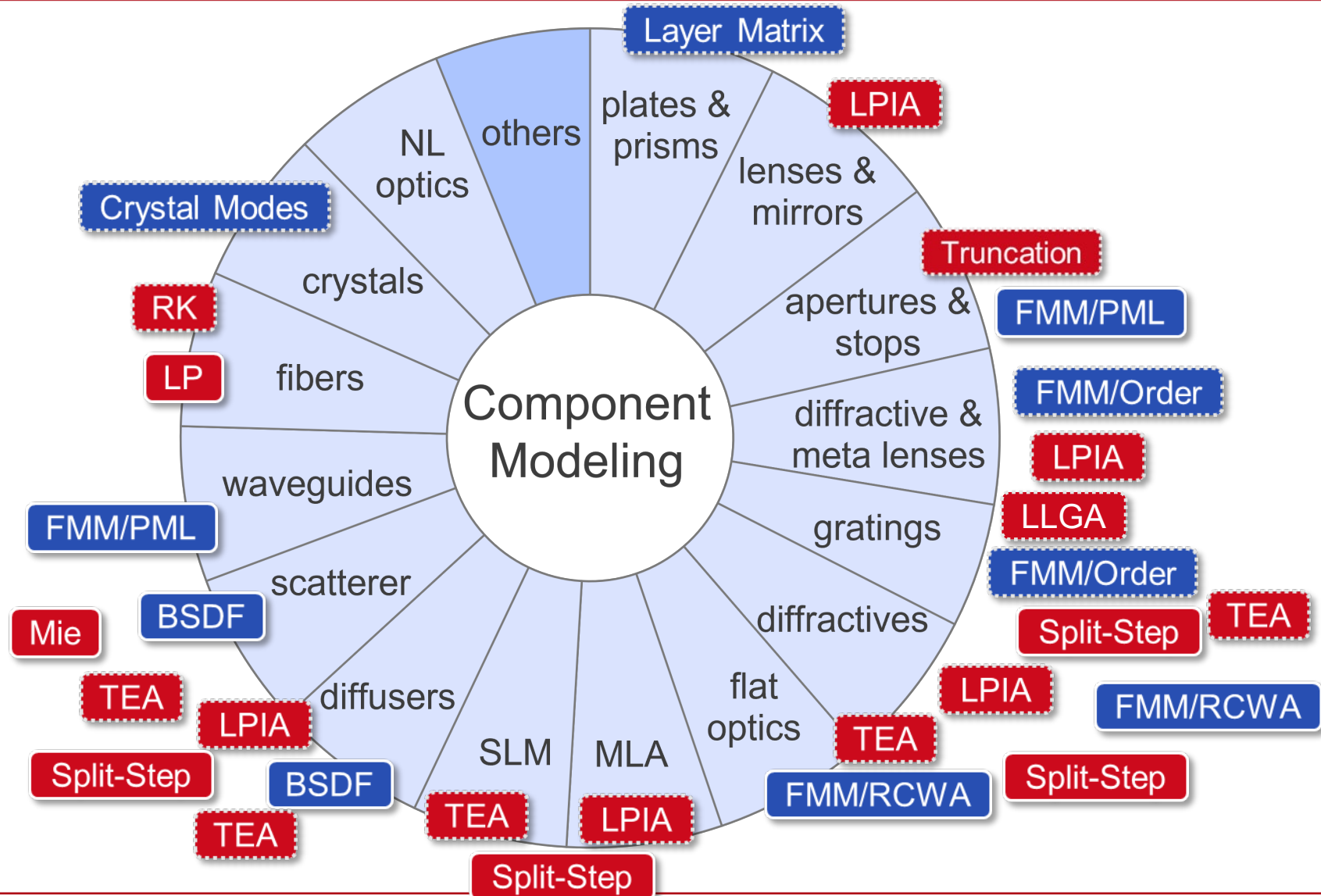
R. Shi, C. Hellmann, and F. Wyrowski, "Physical-optics propagation through curved surfaces," *J. Opt. Soc. Am. A* **36**, 1252 (2019).

LPIA

Solvers per Component

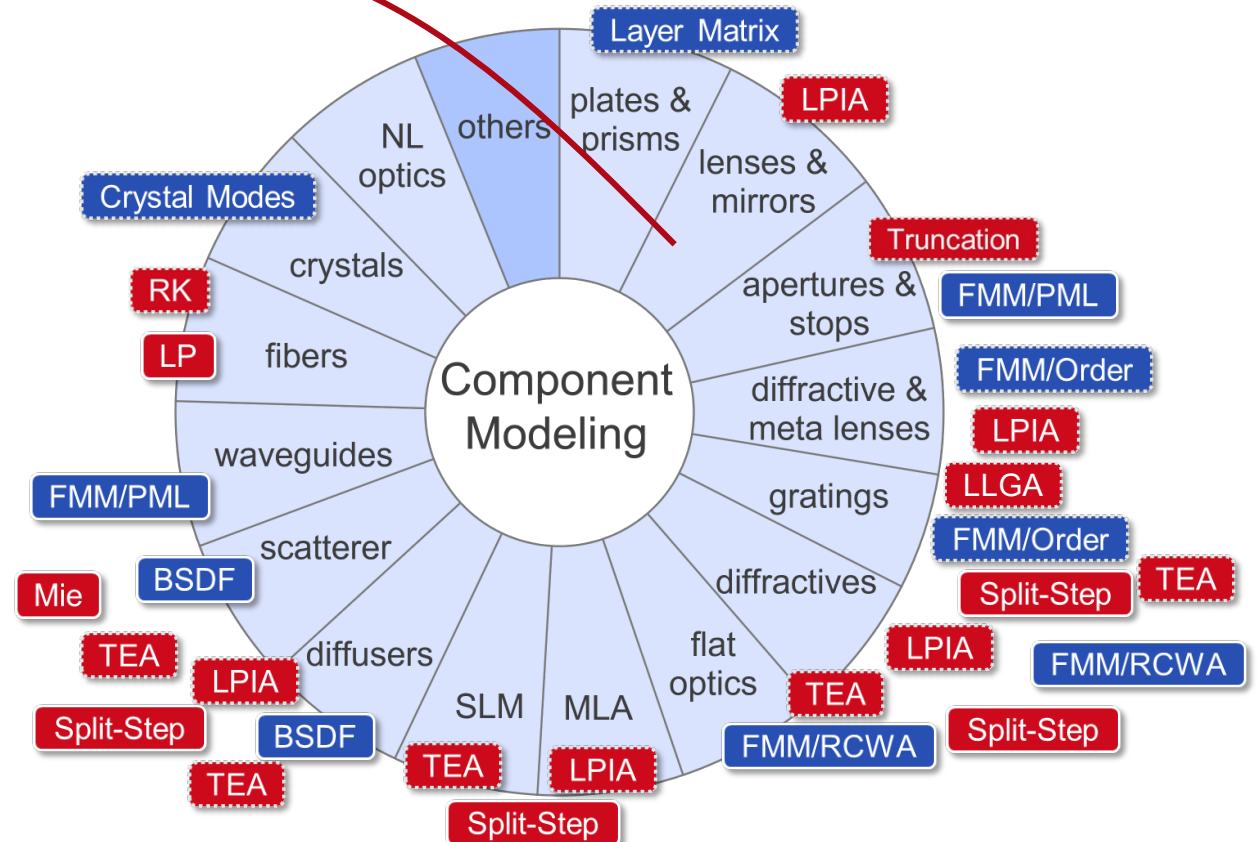
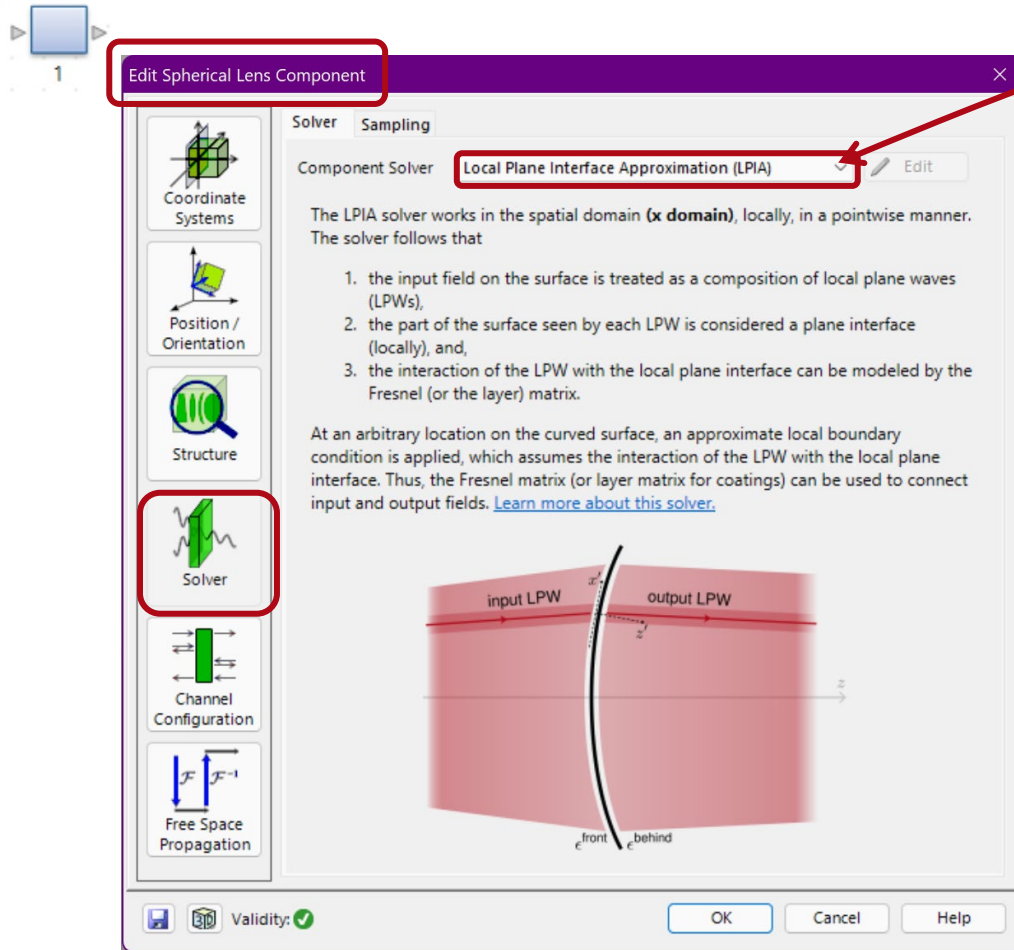
k-domain

x-domain

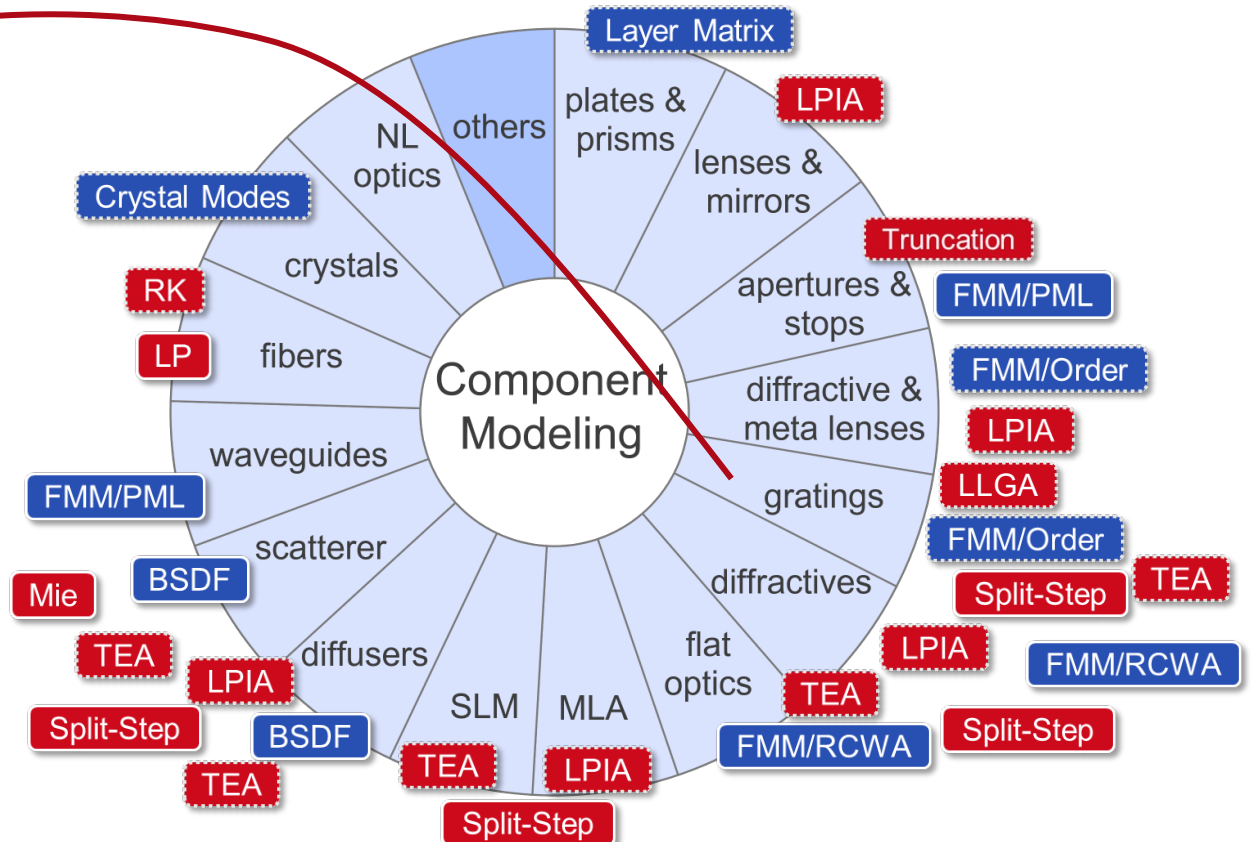
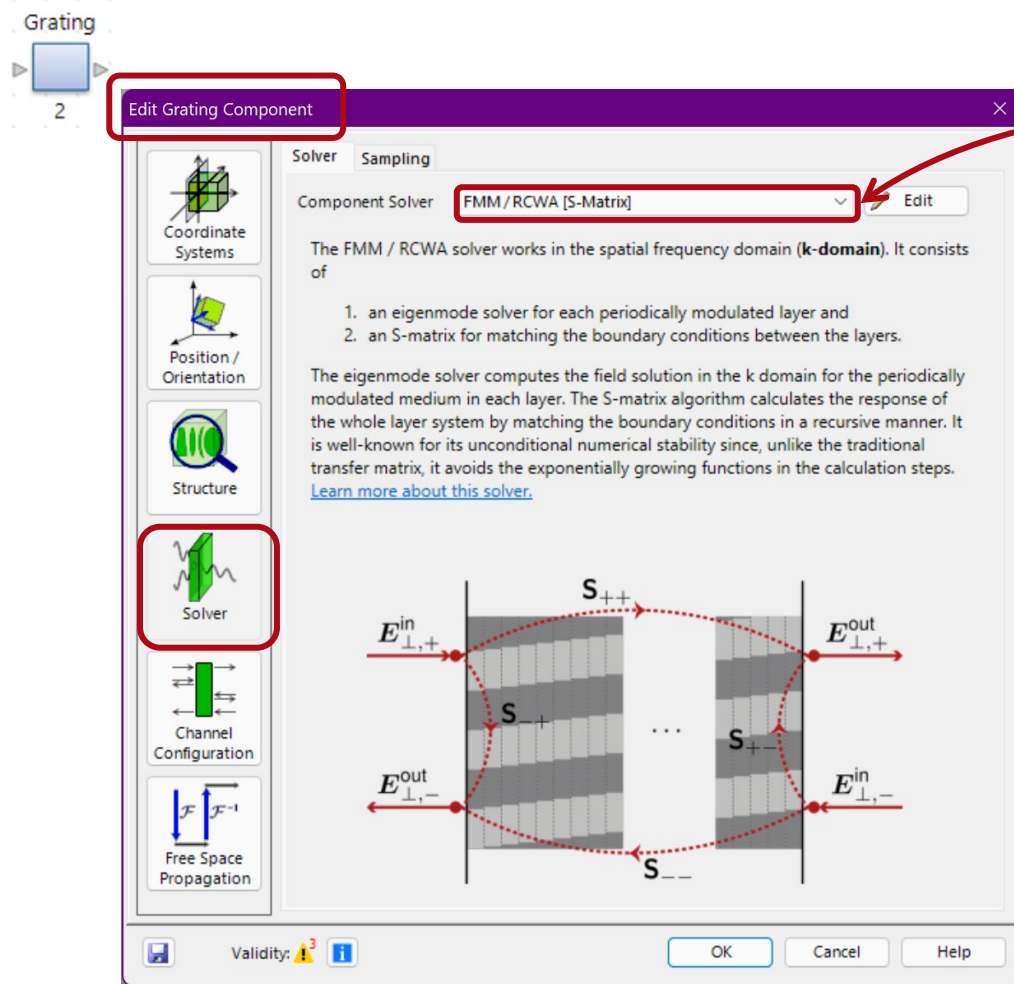


Solvers per Component

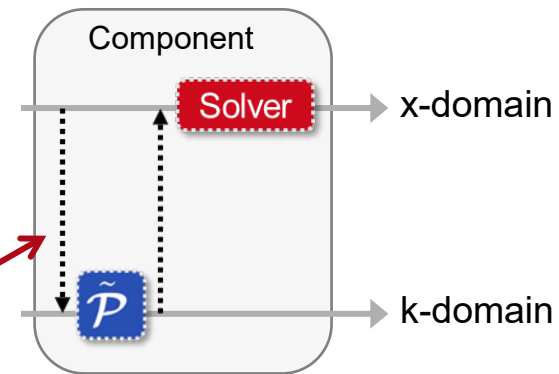
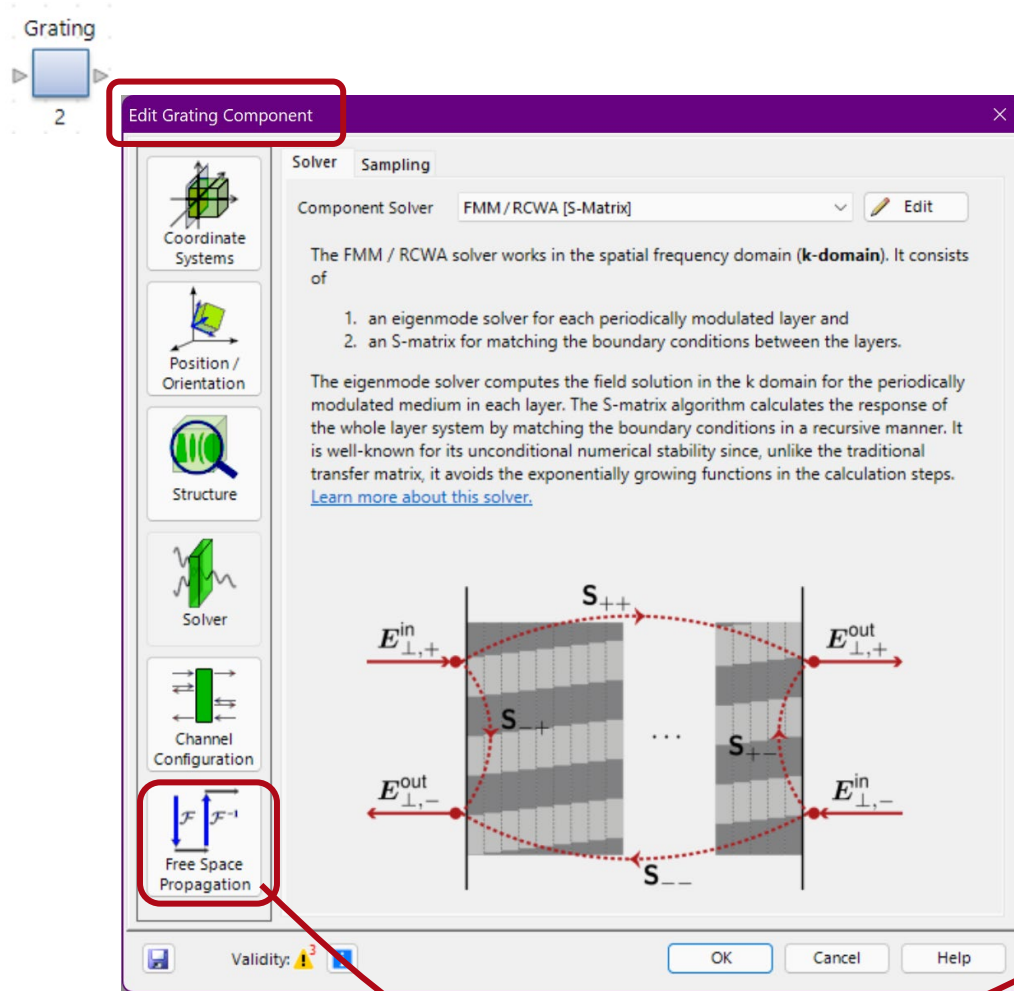
Spherical Lens



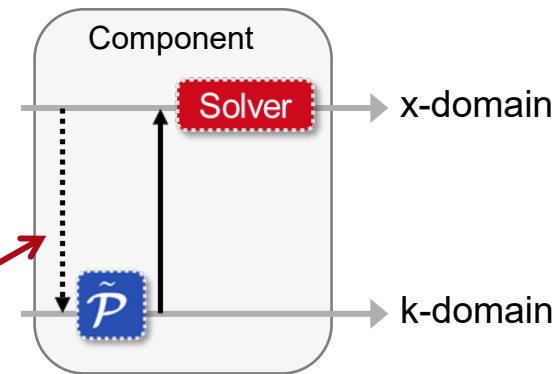
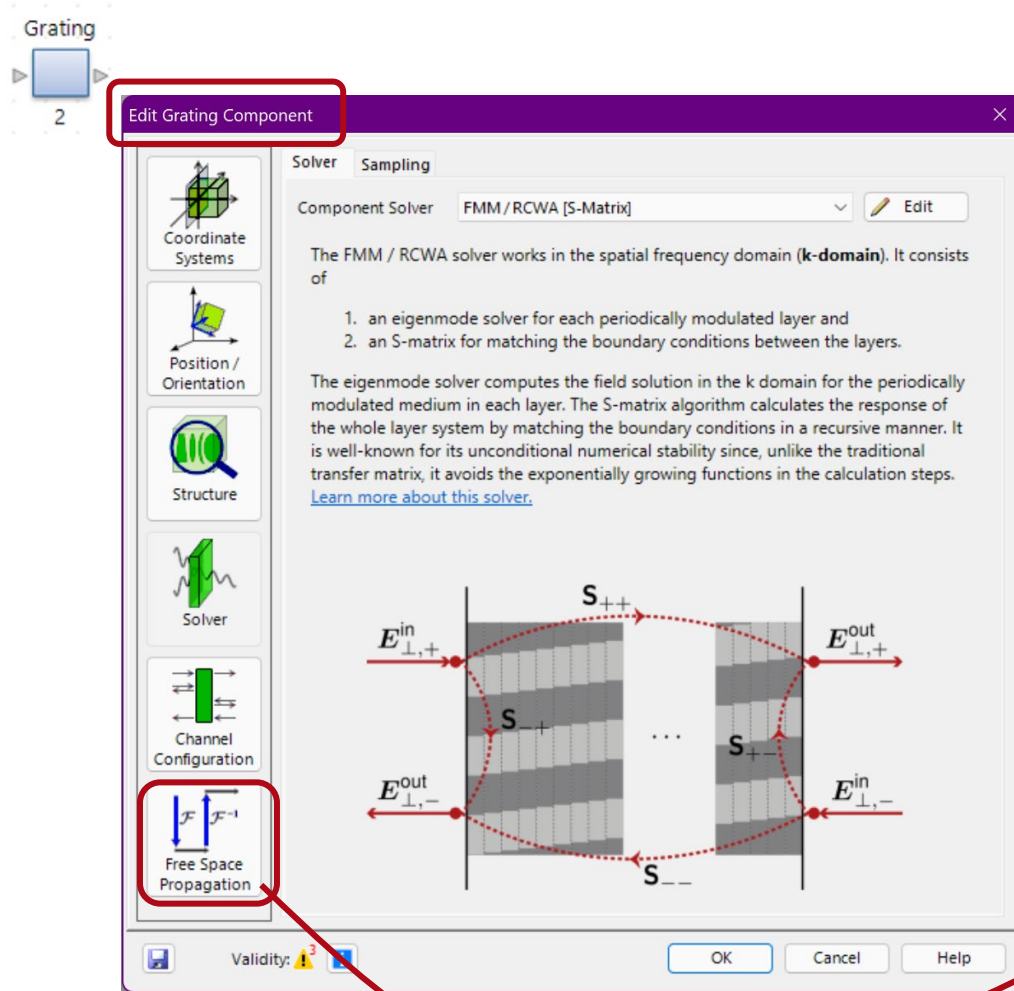
Solvers per Component



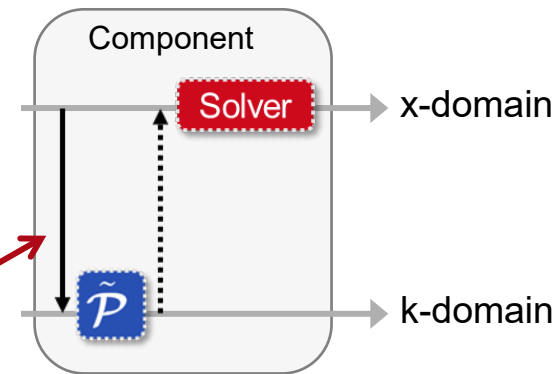
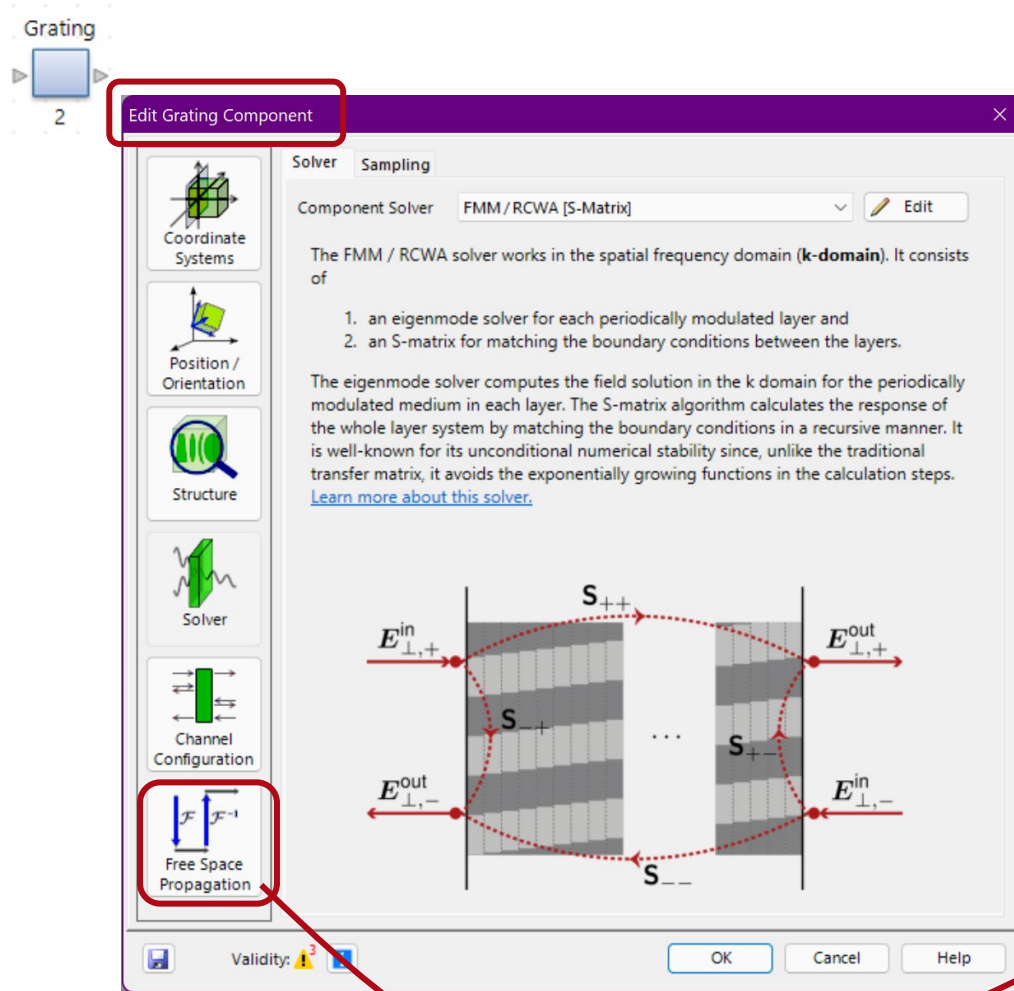
Propagation to Component Settings: Fourier Transforms



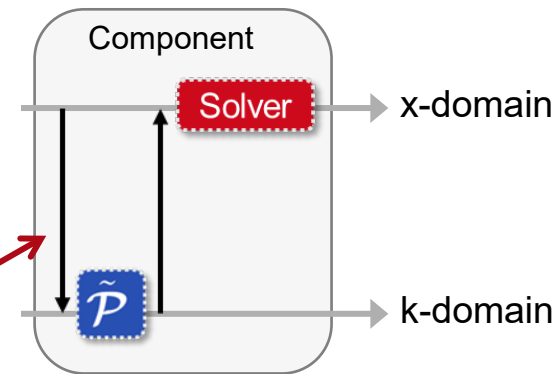
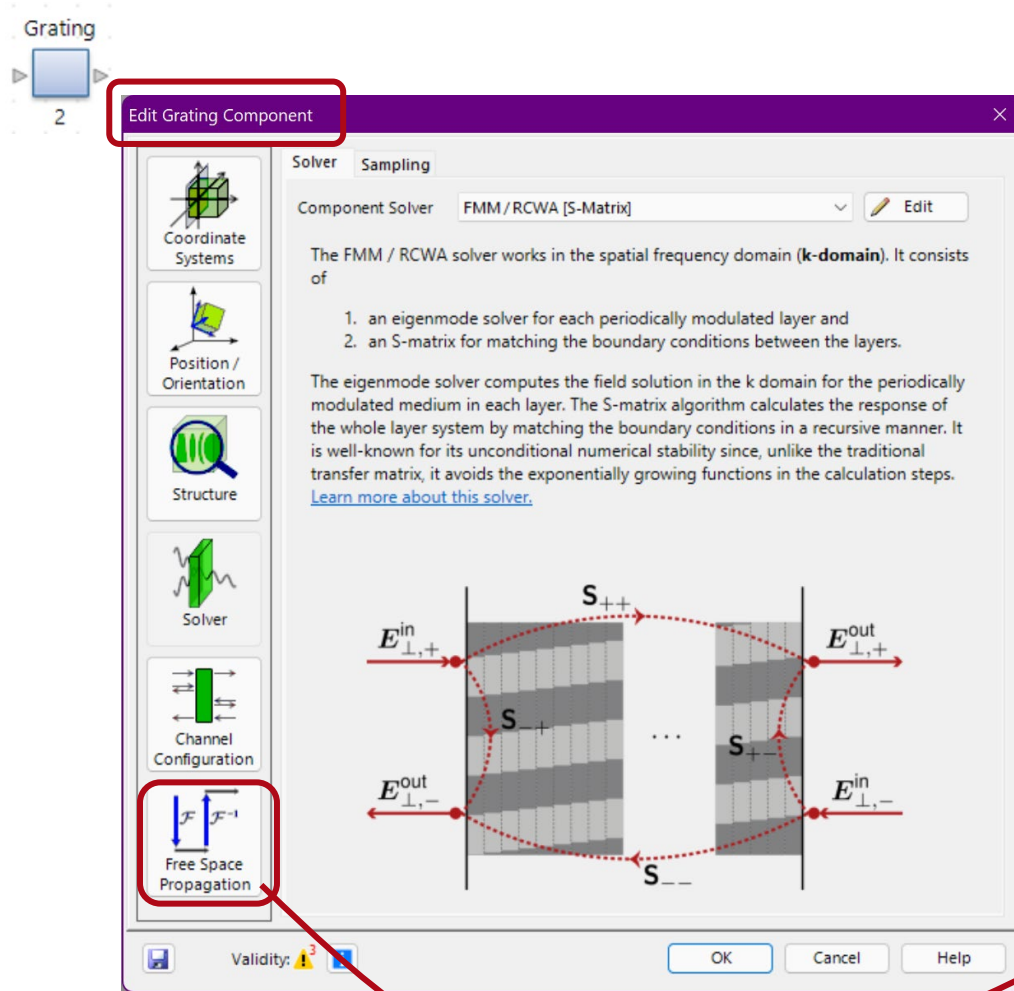
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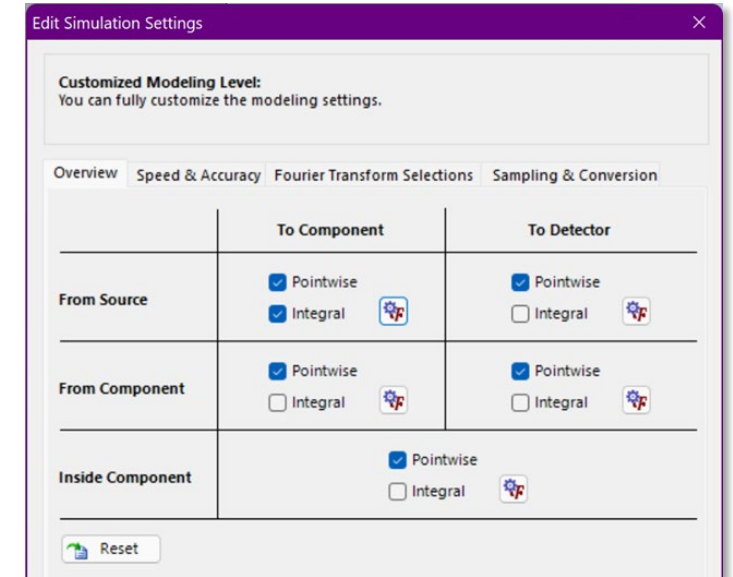
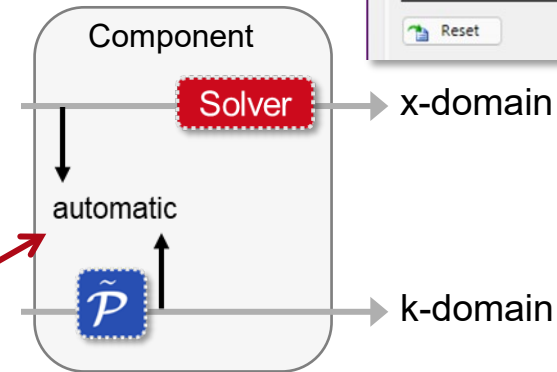
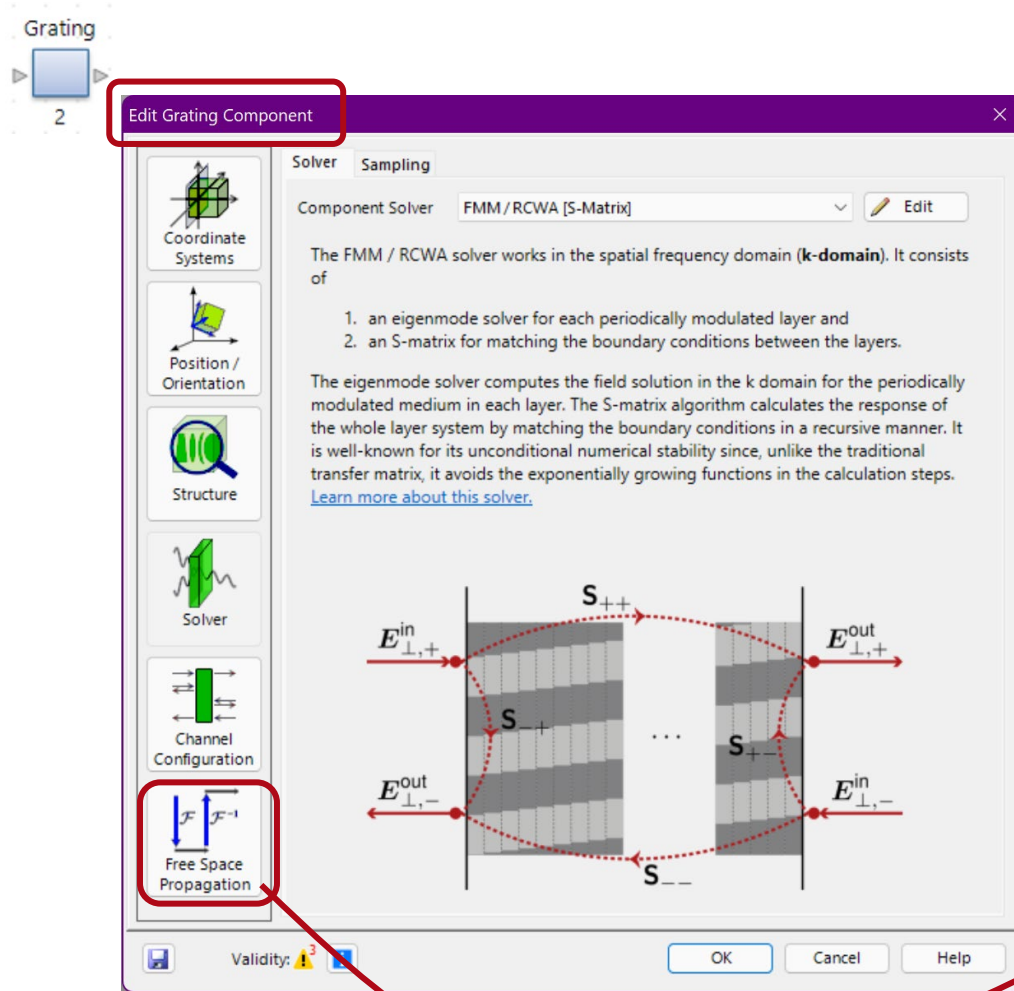
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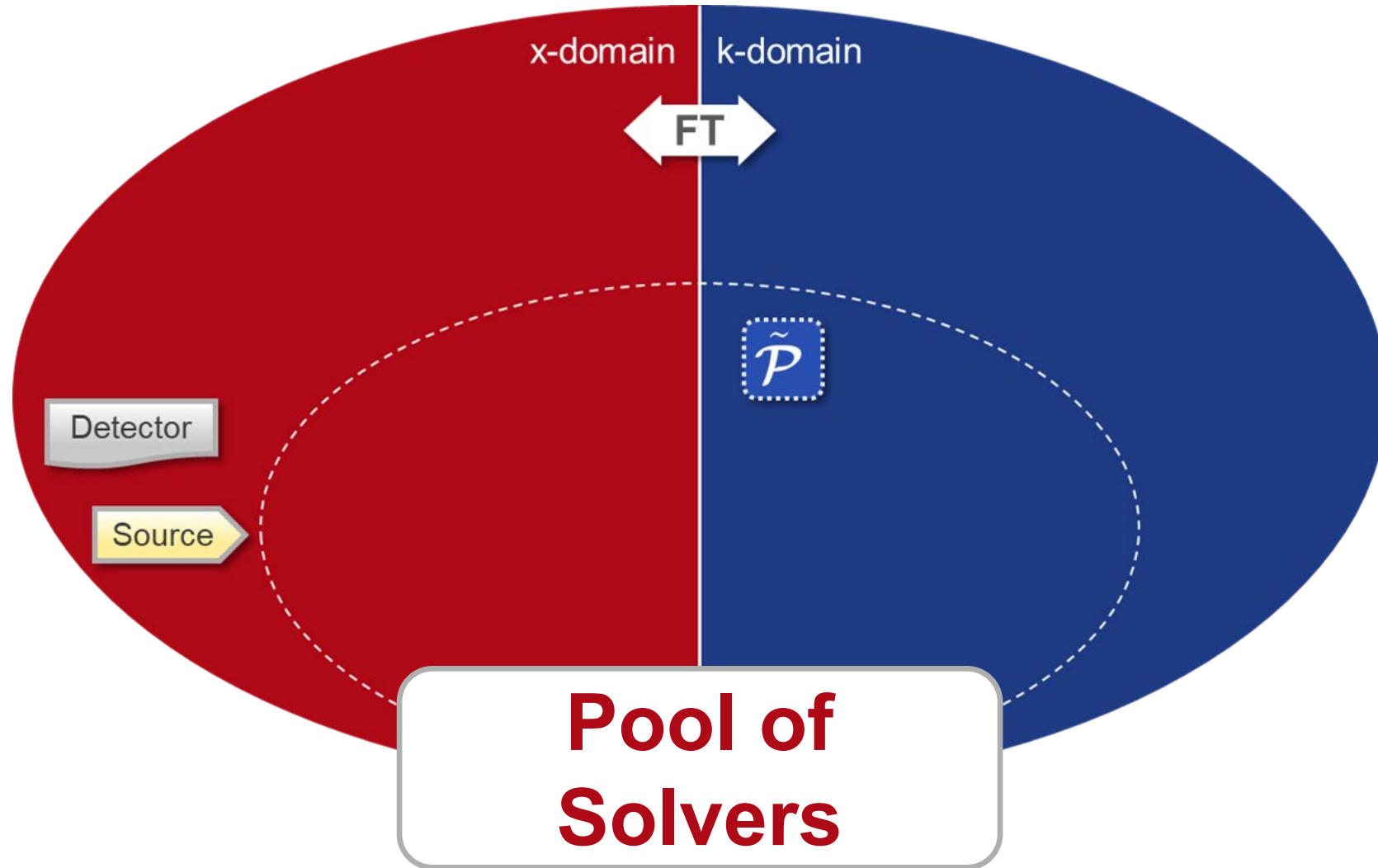
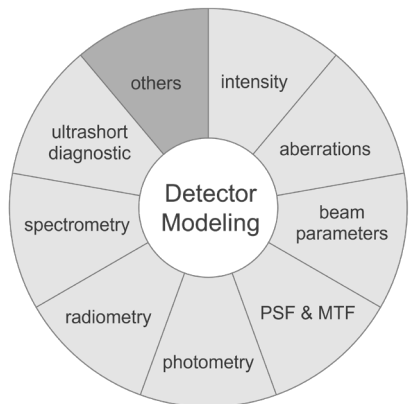
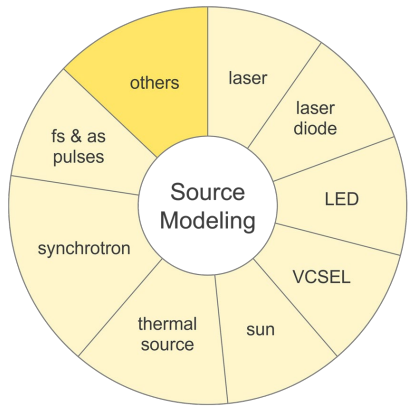
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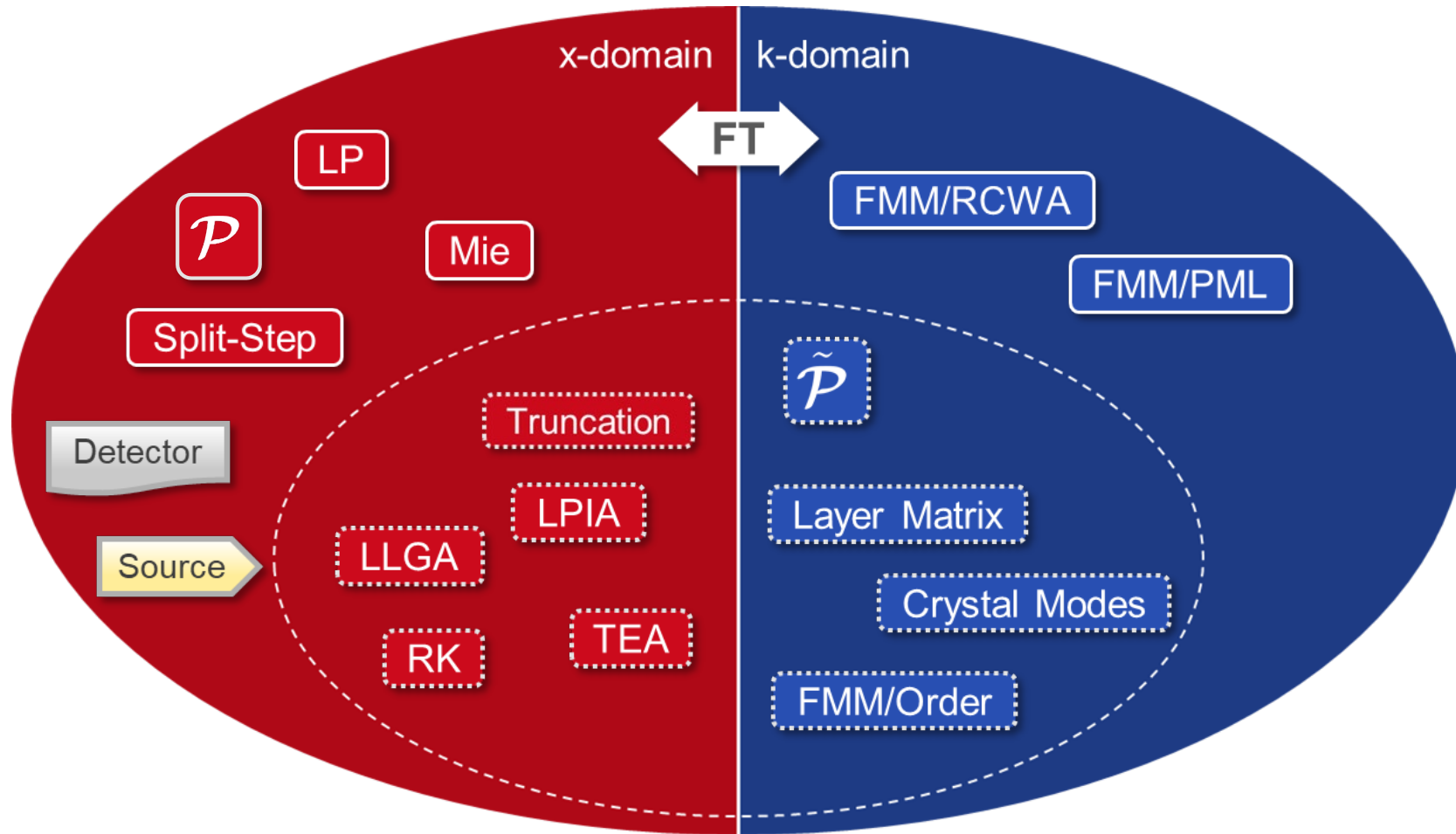
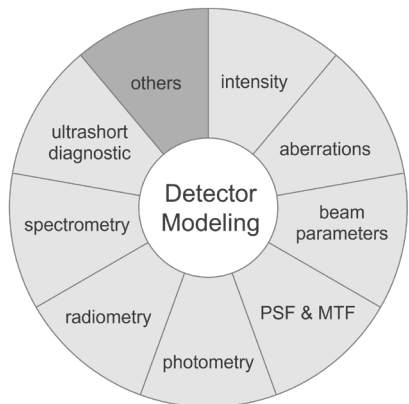
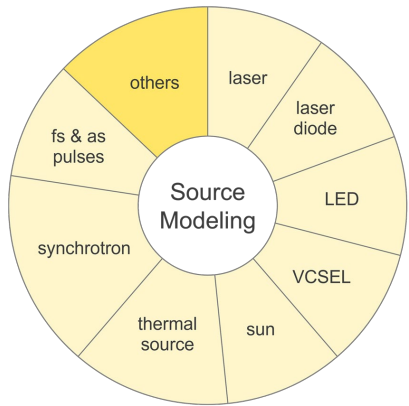
Propagation to Component Settings: Fourier Transforms



Connecting Solvers



Connecting Solvers

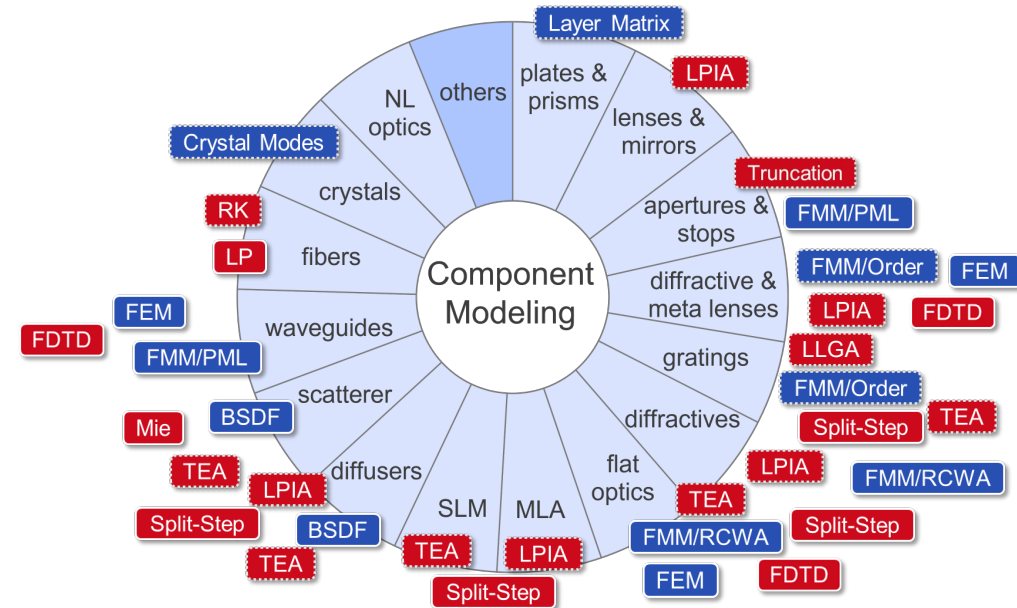
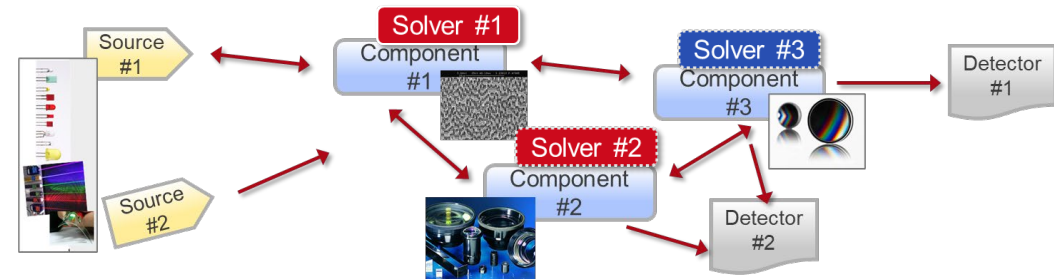


Connecting Solvers

- Build the system by selecting and positioning components.
- Select the Fourier transforms.
- Customize settings on demand.



- Software evaluates all relevant lightpaths through the system based on the 3D system configuration.
- Software knows and evaluates all lightpaths by connecting solvers in a non-sequential way.

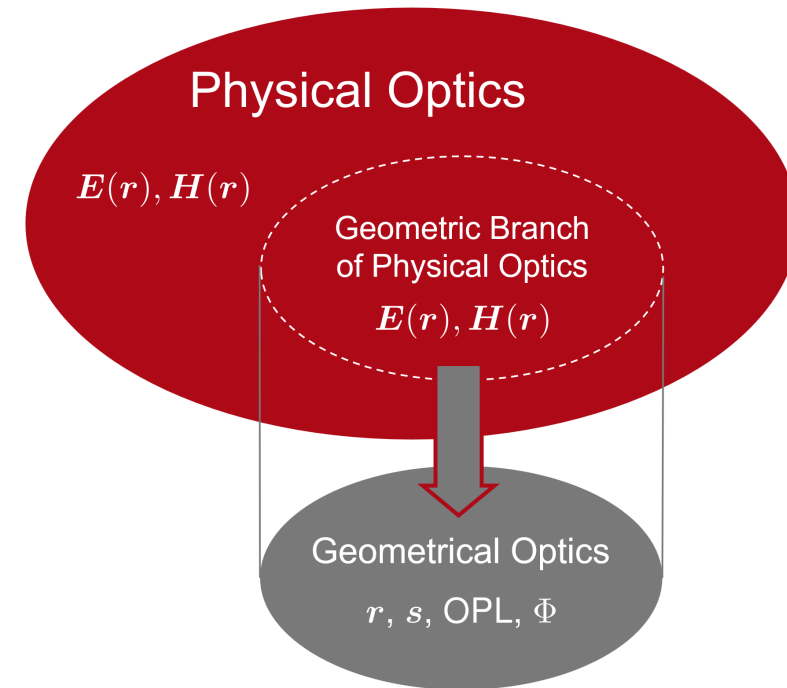
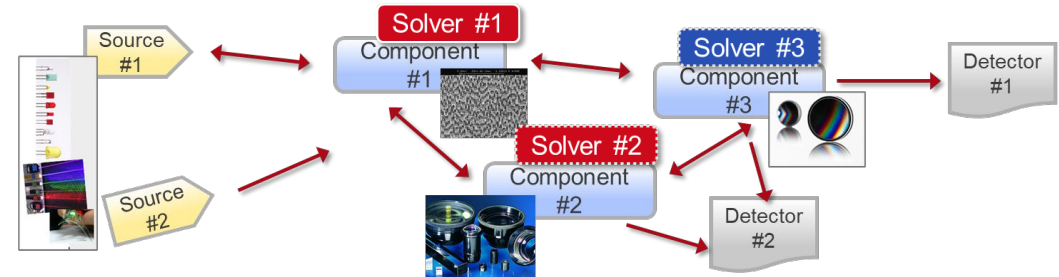


Connecting Solvers

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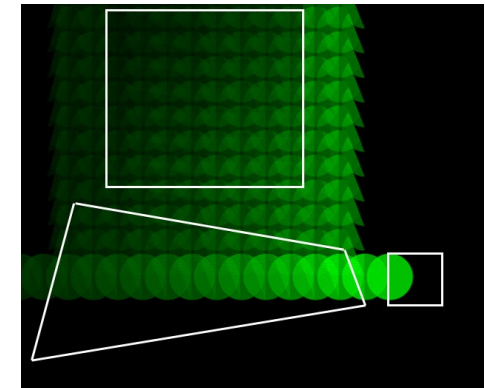
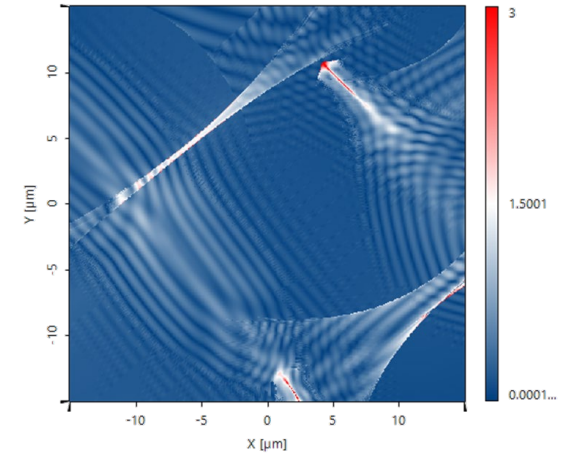
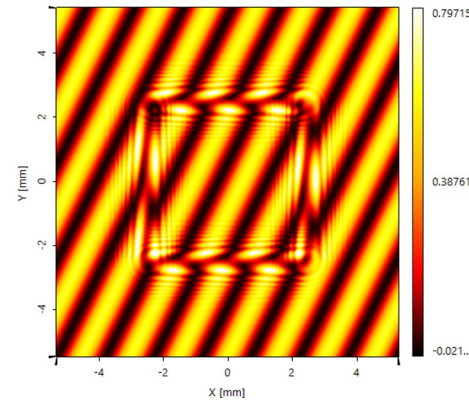
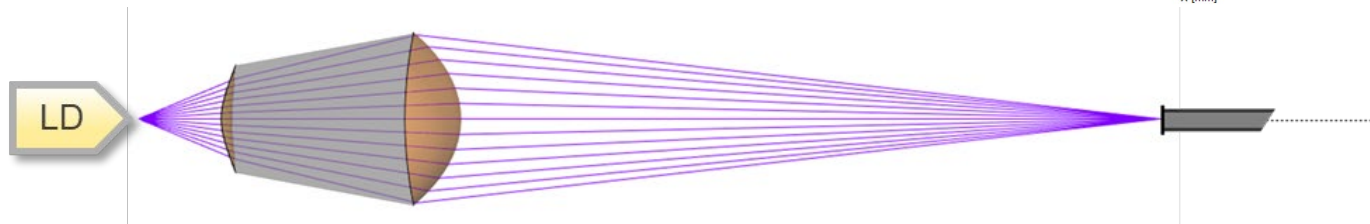


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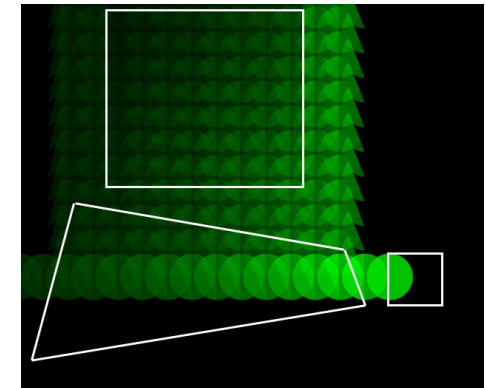
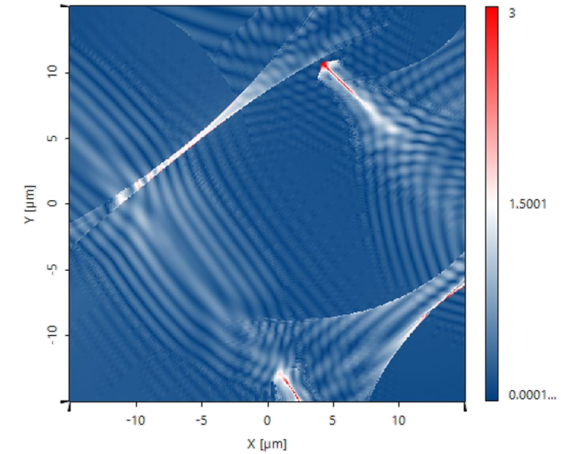
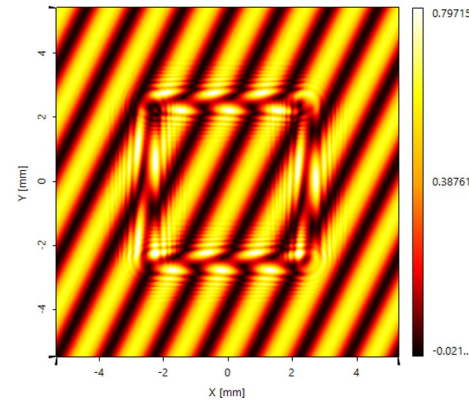
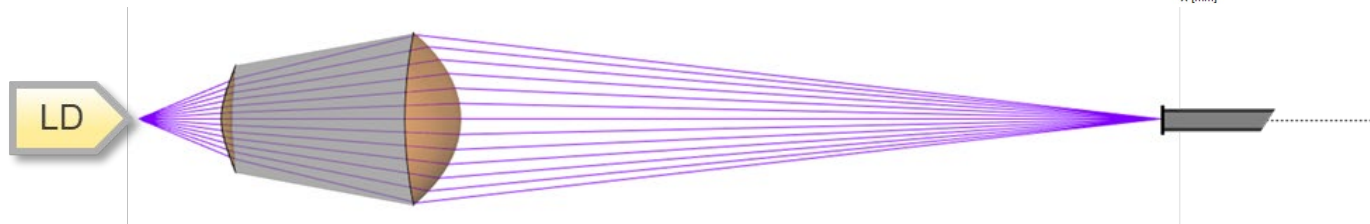
Content Overview

- Introduction to a unified approach in optical modeling
- **Theoretical considerations on physical optics modeling**
- Modeling examples
 - Talk
 - Follow-up material

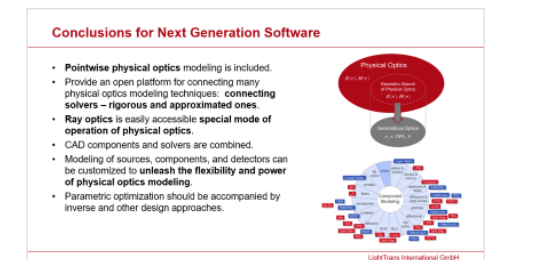
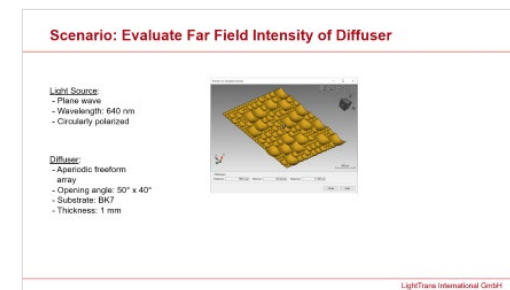
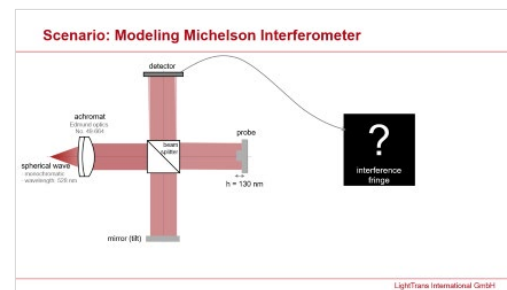
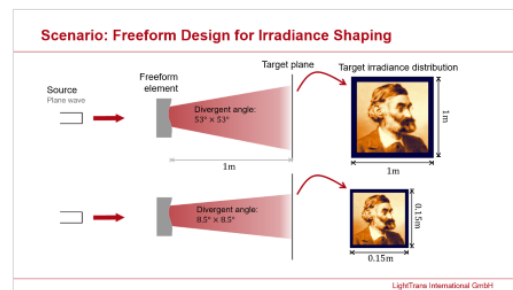
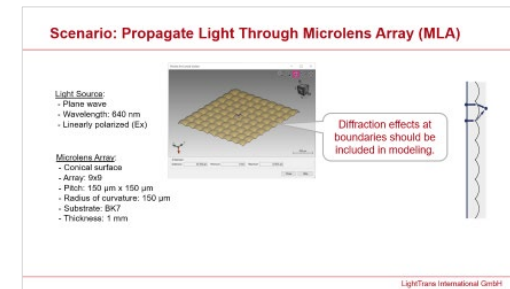
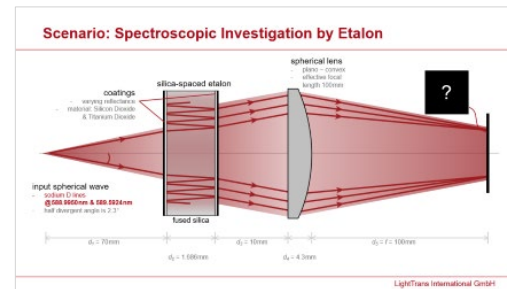
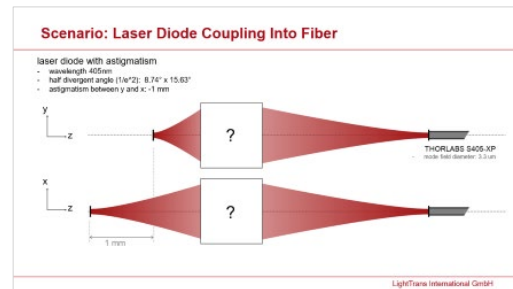
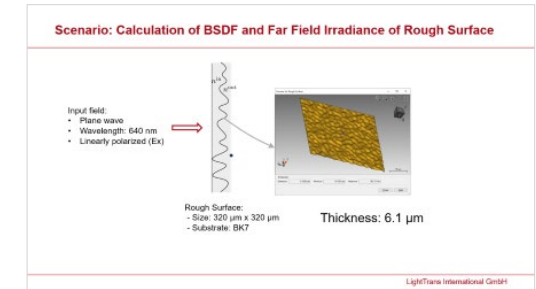
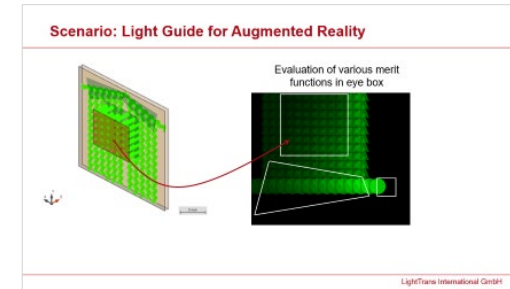
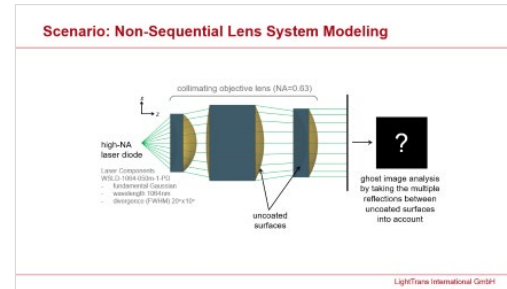
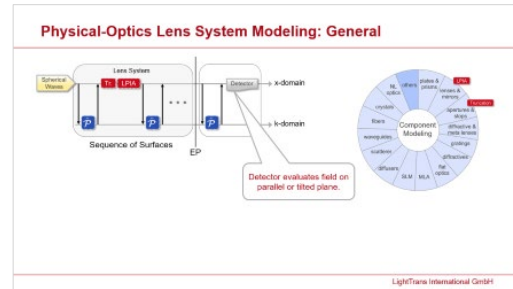


Content Overview

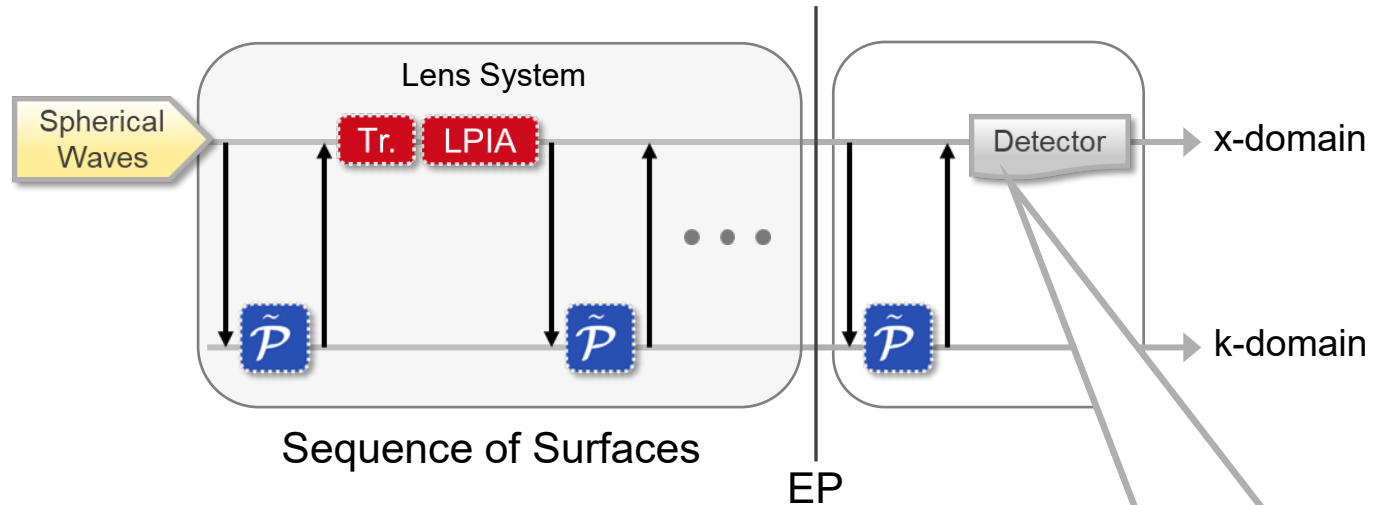
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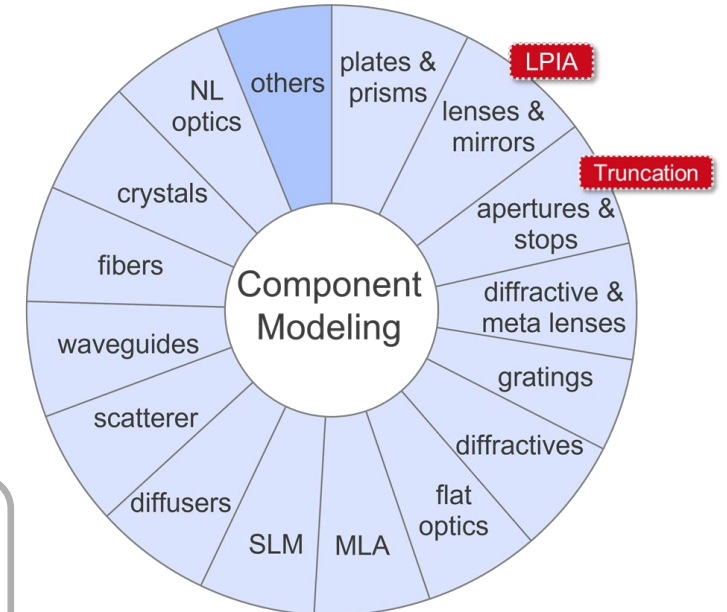
Modeling and Design Examples



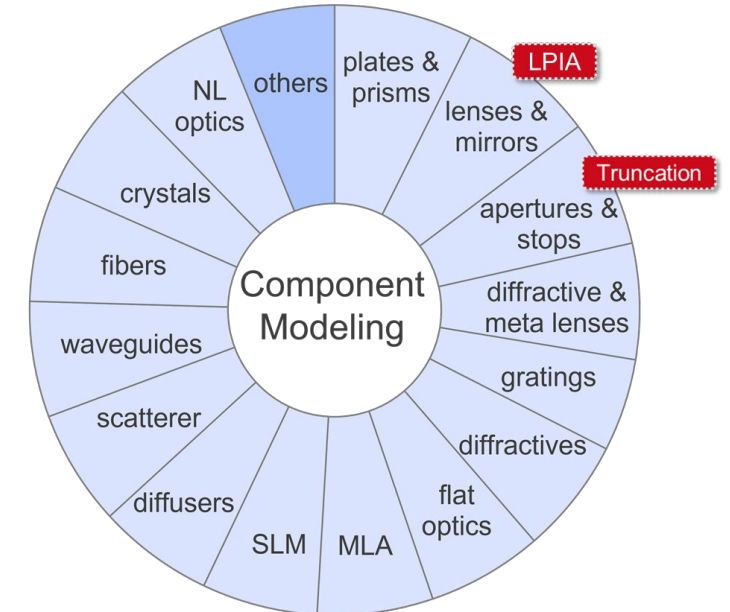
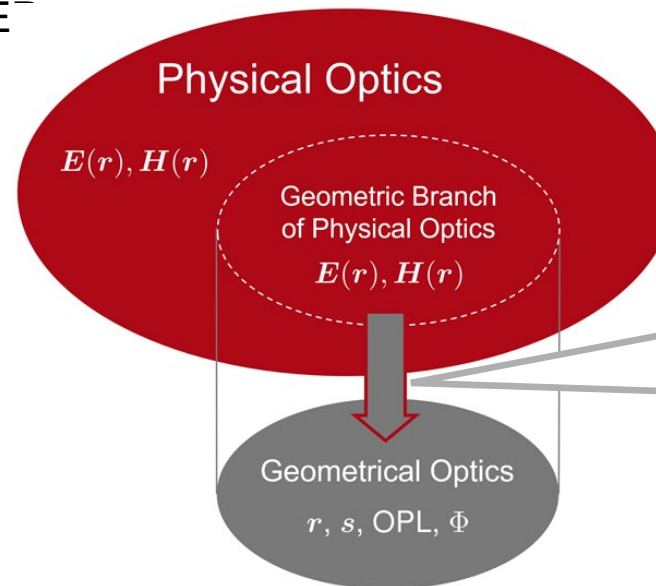
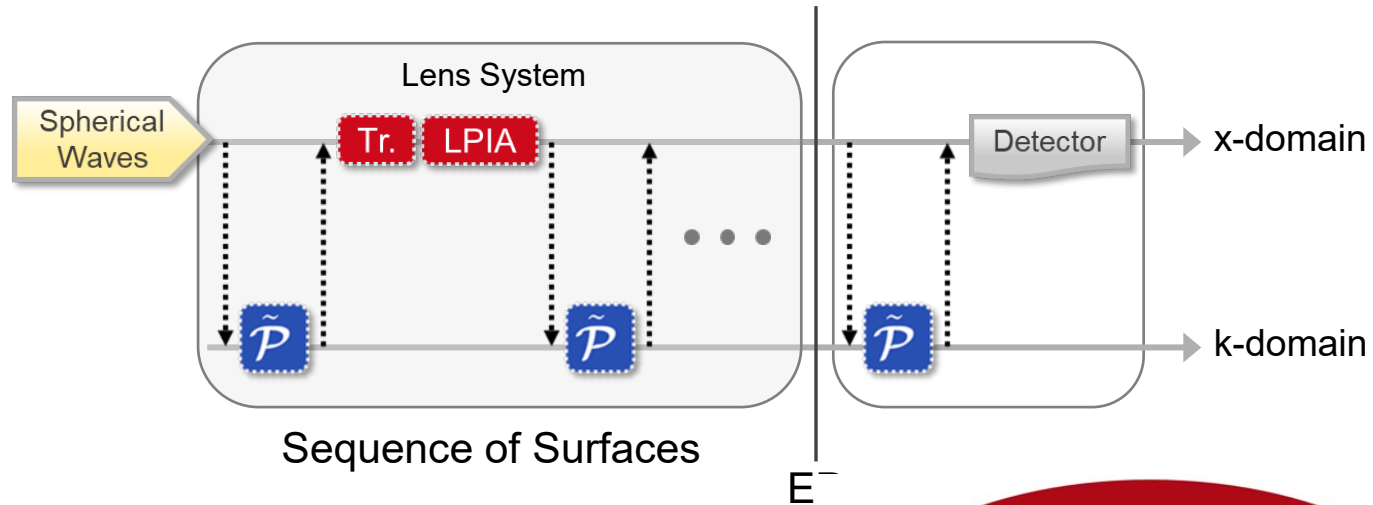
Physical-Optics Lens System Modeling: General



Detector evaluates field on parallel or tilted plane.

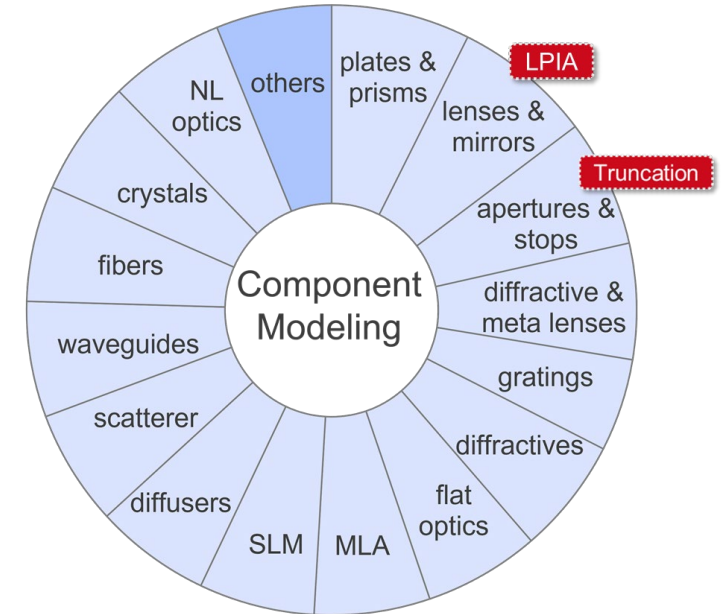
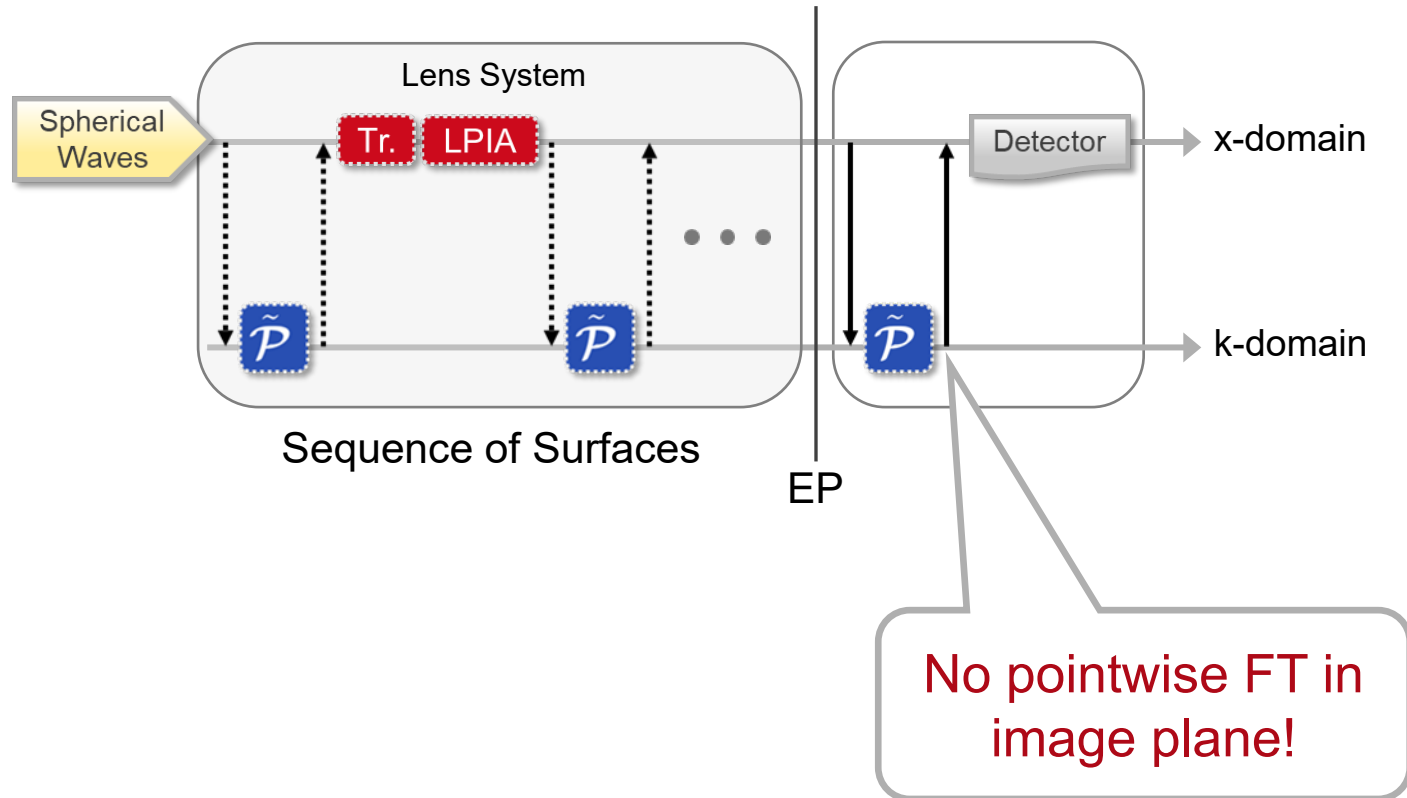


Lens System Modeling: Pointwise

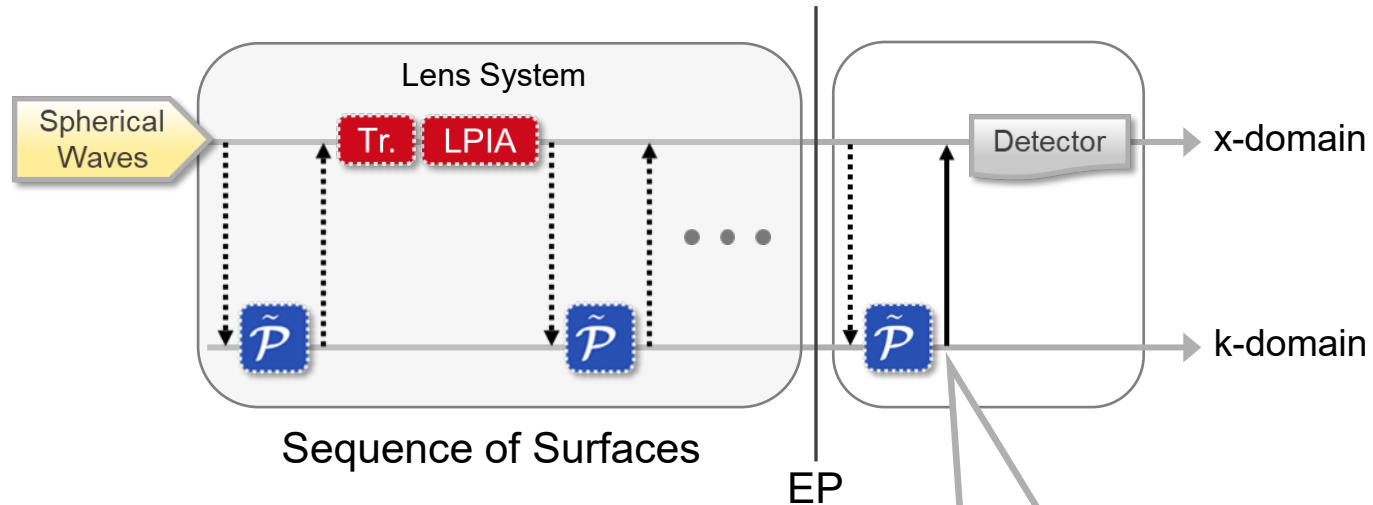


Pointwise physical-optics modeling provides results known from ray tracing with identical numerical complexity!

Lens System Modeling: PSF Calculation

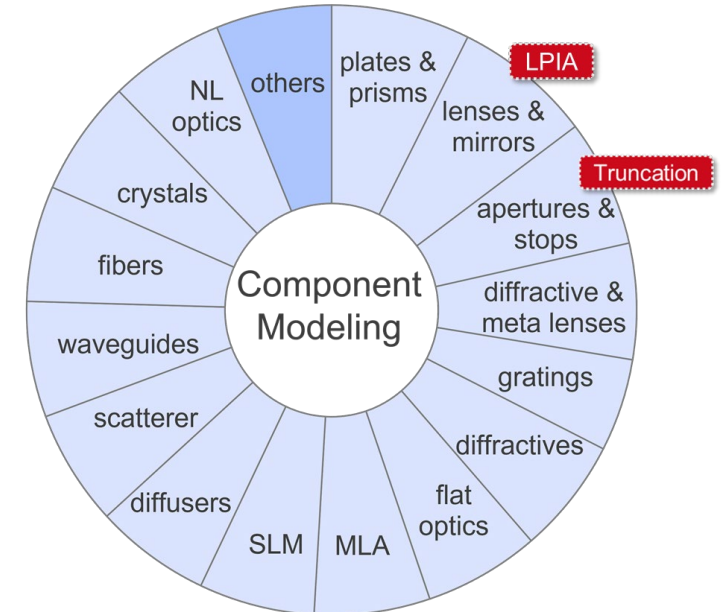


Lens System Modeling: PSF Calculation (Debye Integral)

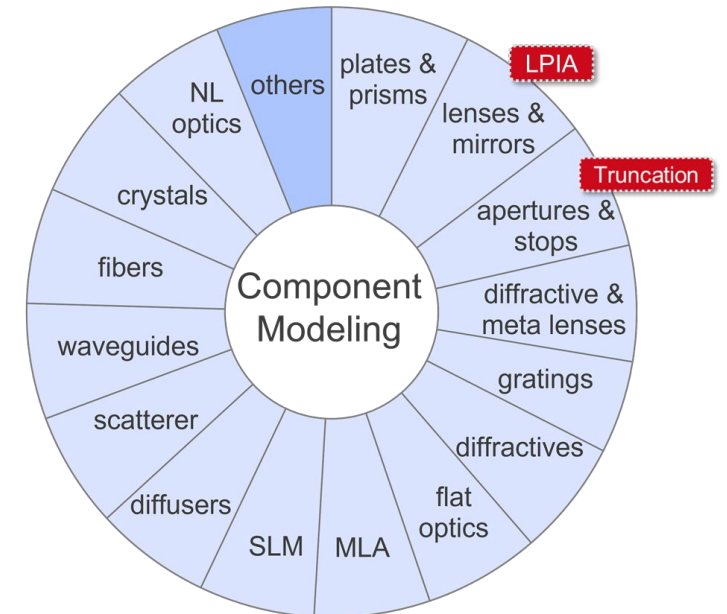
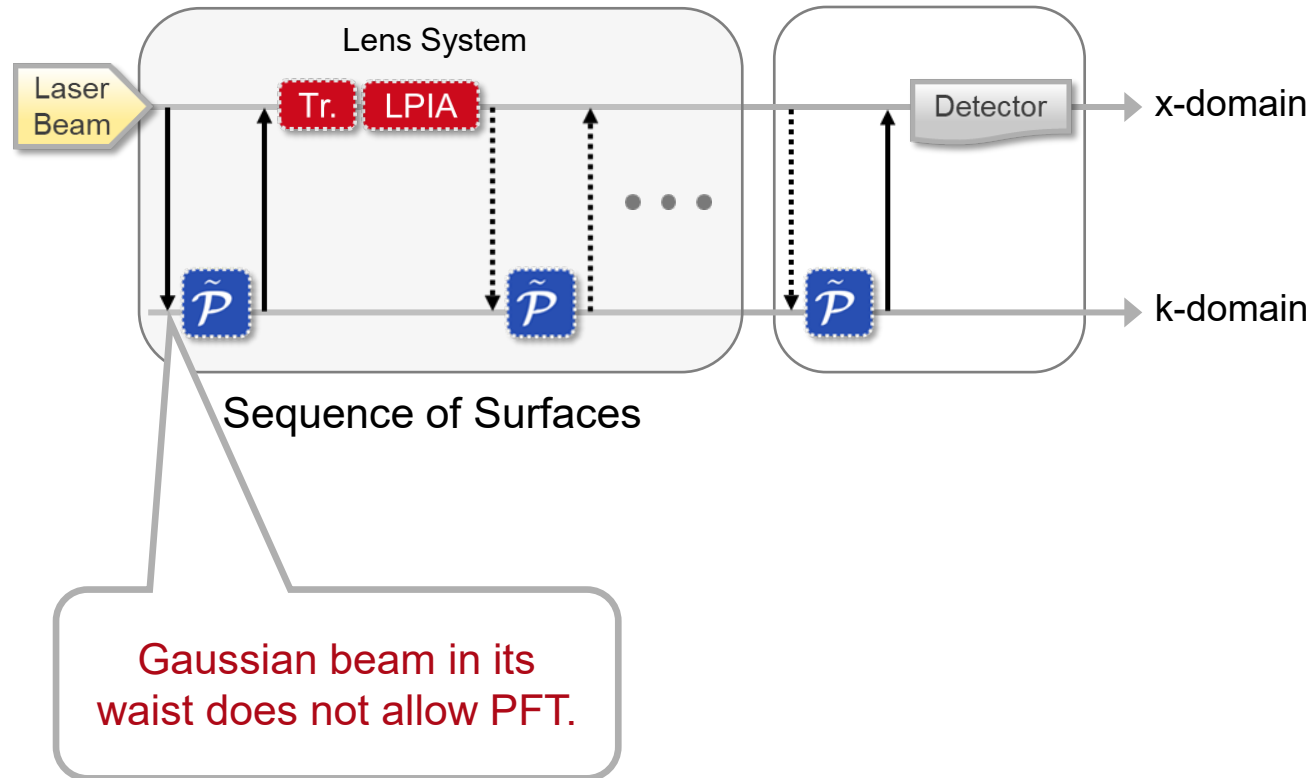


No pointwise FT in
image plane!

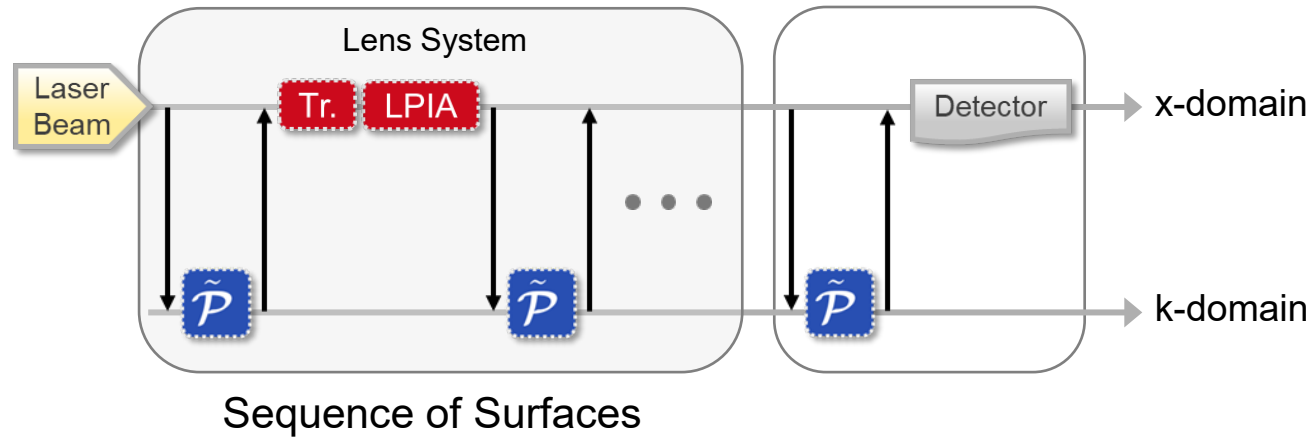
This modeling configuration is
typically assumed in ray tracing
software for PSF calculation.



Lens System Modeling: Laser Beam

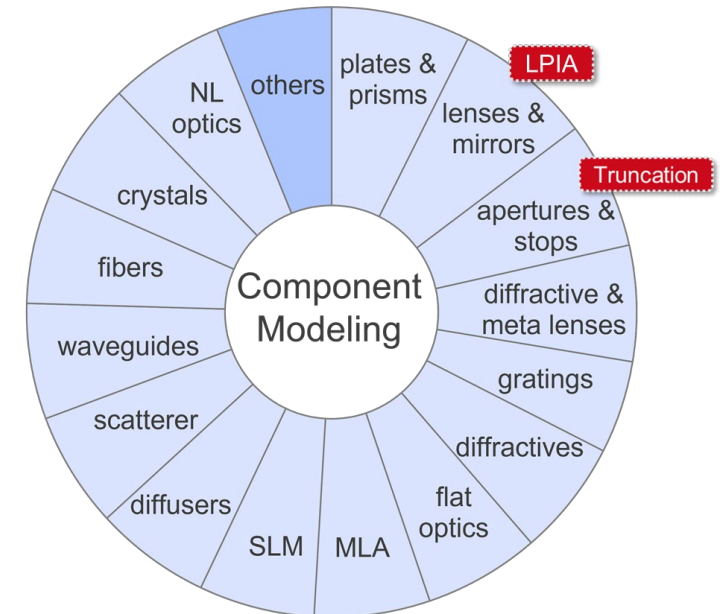


Lens System Modeling: Laser Beam

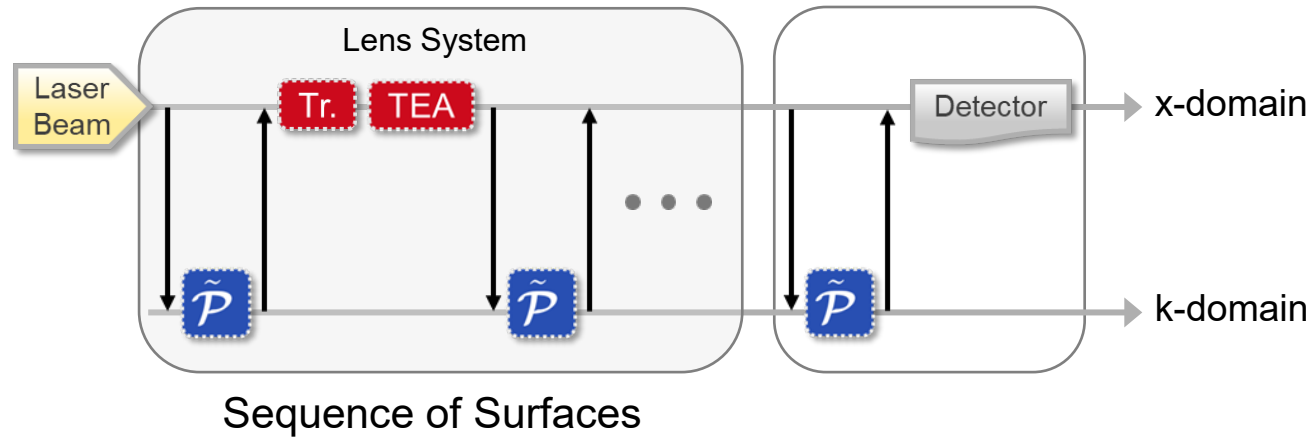


Paraxial fields typically
require integral FT.

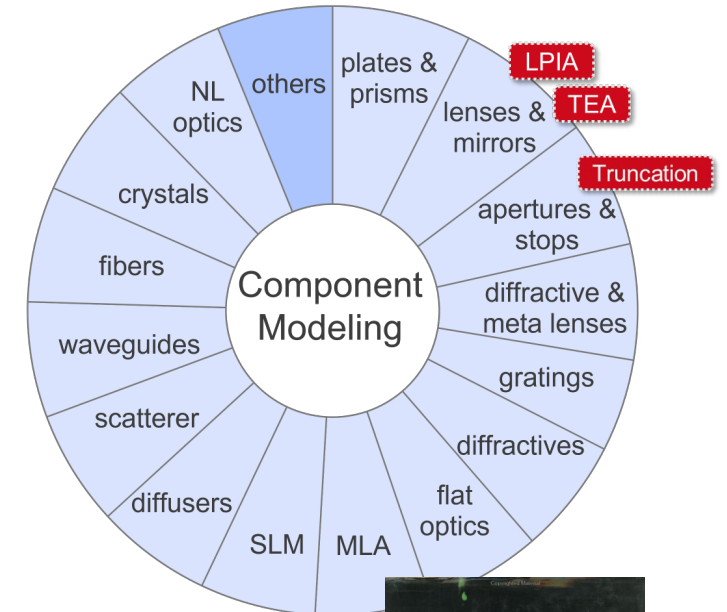
By switching the type of Fourier
transforms any kind of lens modeling
is enabled, including lens system
modeling for paraxial light.



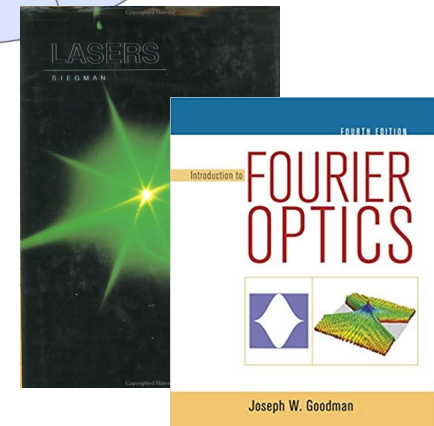
Paraxial Lens System Modeling



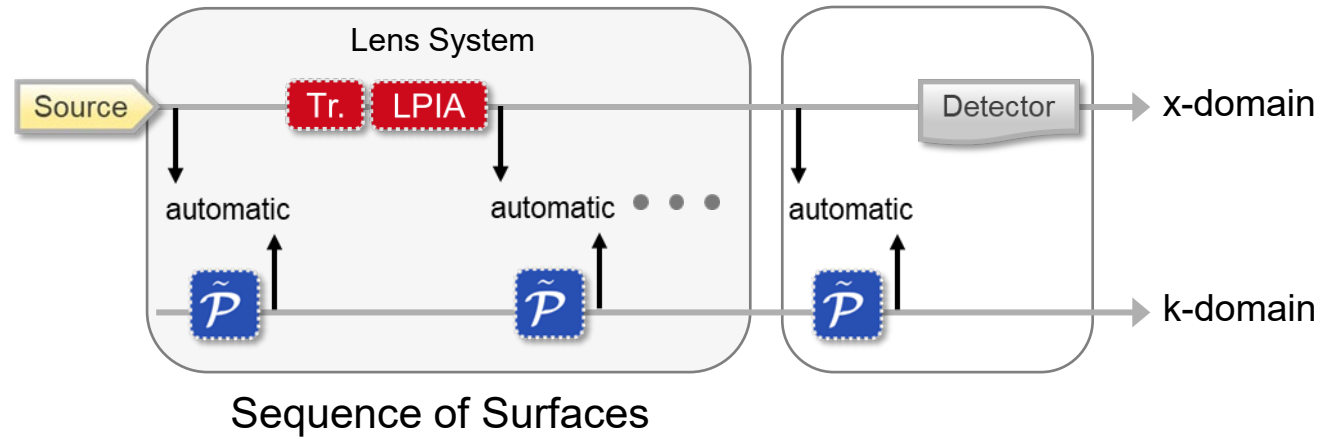
Paraxial lens modeling
allows use of TEA.



This modeling configuration is
typically used in Fourier optics and
laser optics books.

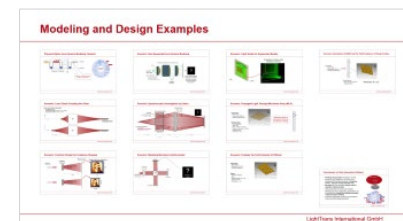
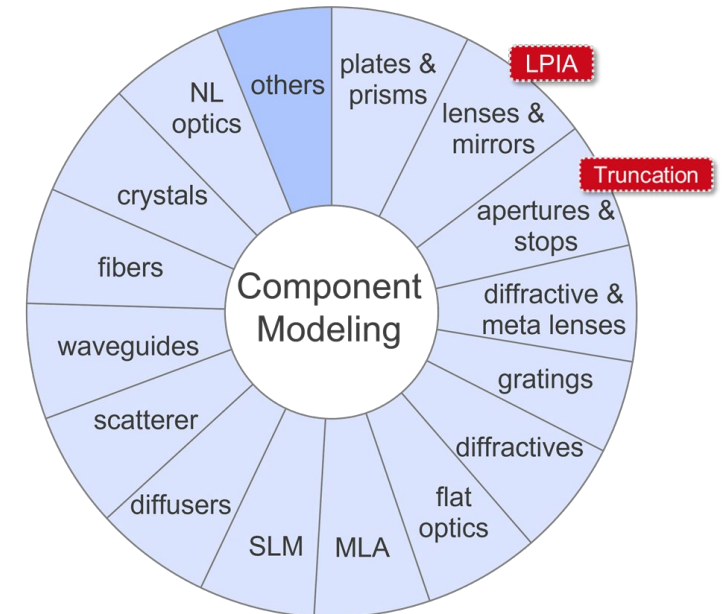


Lens System Modeling: General



Software algorithms decide about FT selection according to accuracy criterion.

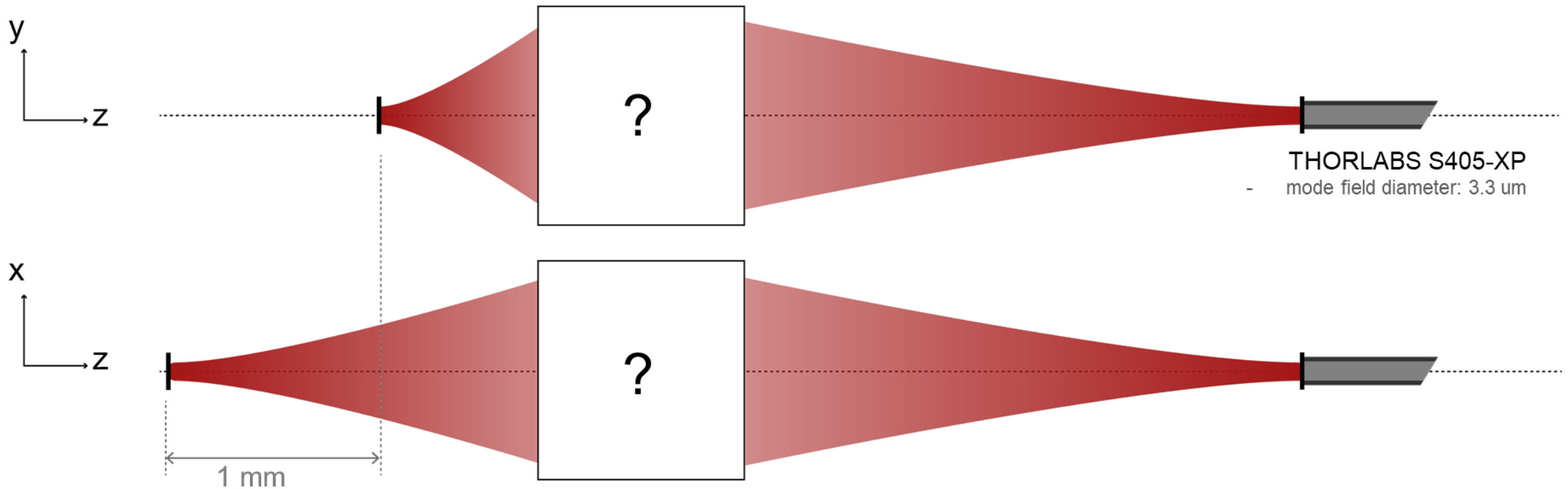
All lens modeling situations are included in a seamless modeling approach!



Scenario: Laser Diode Coupling Into Fiber

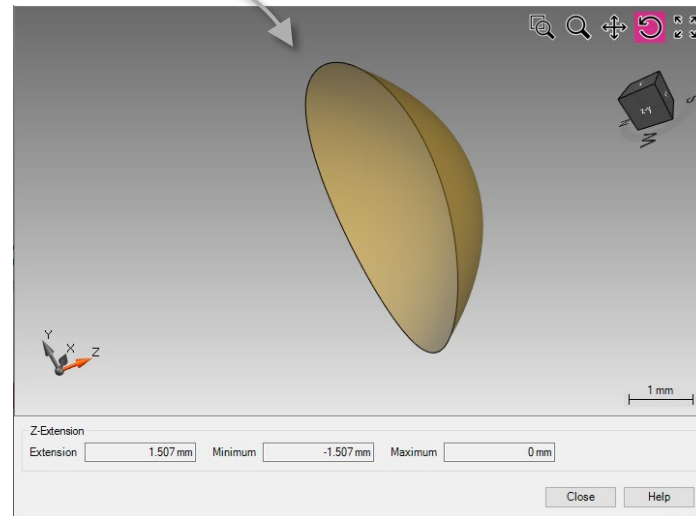
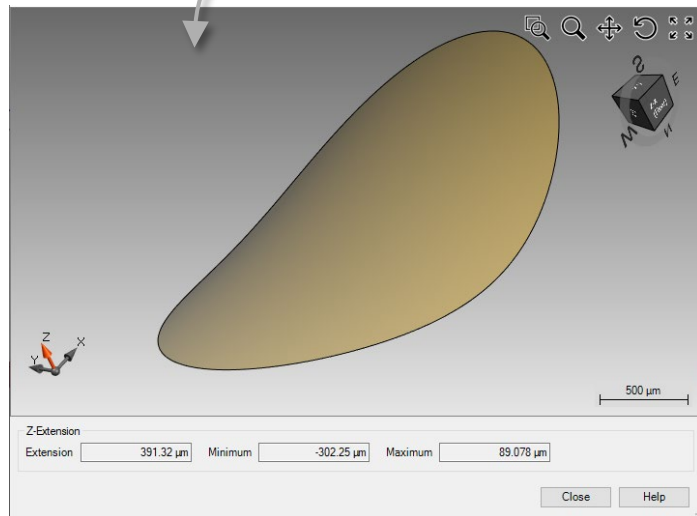
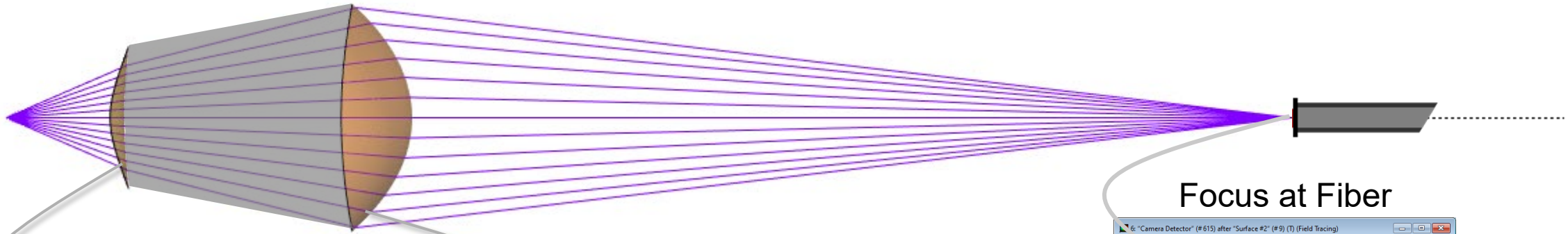
laser diode with astigmatism

- wavelength 405nm
- half divergent angle ($1/e^2$): $8.74^\circ \times 15.63^\circ$
- astigmatism between y and x: -1 mm

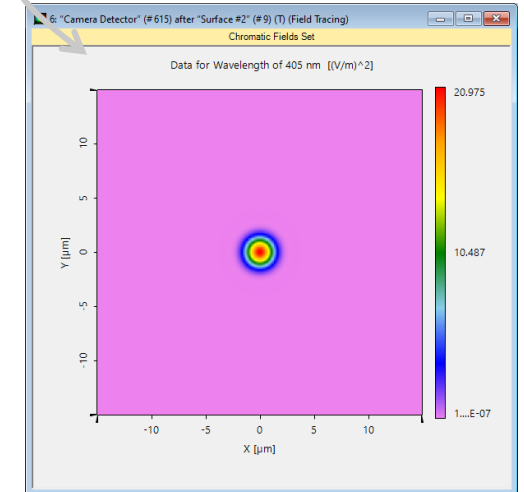


Laser Diode Coupling Into Fiber: Freeform Design

By Inverse Design

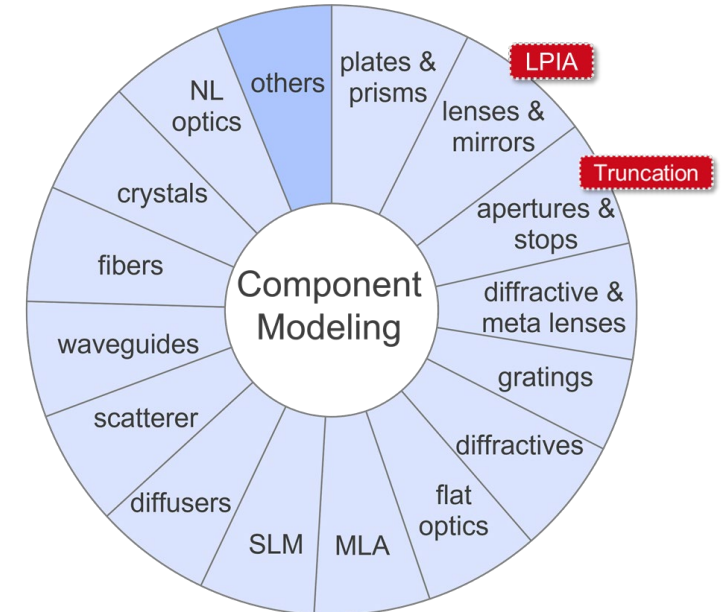
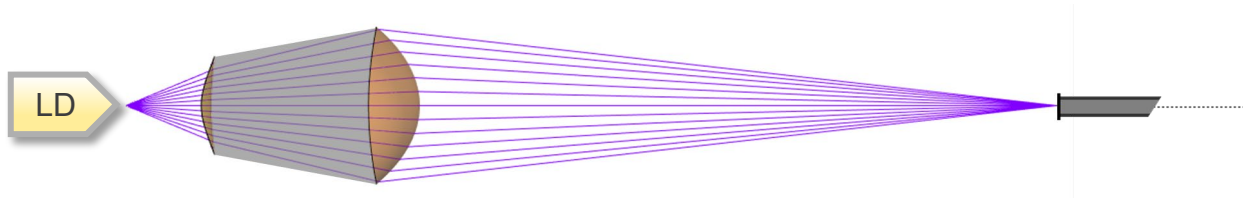
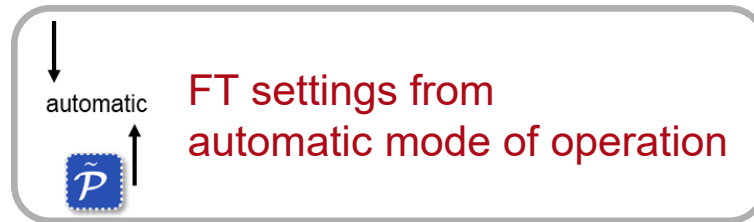
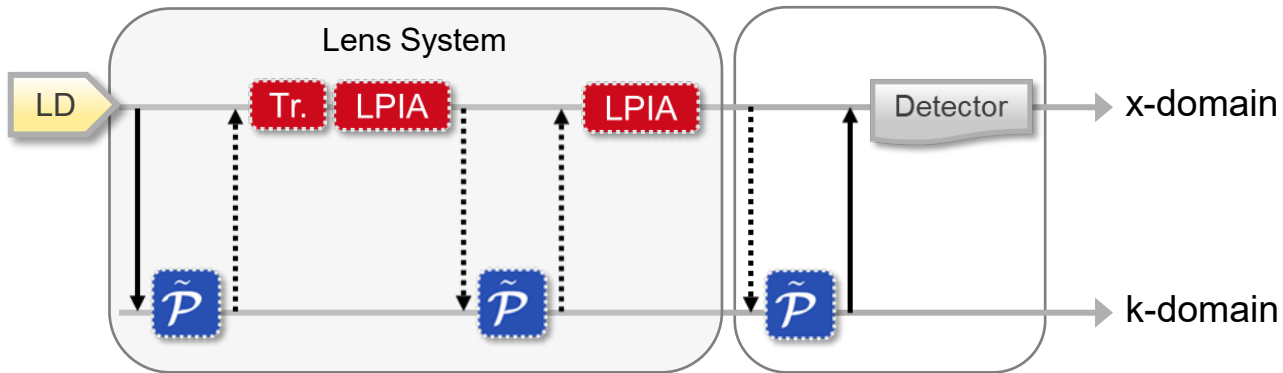


Focus at Fiber

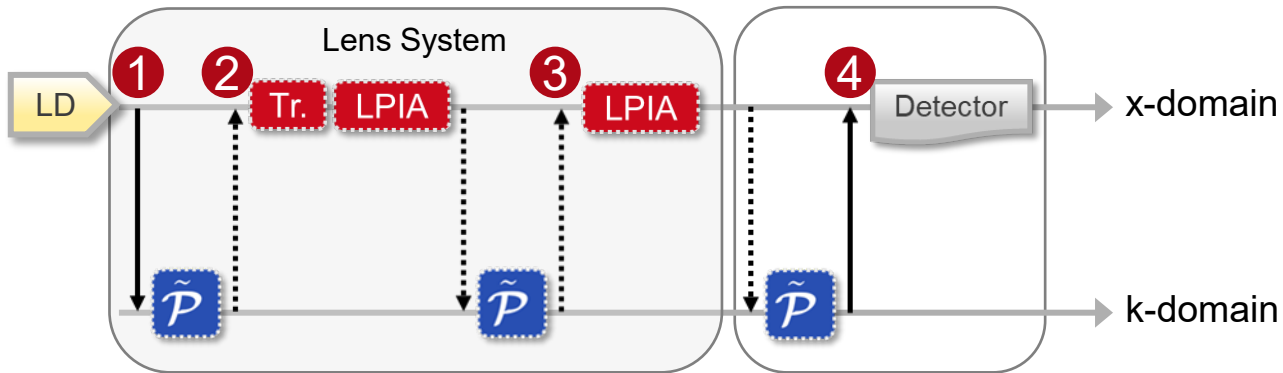


Incoupling Efficiency: 98%

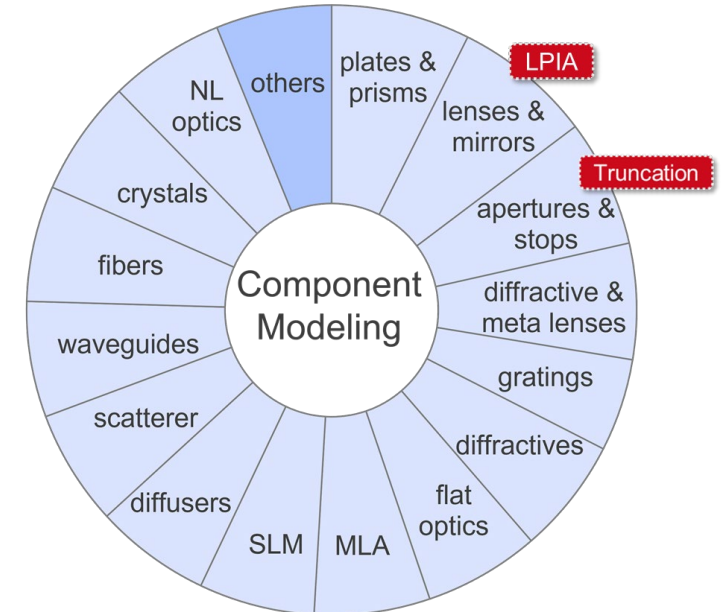
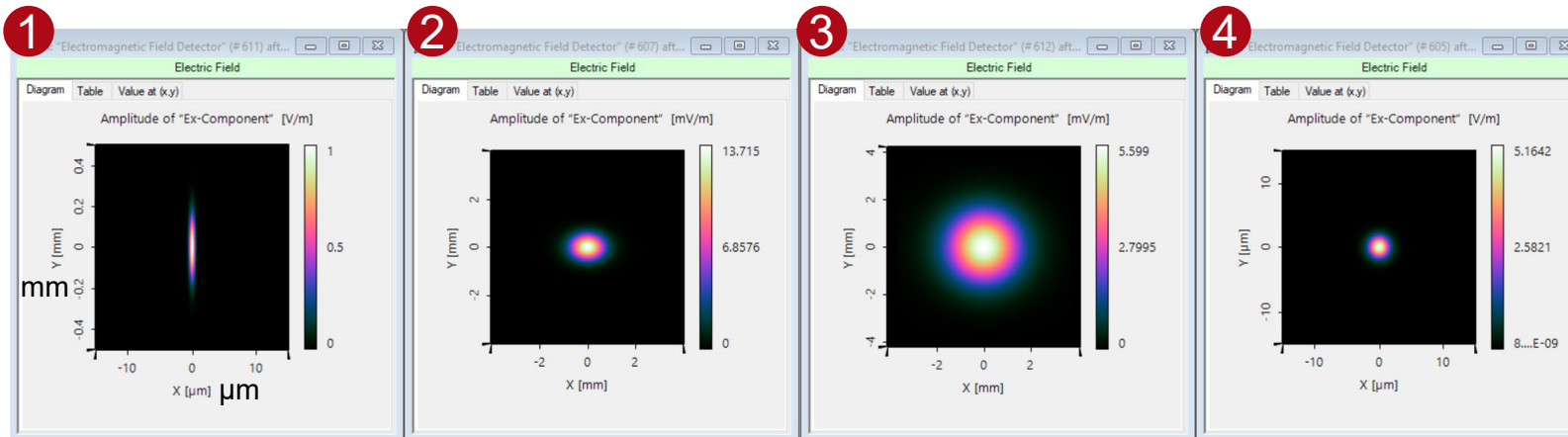
Lens System Modeling: Laser Diode Fiber Coupling



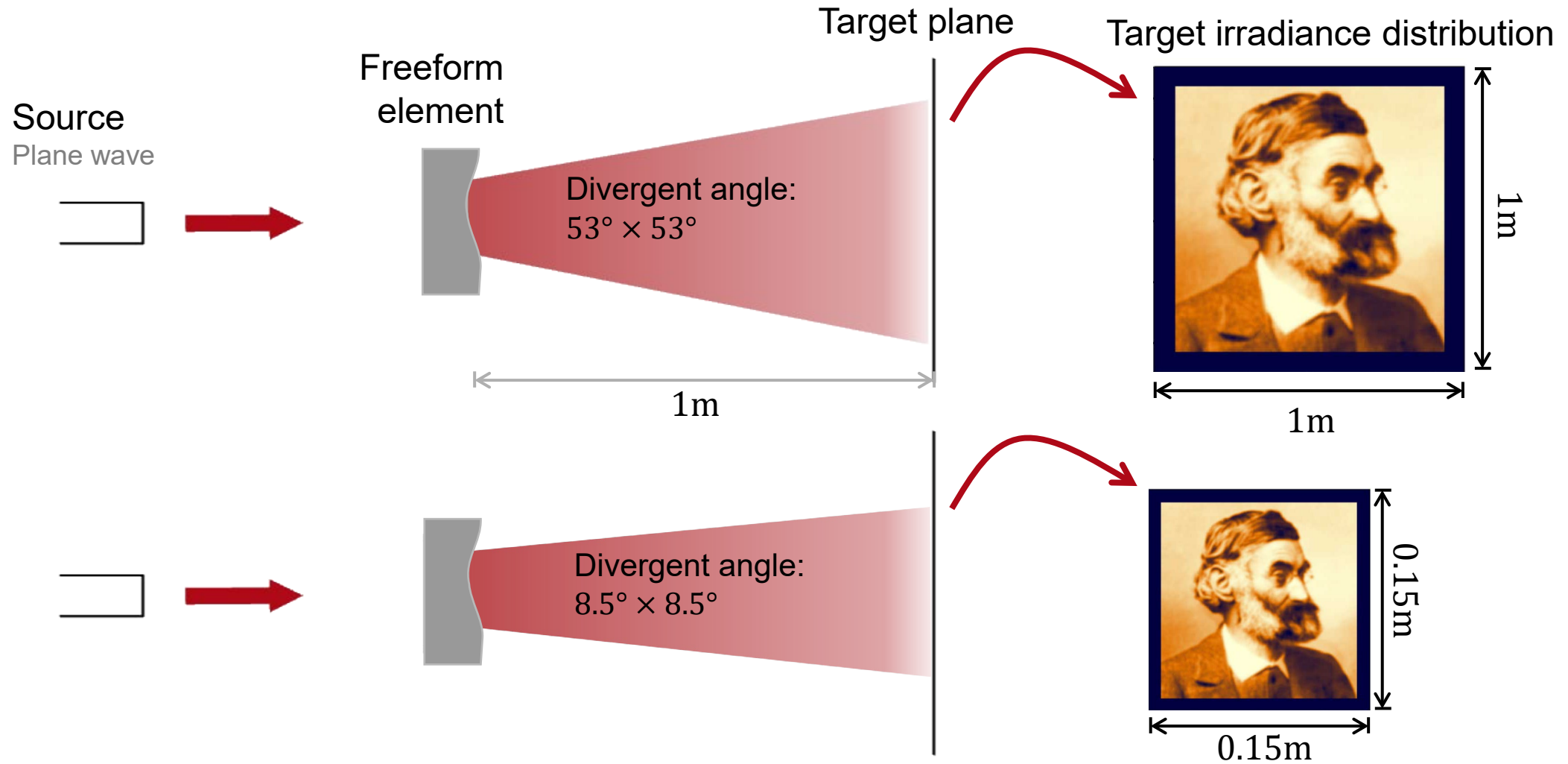
Lens System Modeling: Laser Diode Fiber Coupling



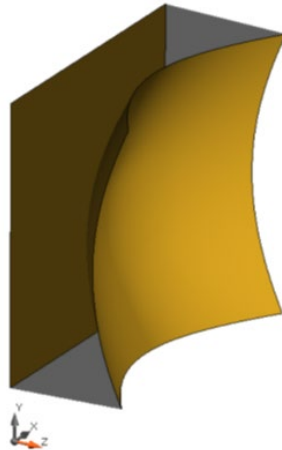
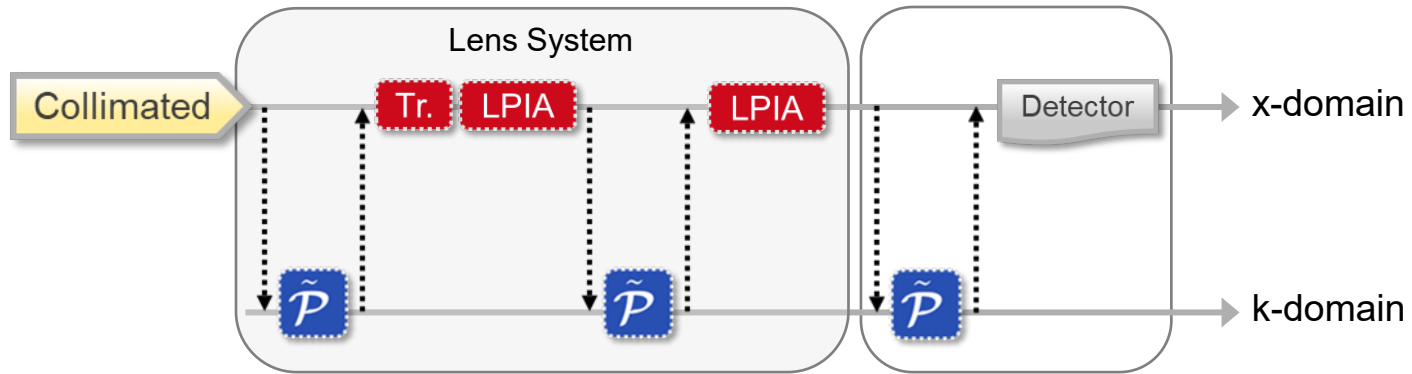
Field Amplitudes



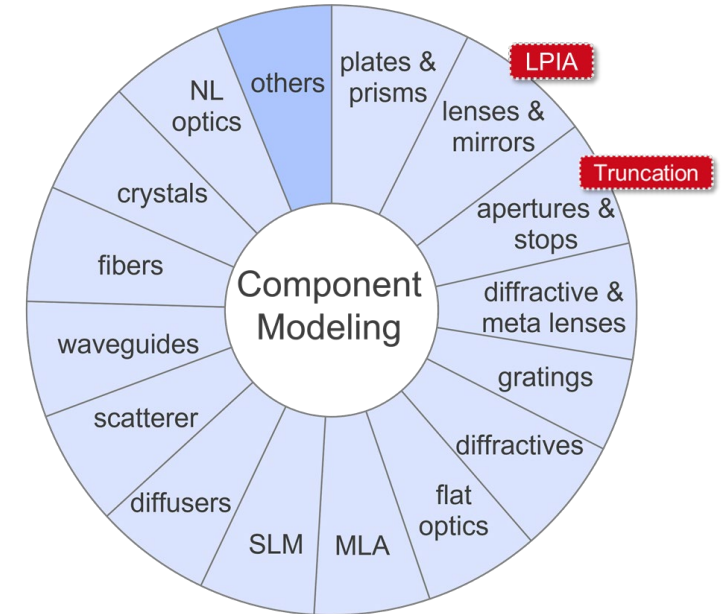
Scenario: Freeform Design for Irradiance Shaping



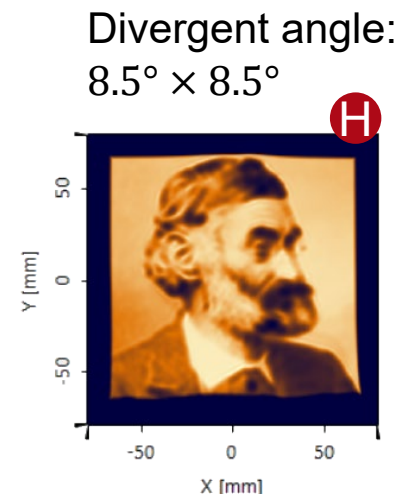
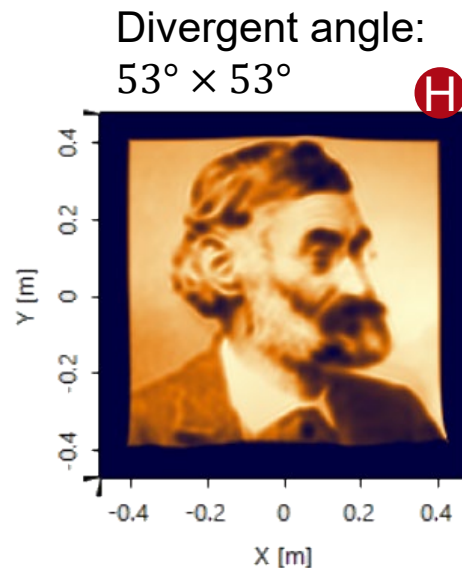
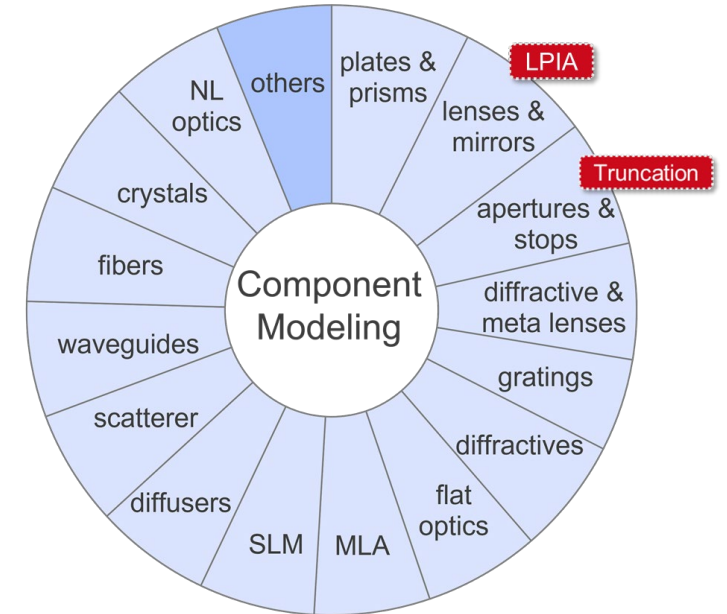
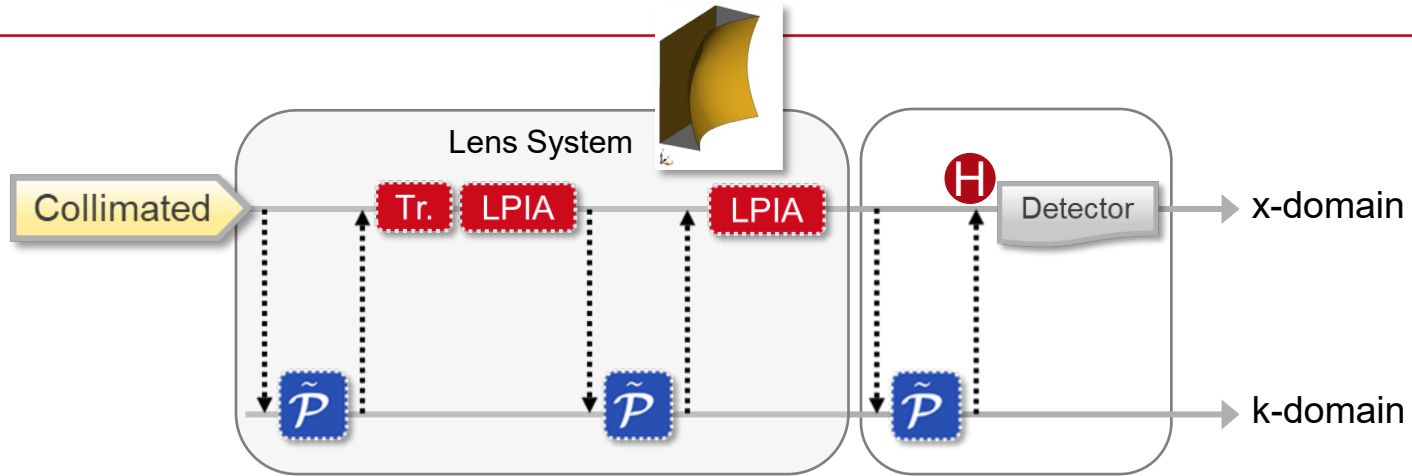
Freeform Design for Irradiance Shaping: Pointwise Design



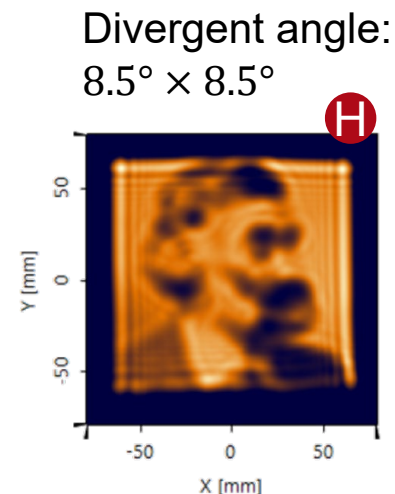
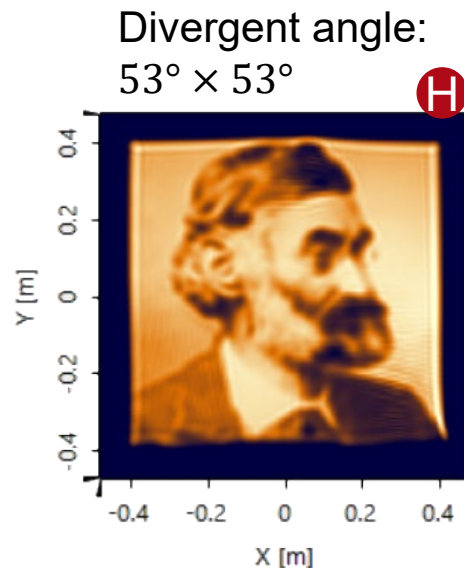
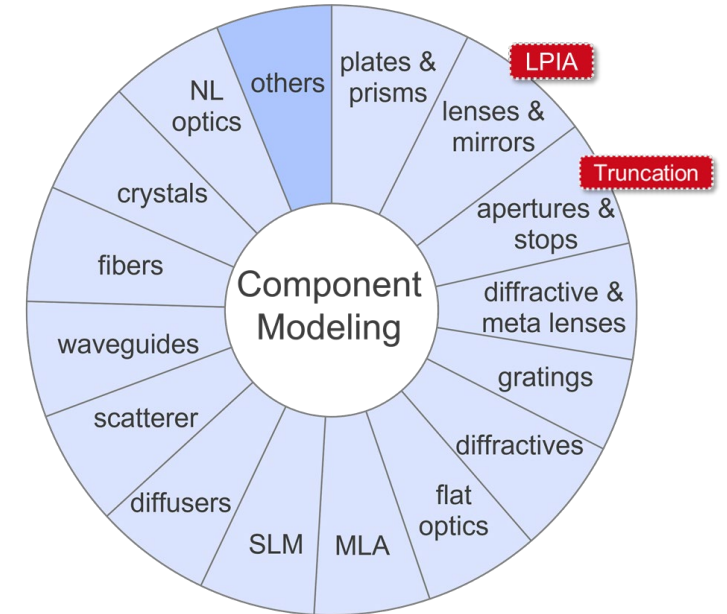
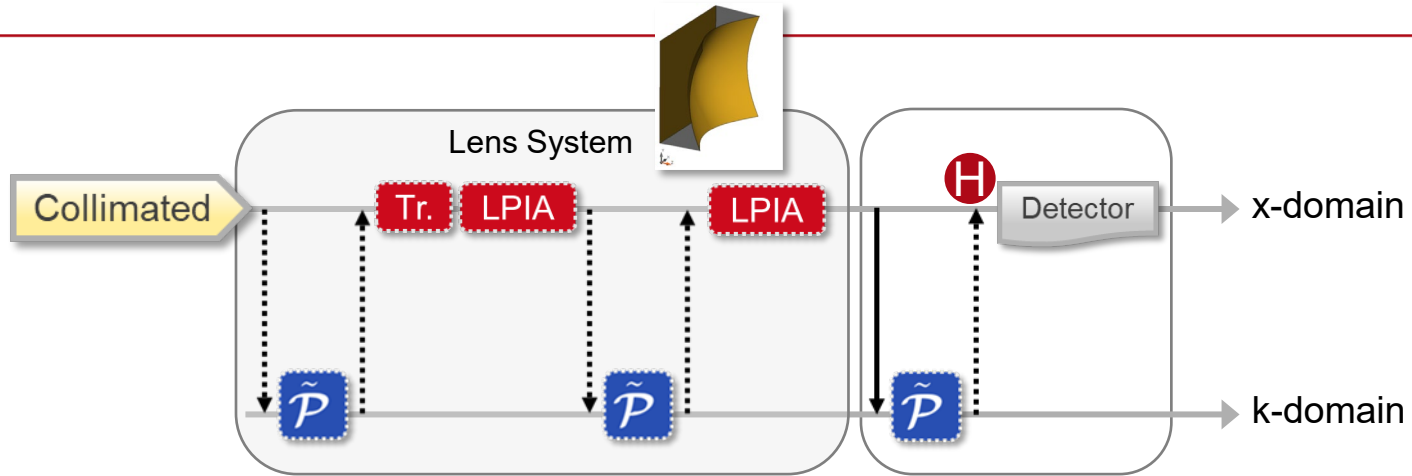
Design method is based on pointwise Fourier transform.



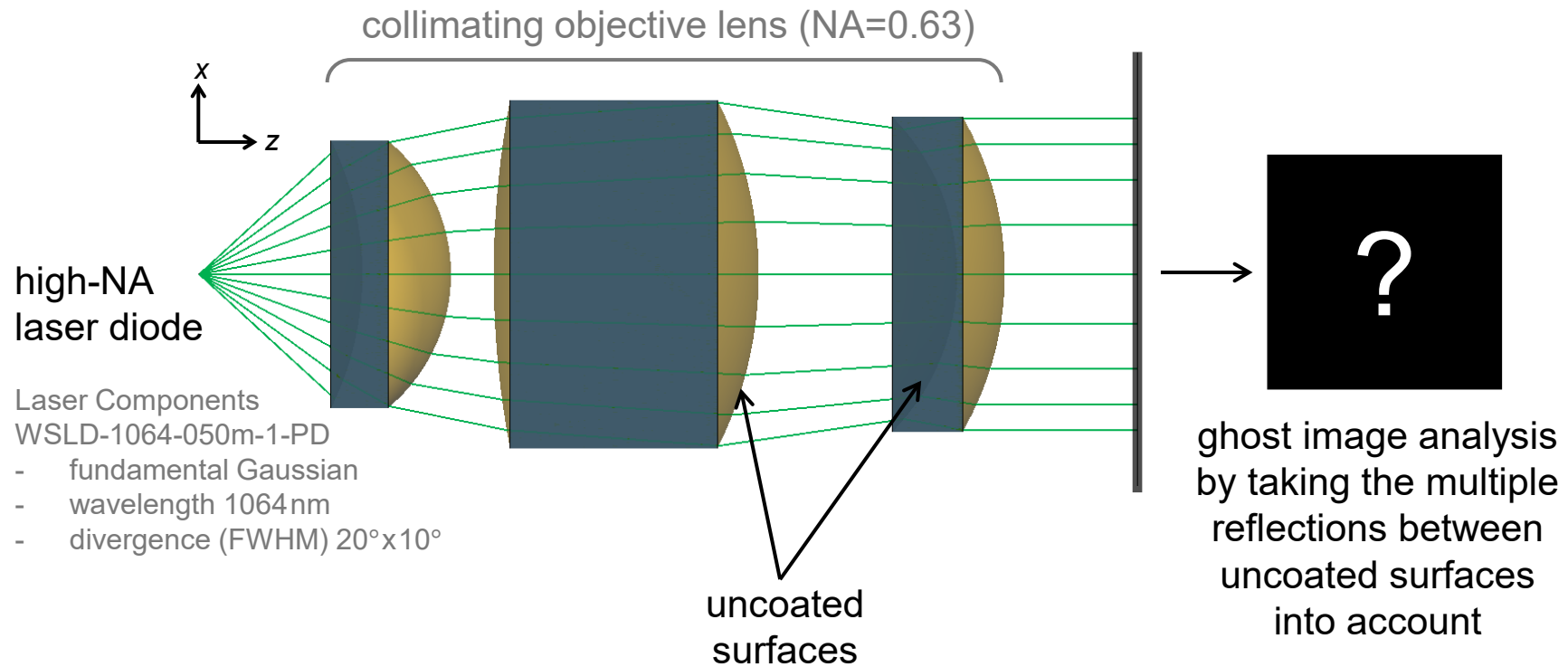
Freeform Design for Irradiance Shaping: Pointwise Modeling



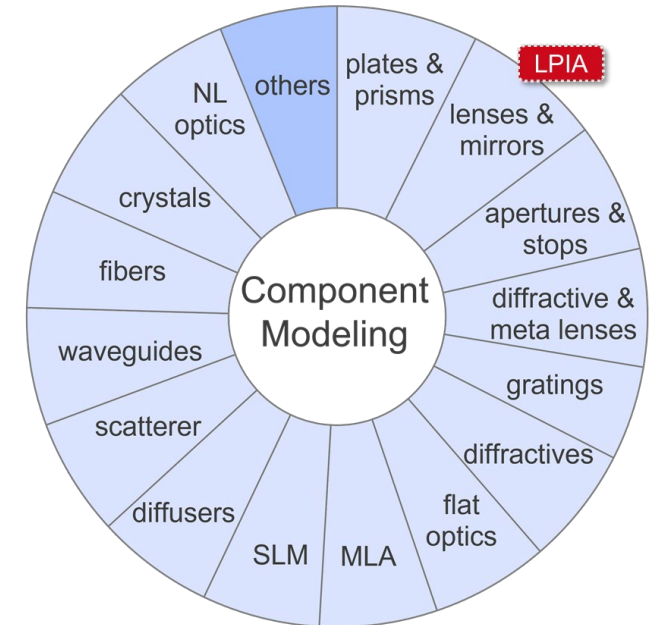
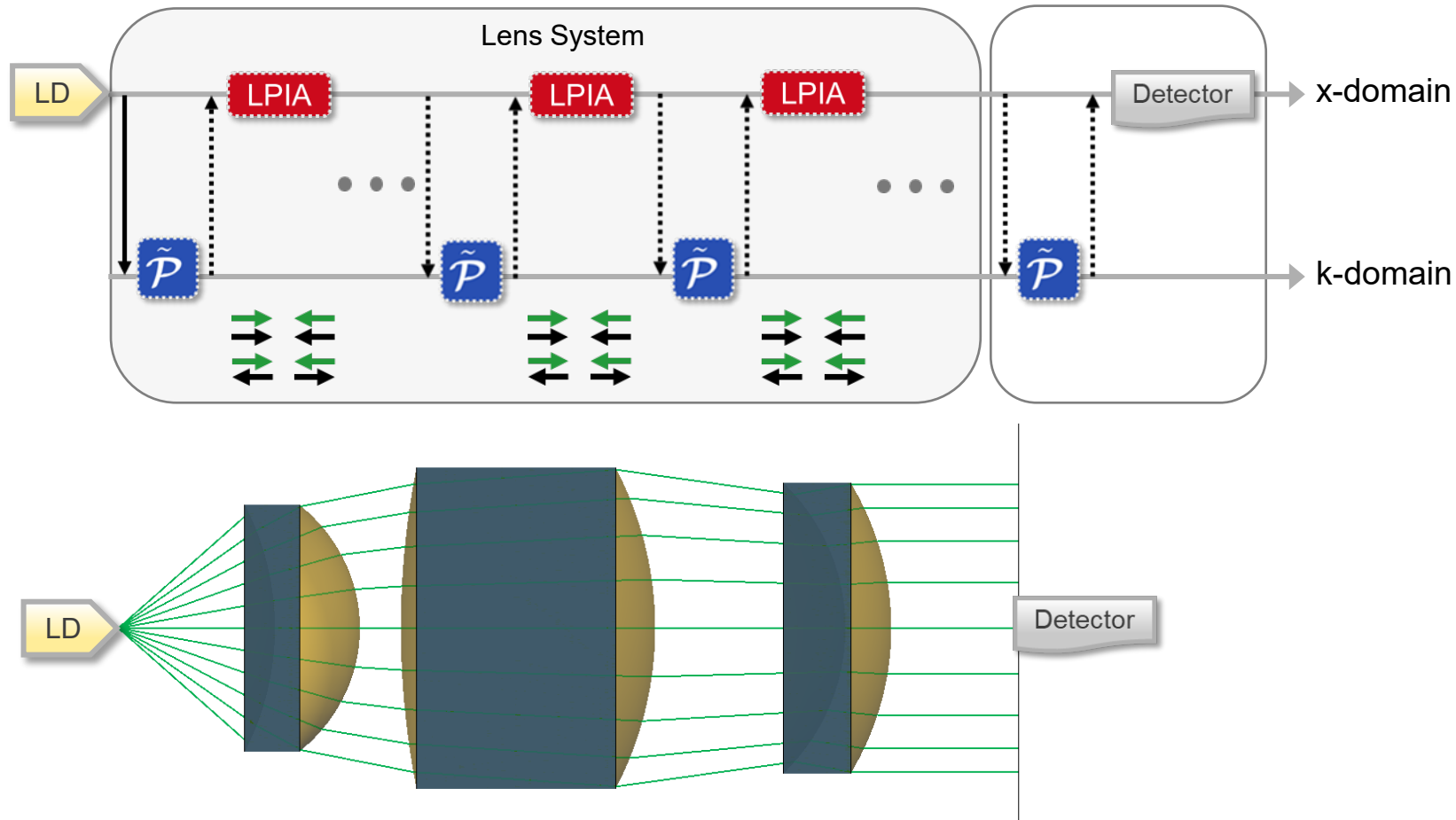
Freeform Design for Irradiance Shaping: Integral Modeling



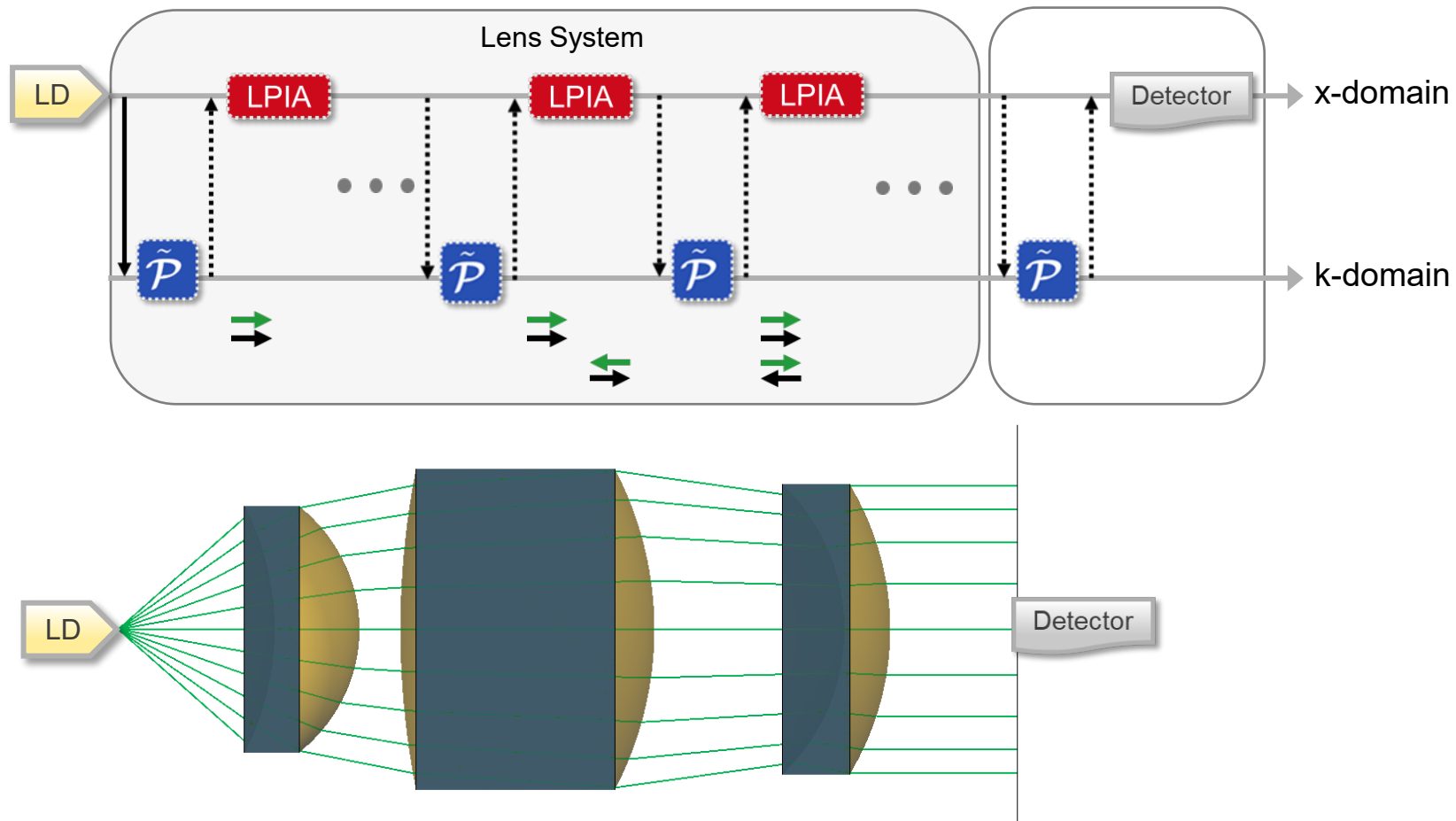
Scenario: Non-Sequential Lens System Modeling



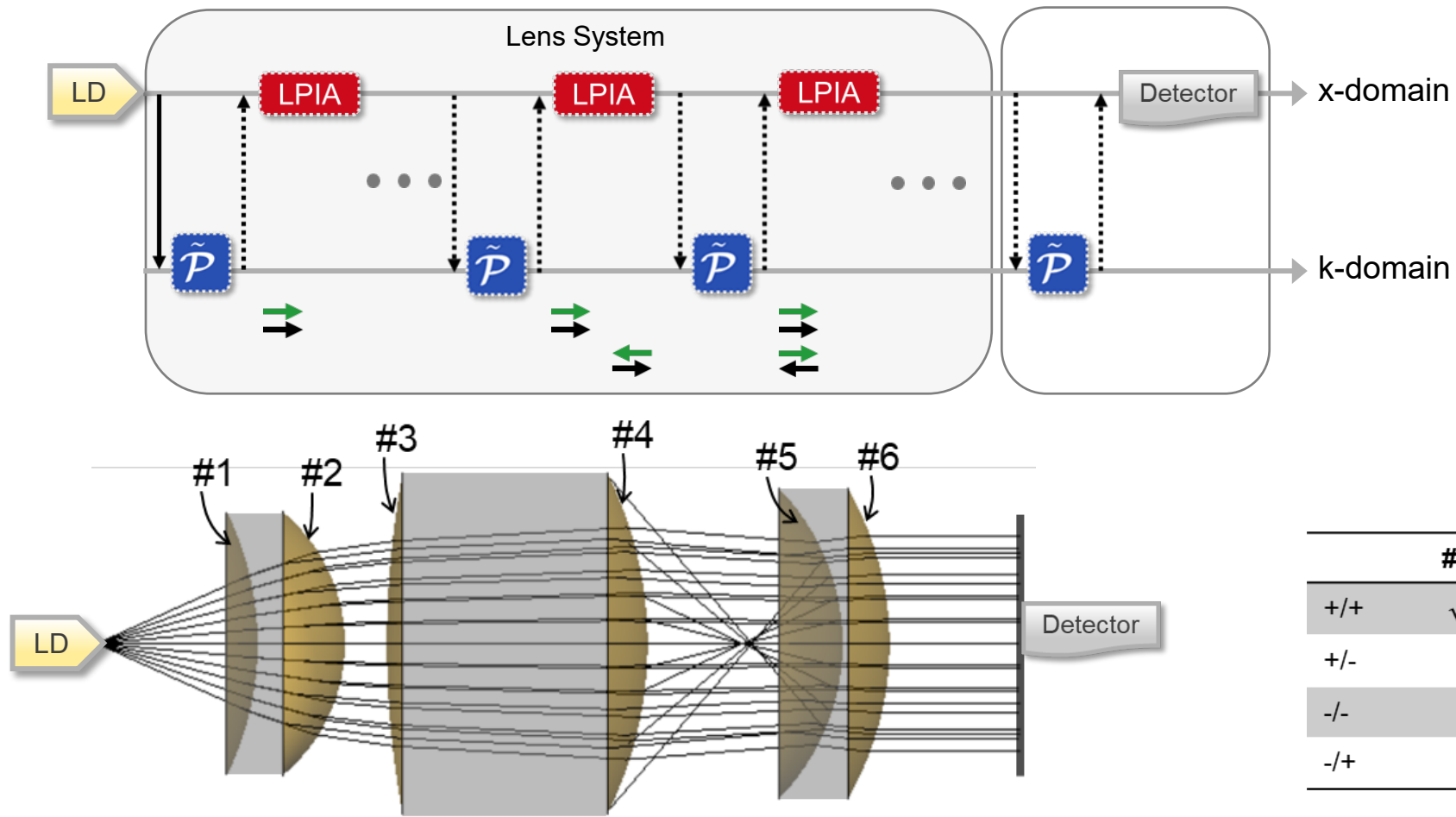
Scenario: Non-Sequential Lens System Modeling



Scenario: Non-Sequential Lens System Modeling

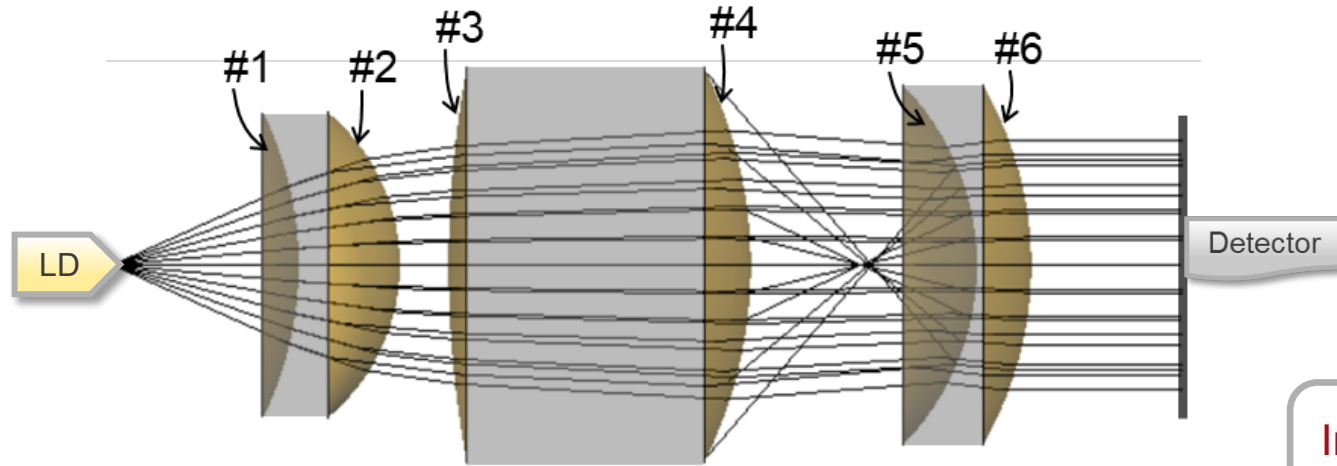
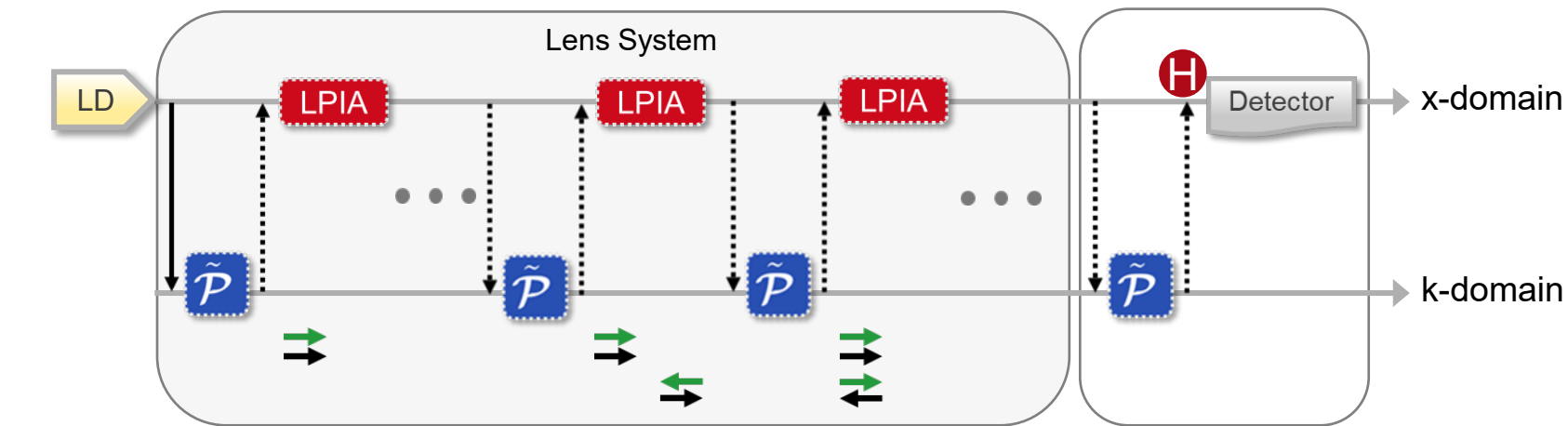


Scenario: Non-Sequential Lens System Modeling

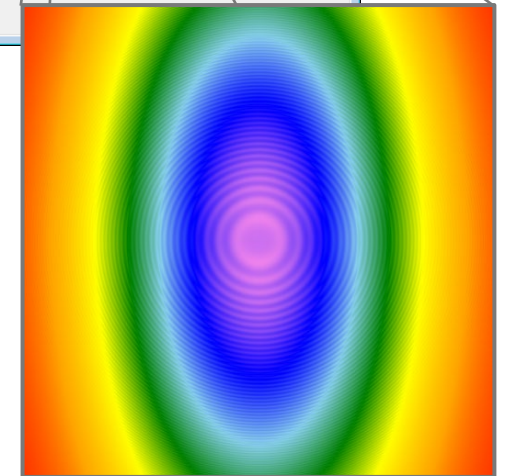
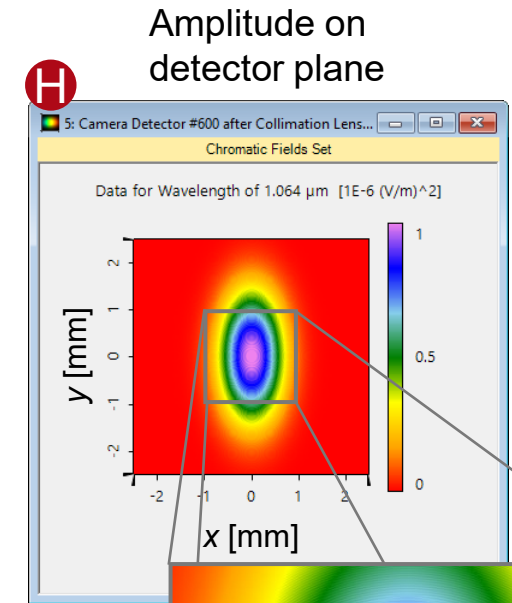


	#1	#2	#3	#4	#5	#6
+/+	√	√	√	√	√	√
+/-					√	
-/-						
-/+				√		

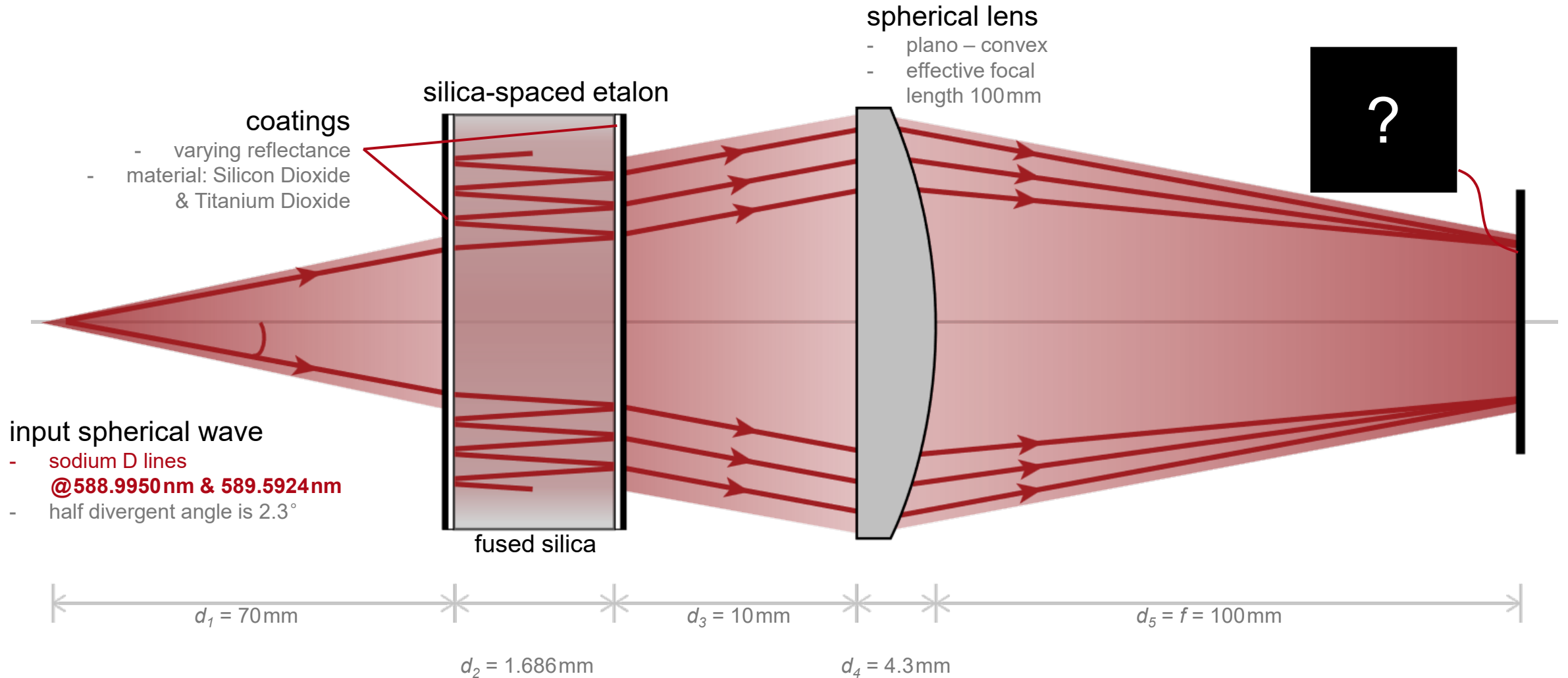
Scenario: Non-Sequential Lens System Modeling



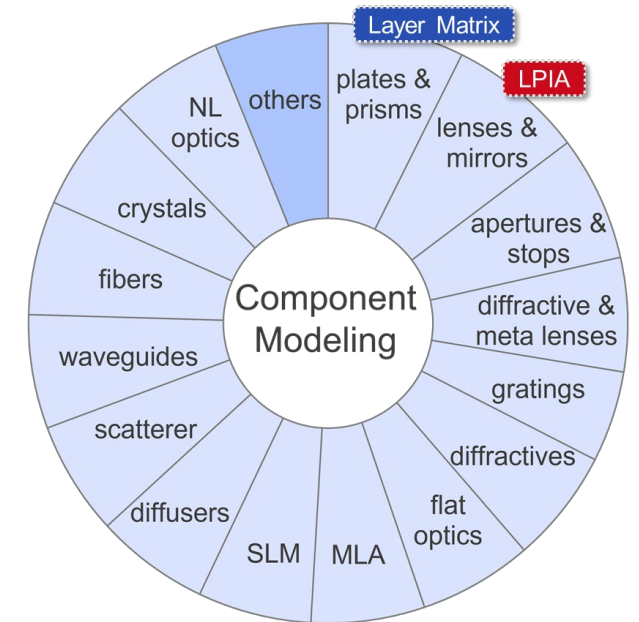
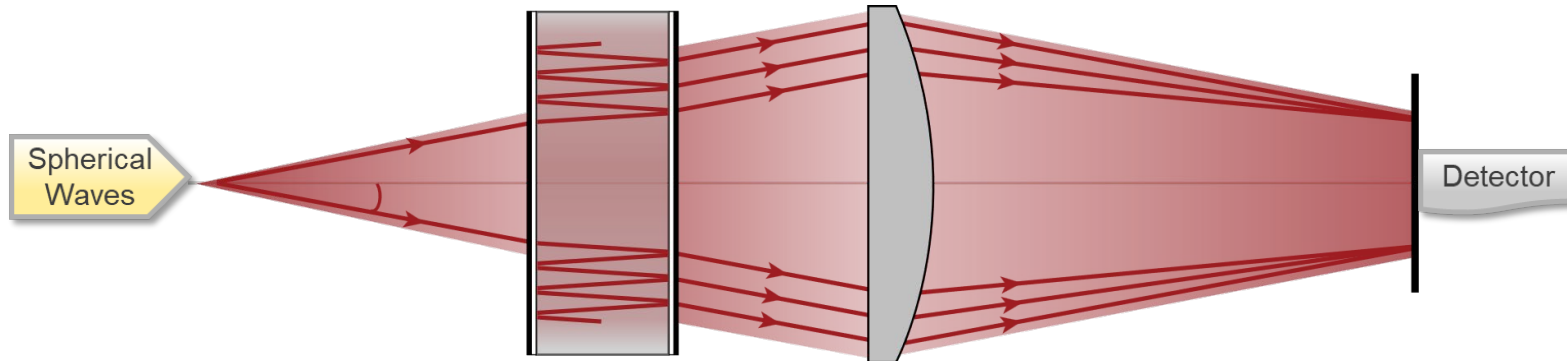
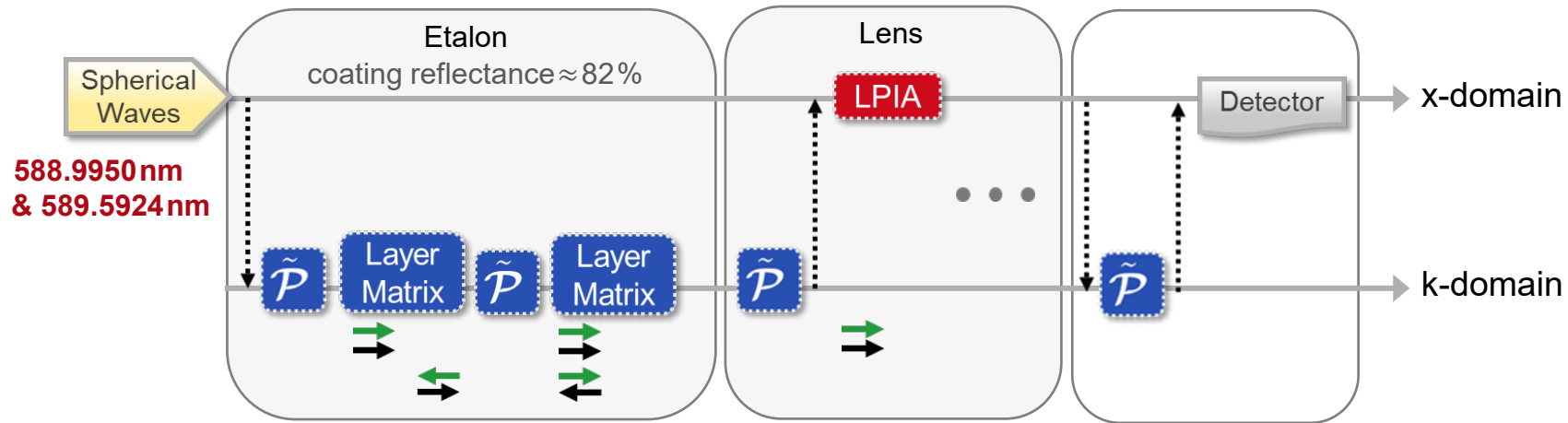
Interference of two modes by internal reflection.



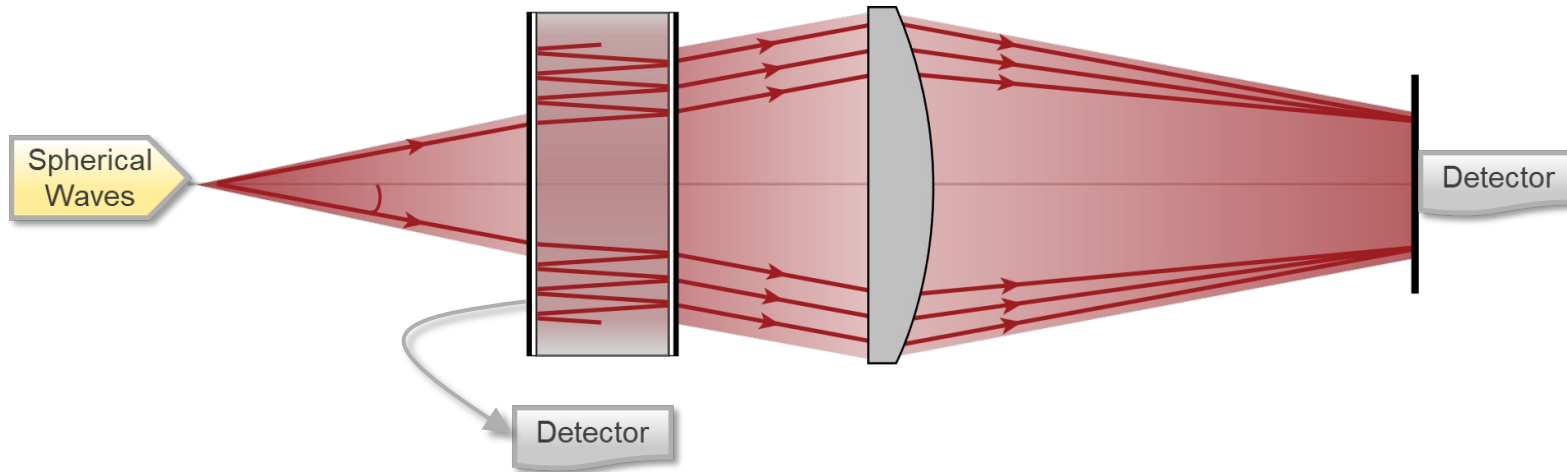
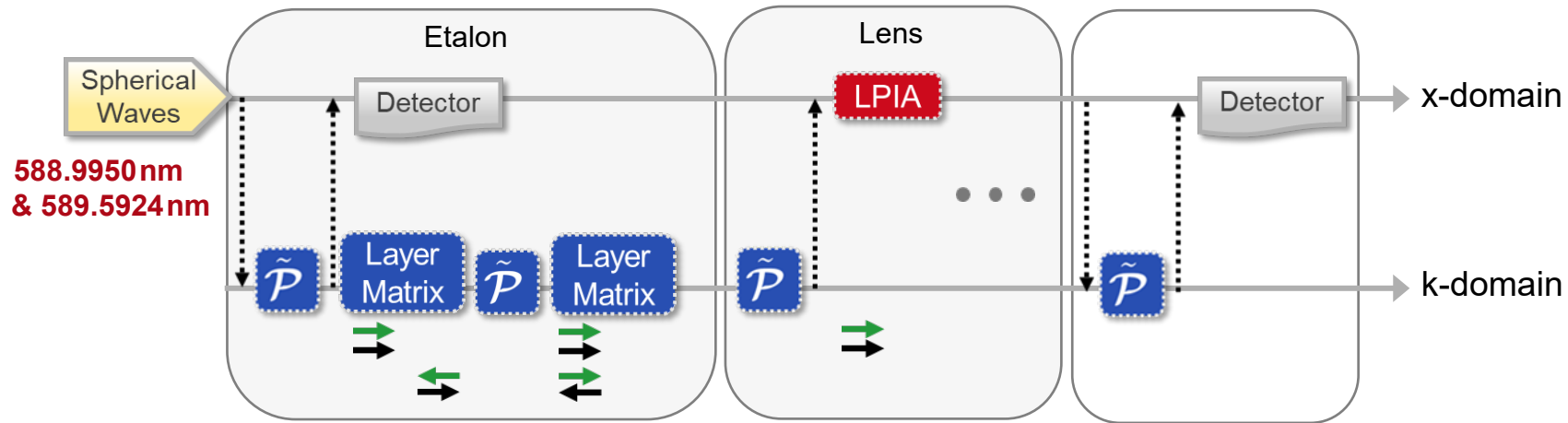
Scenario: Spectroscopic Investigation by Etalon



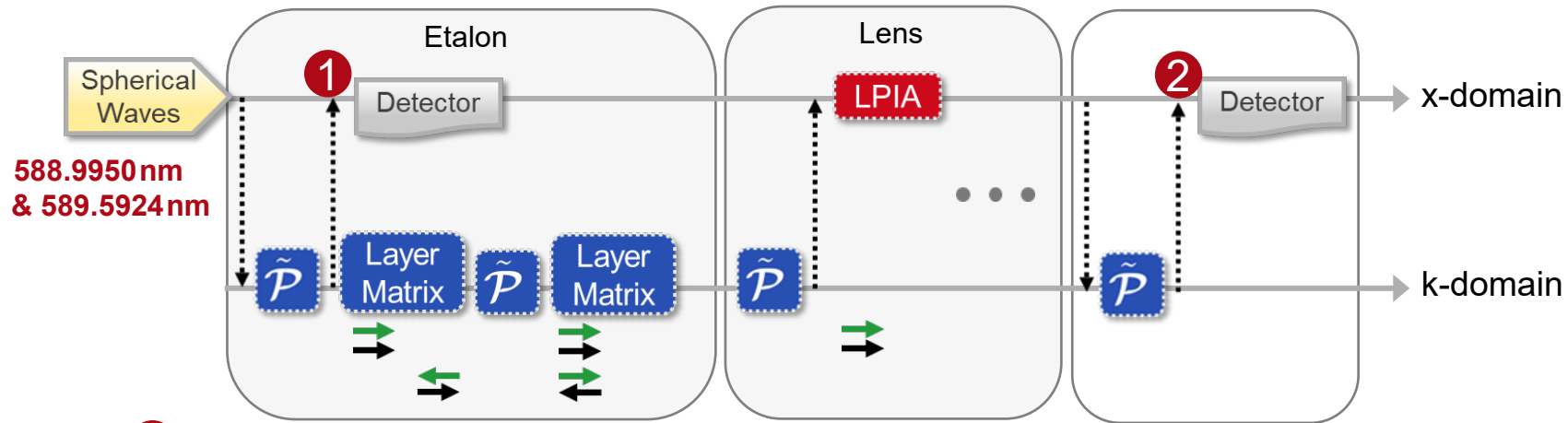
Non-Sequential Pointwise Modeling Etalon + Lens



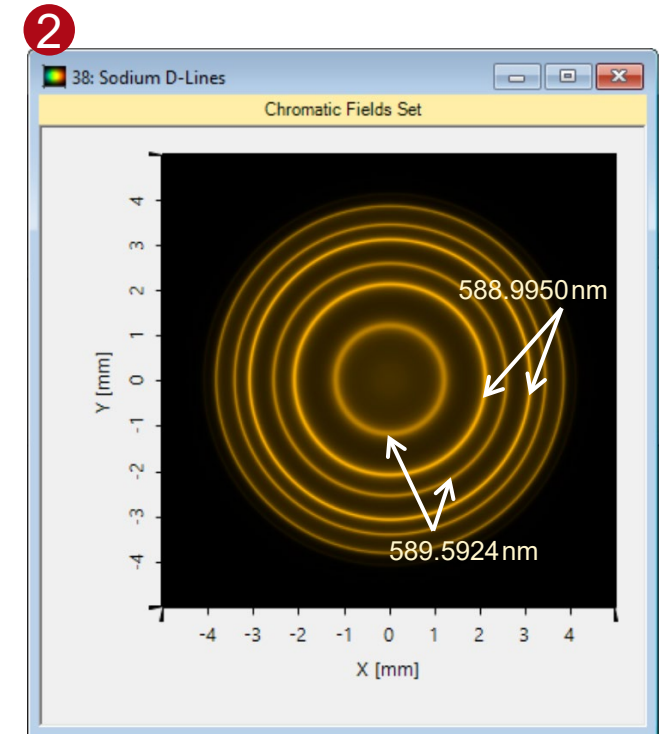
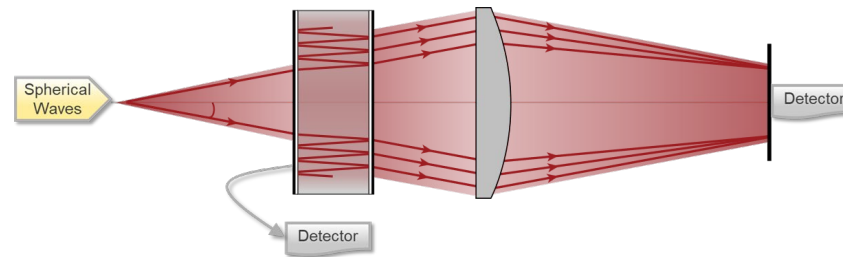
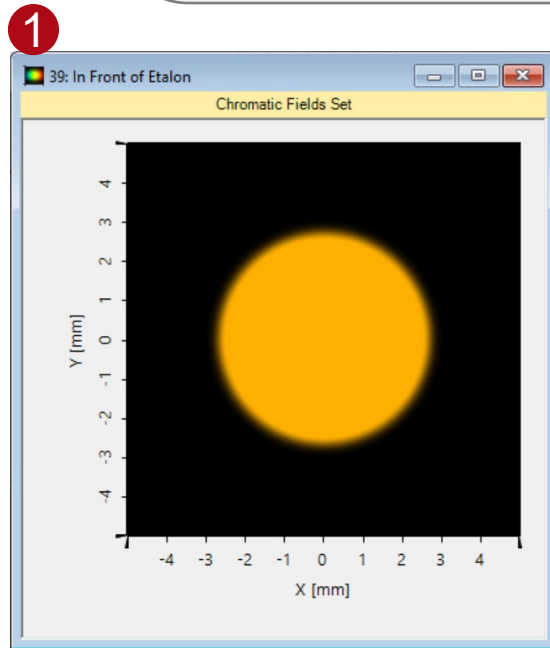
Non-Sequential Pointwise Modeling Etalon + Lens



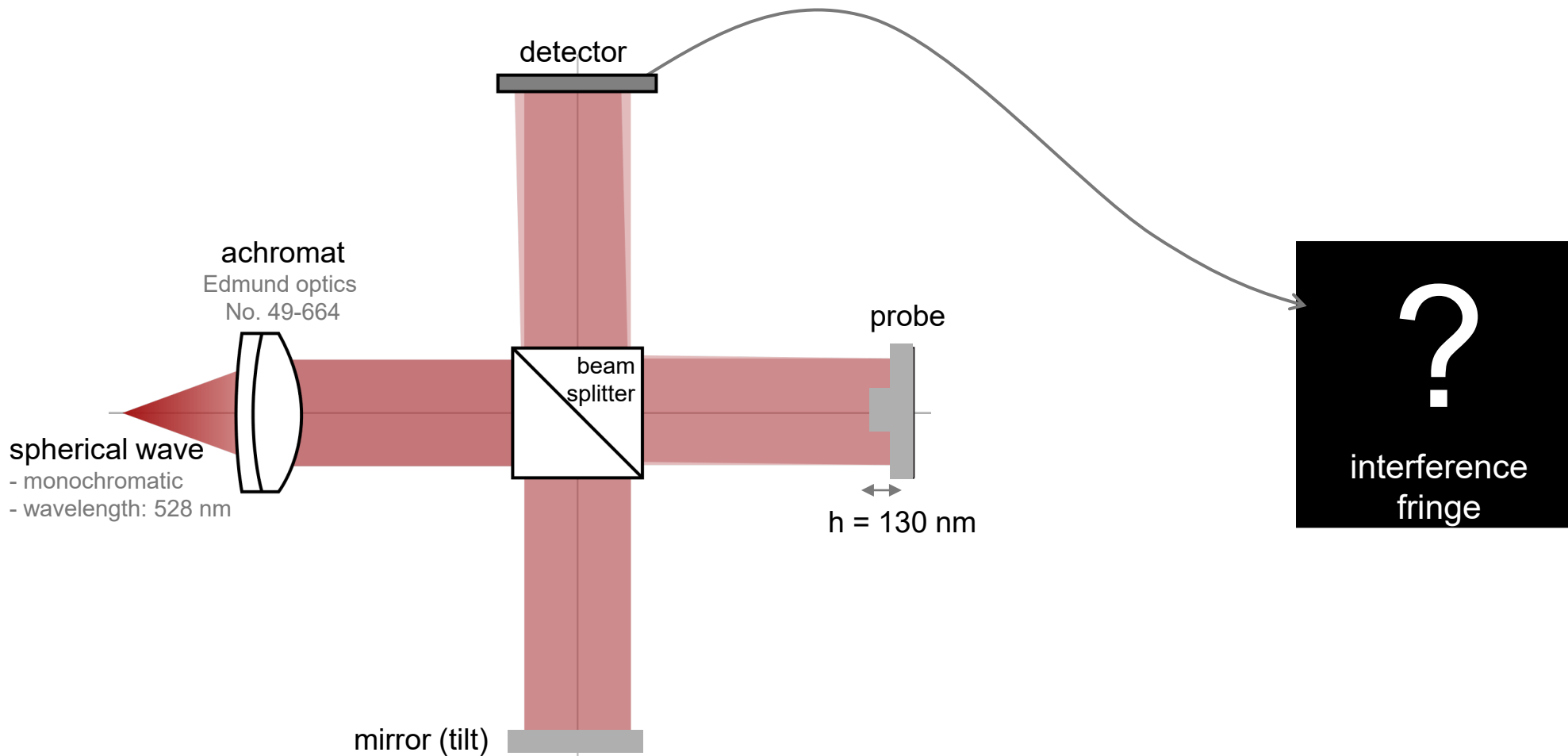
Non-Sequential Pointwise Modeling Etalon + Lens



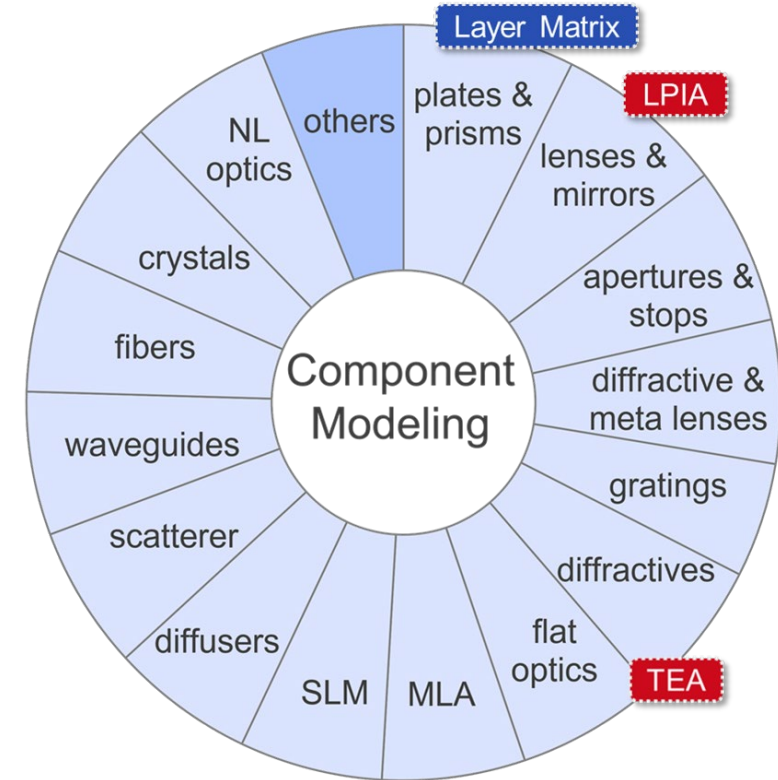
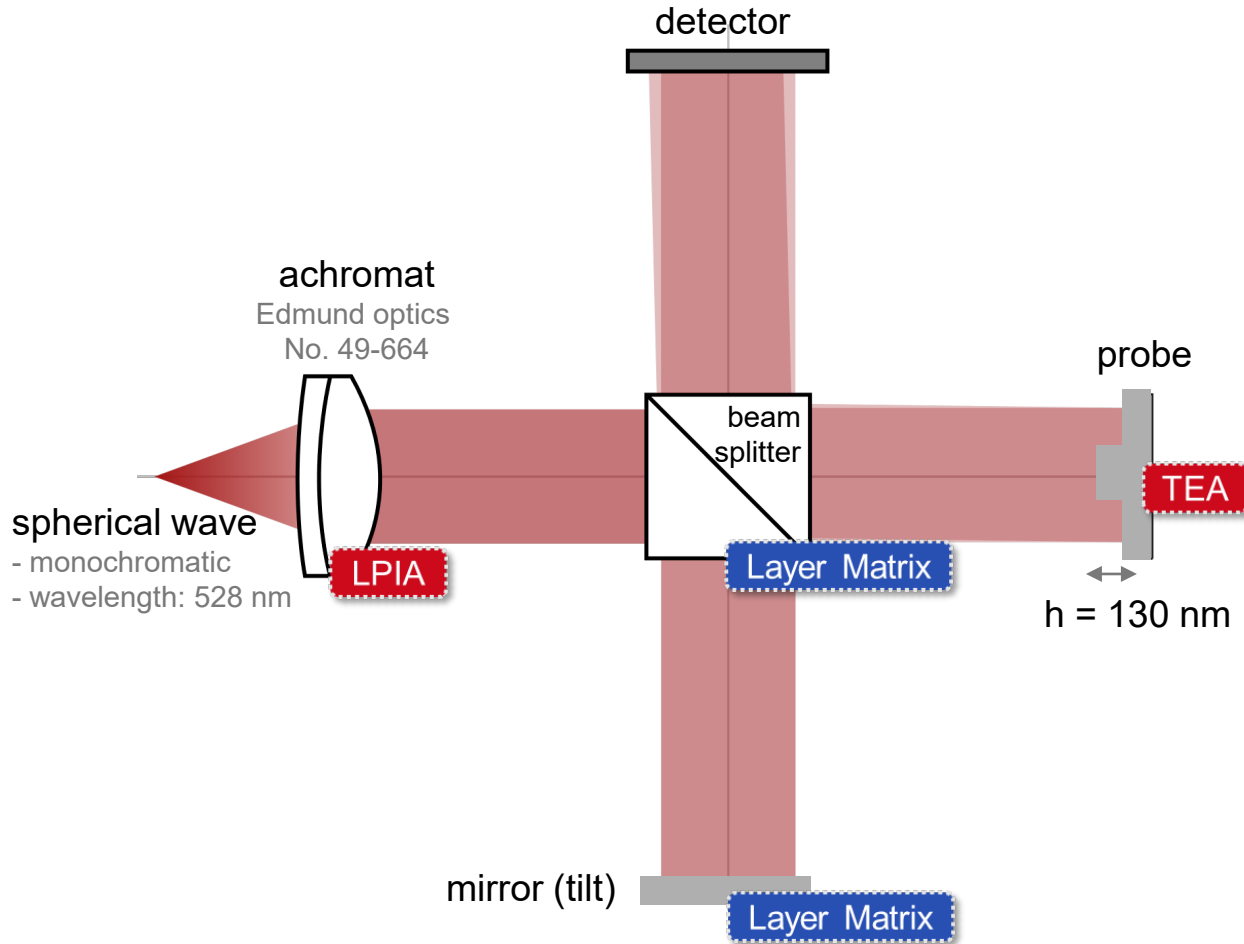
Interference of more than 10 modes by internal reflection.



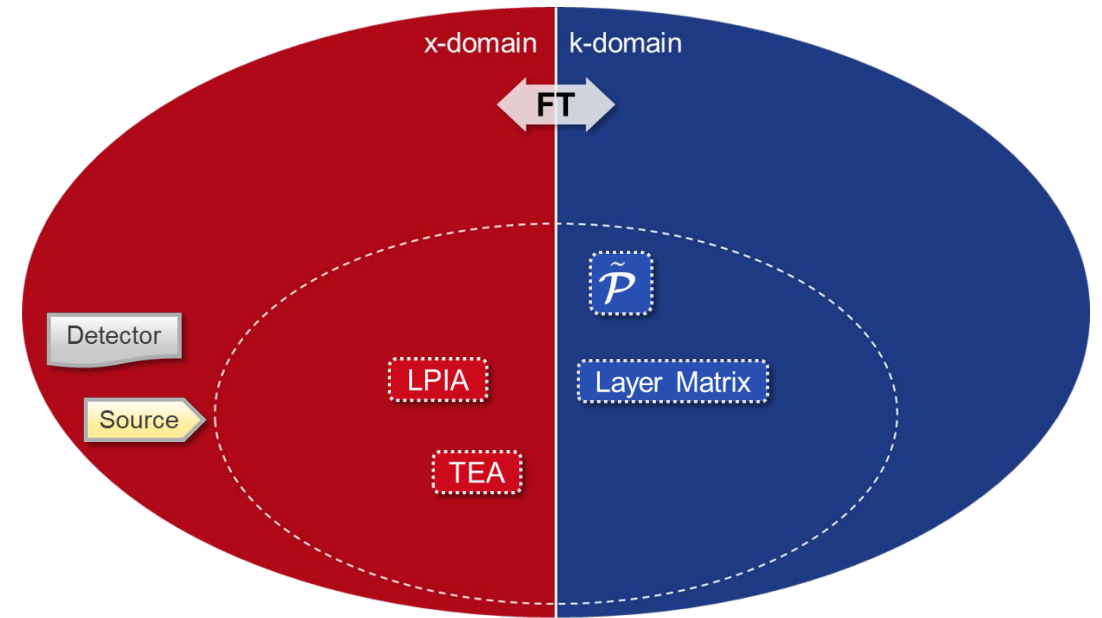
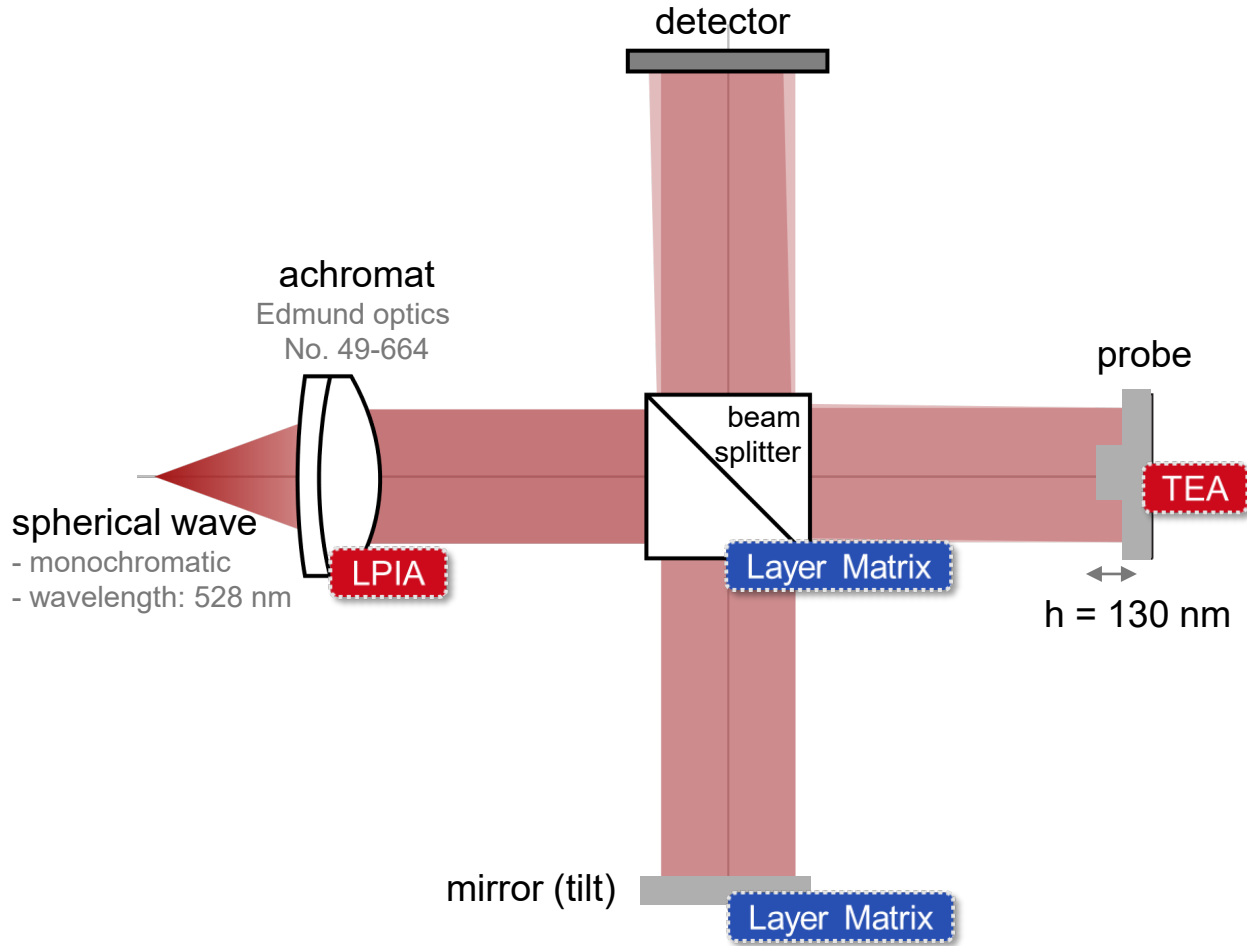
Scenario: Modeling Michelson Interferometer



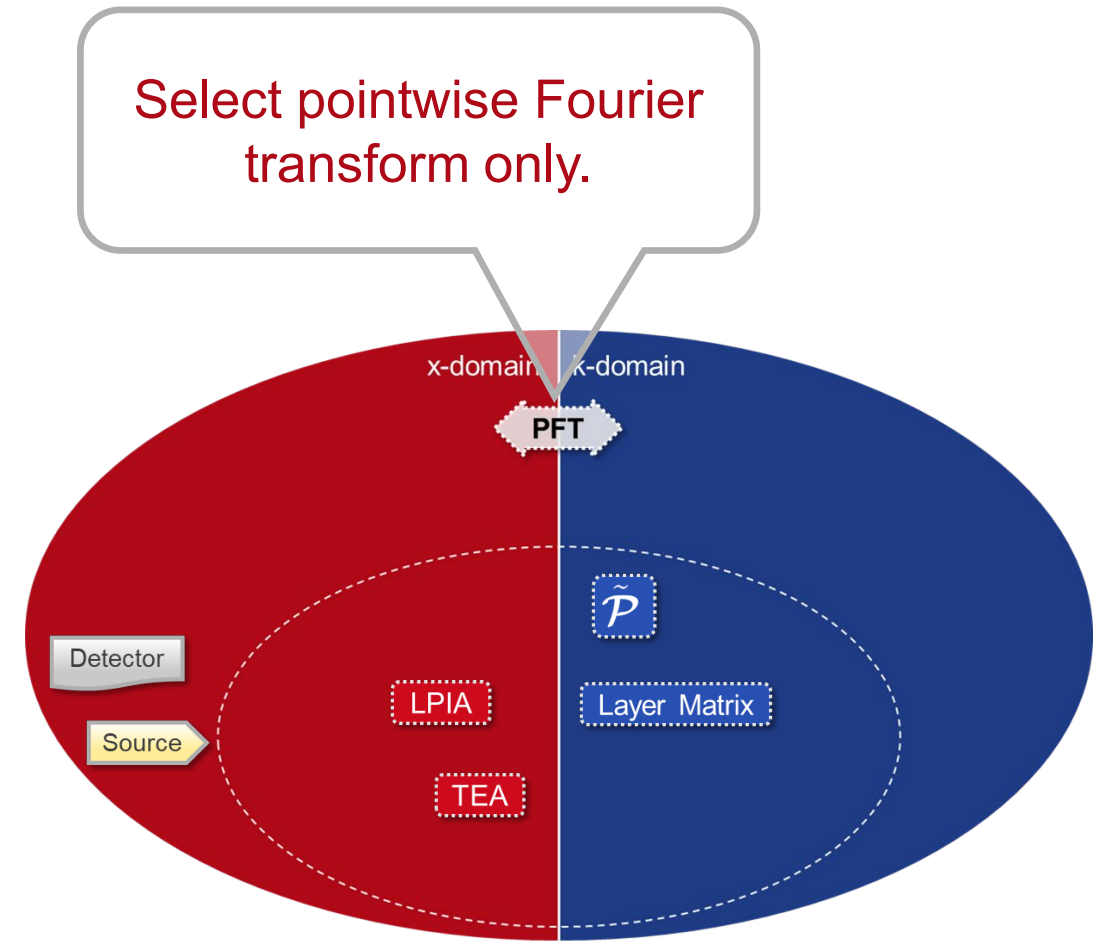
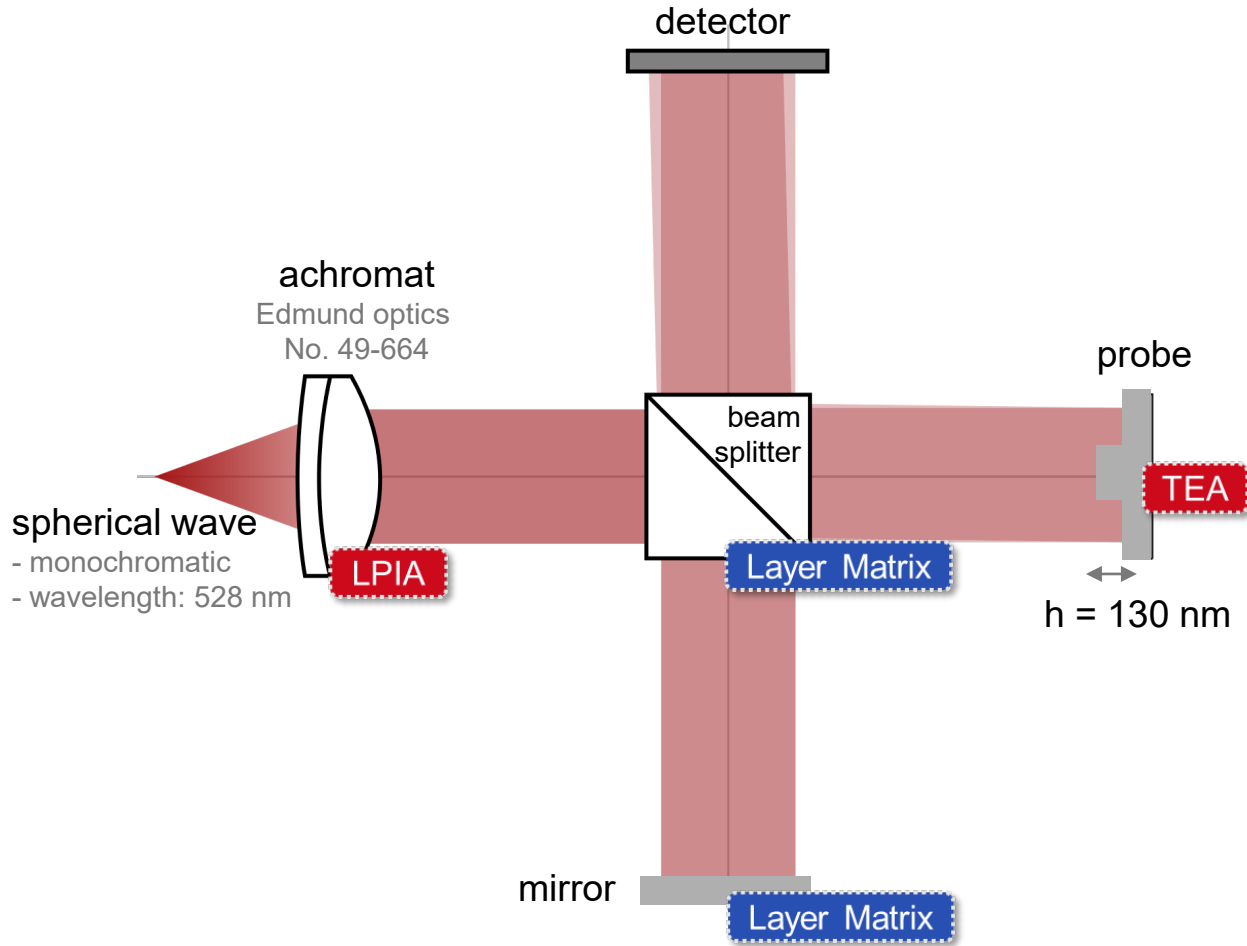
Modeling Michelson Interferometer



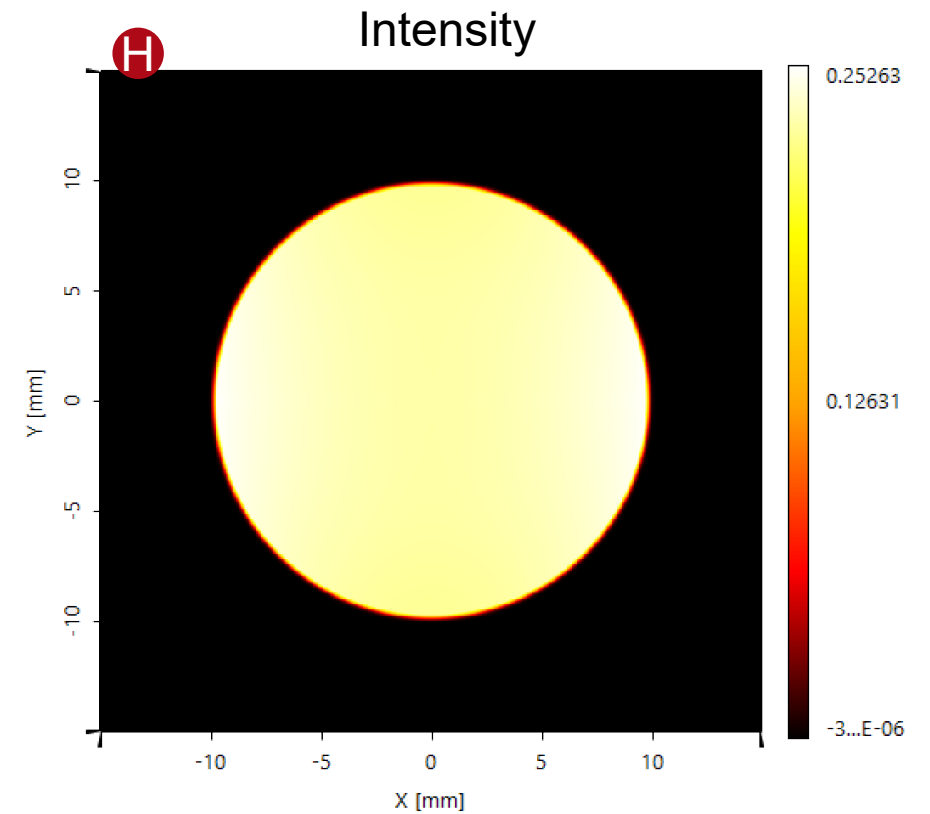
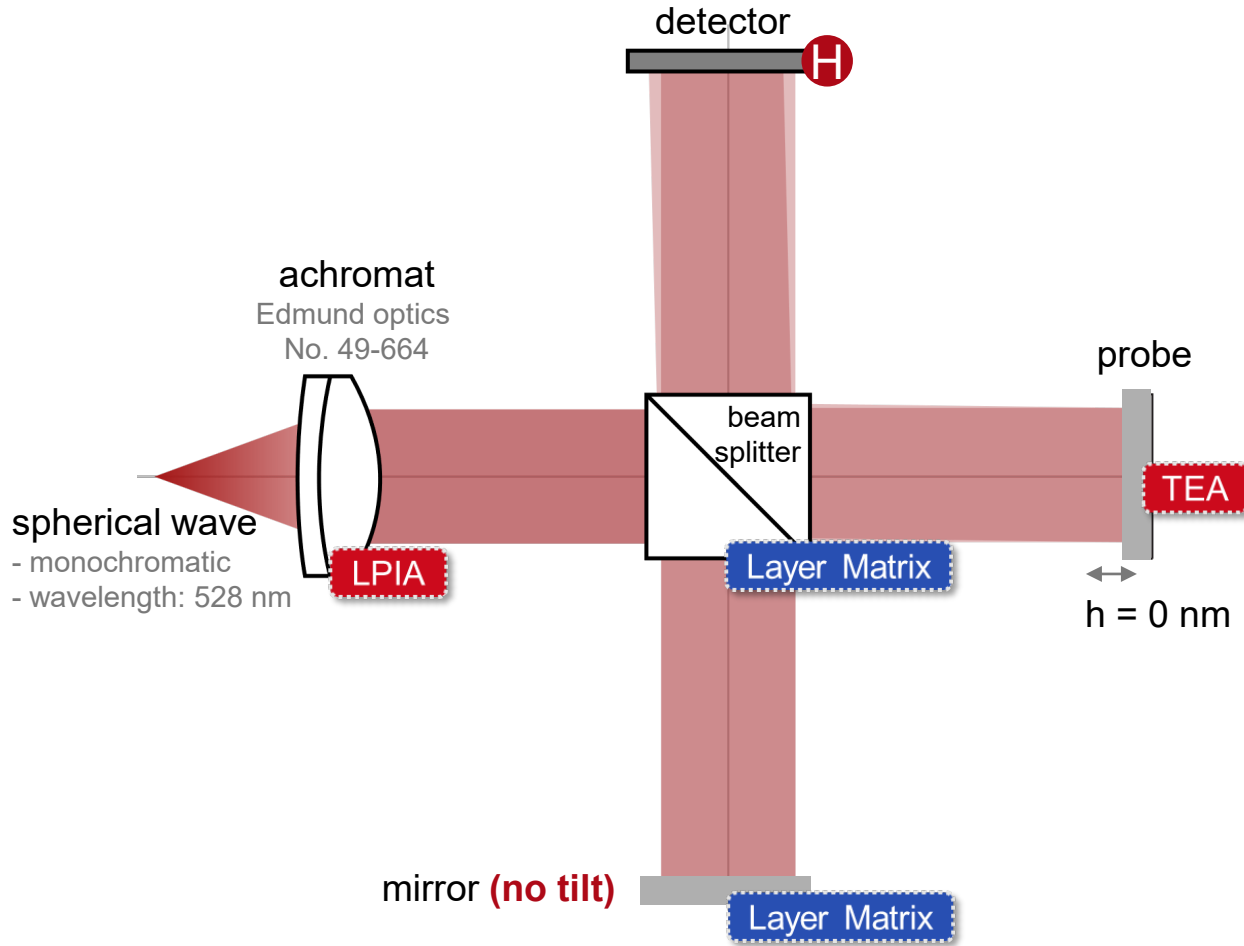
Modeling Michelson Interferometer



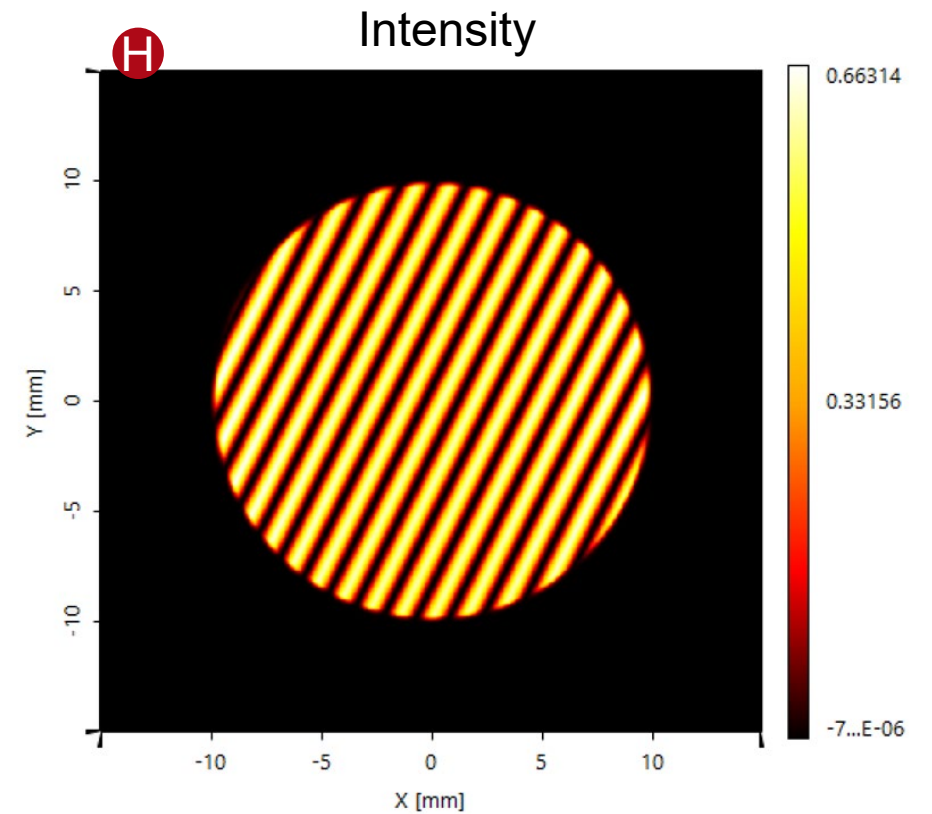
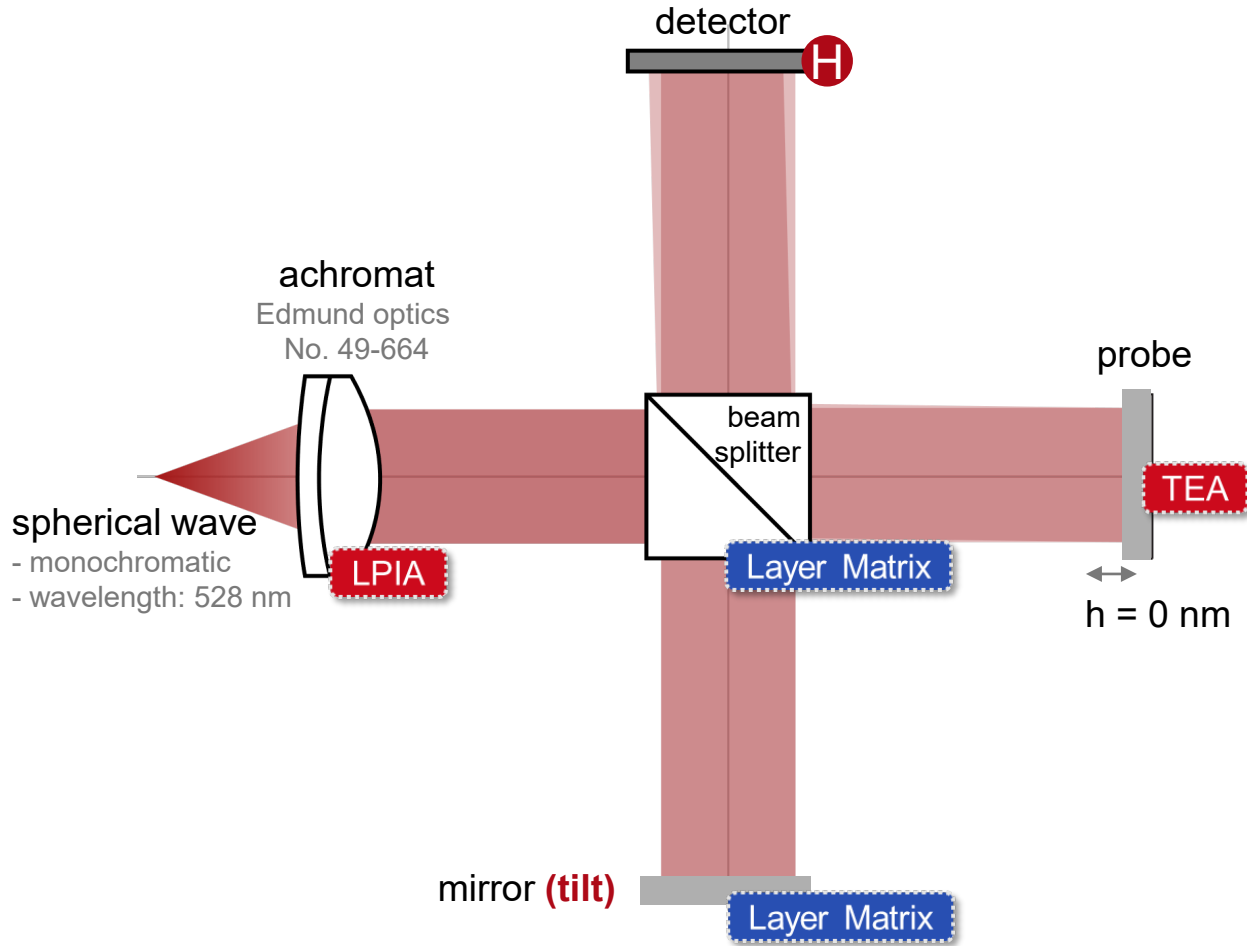
Modeling Michelson Interferometer: Pointwise



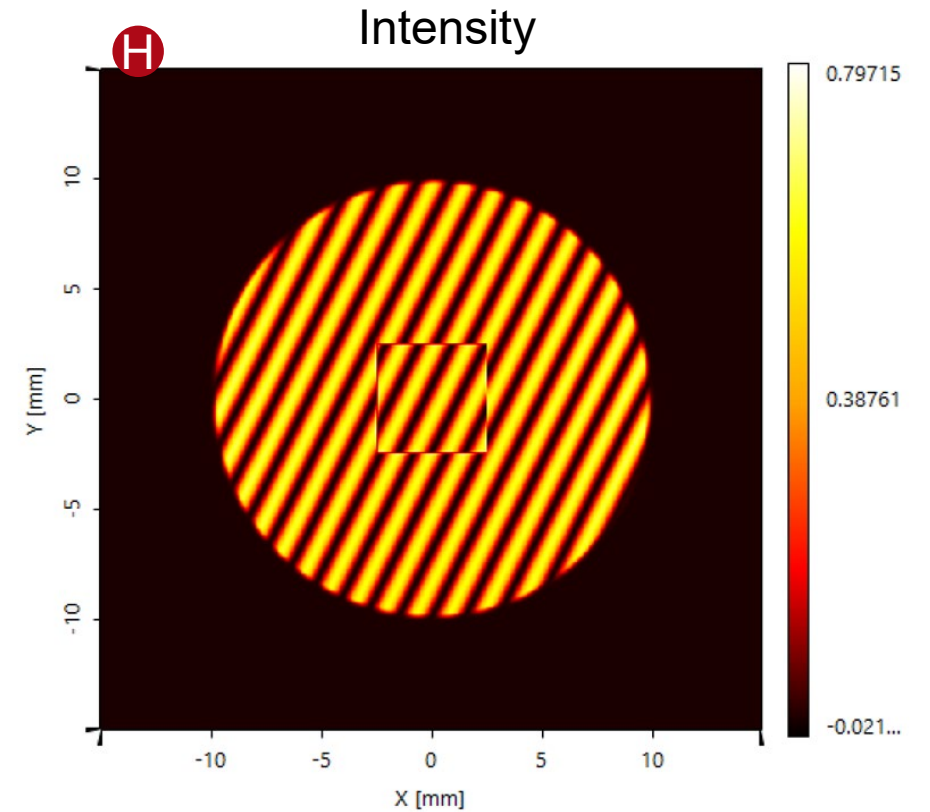
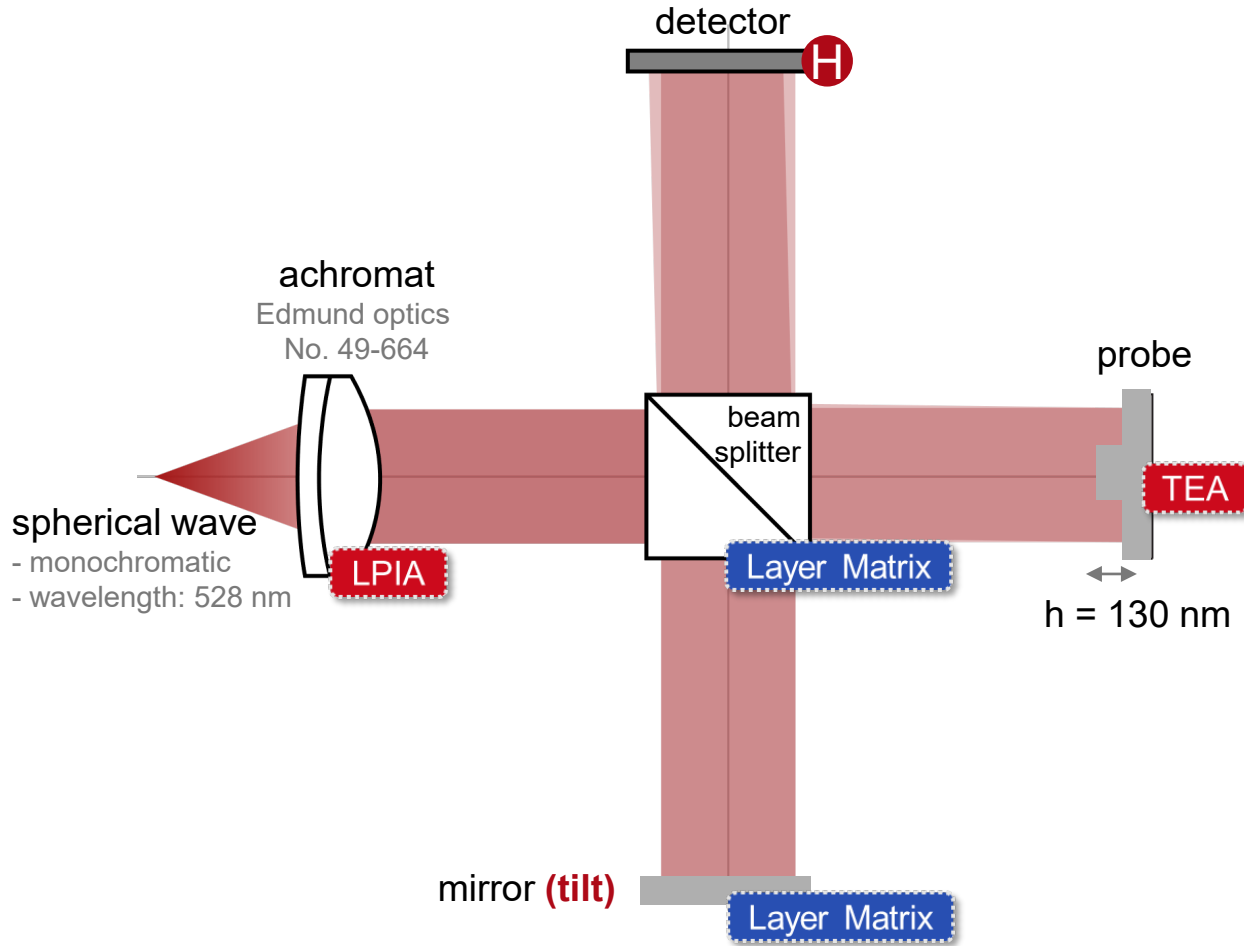
Modeling Michelson Interferometer: Pointwise



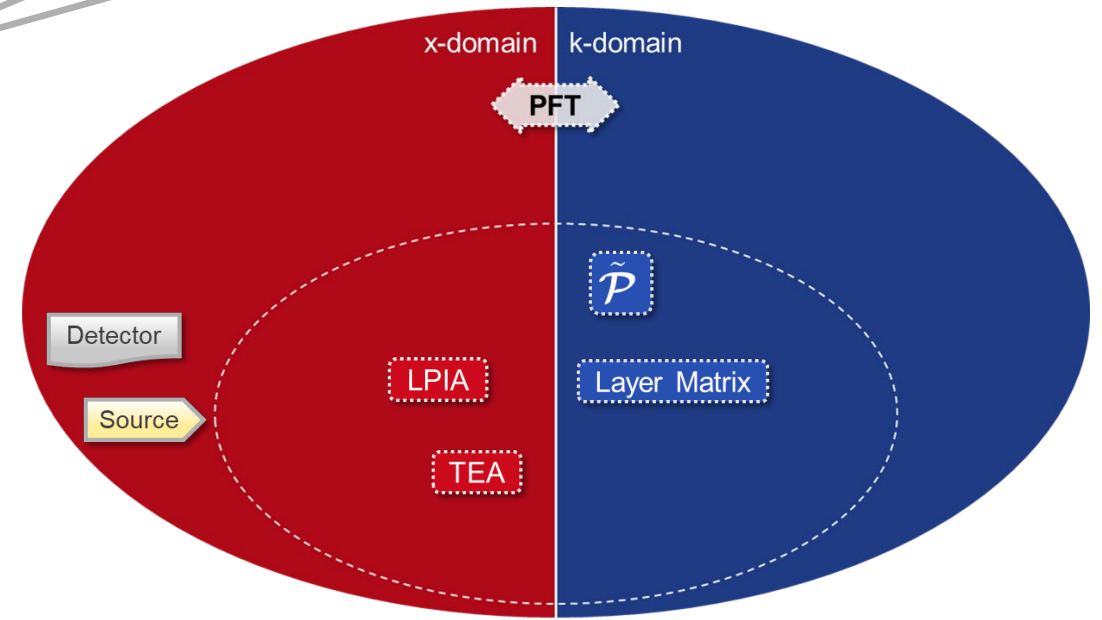
Modeling Michelson Interferometer: Pointwise



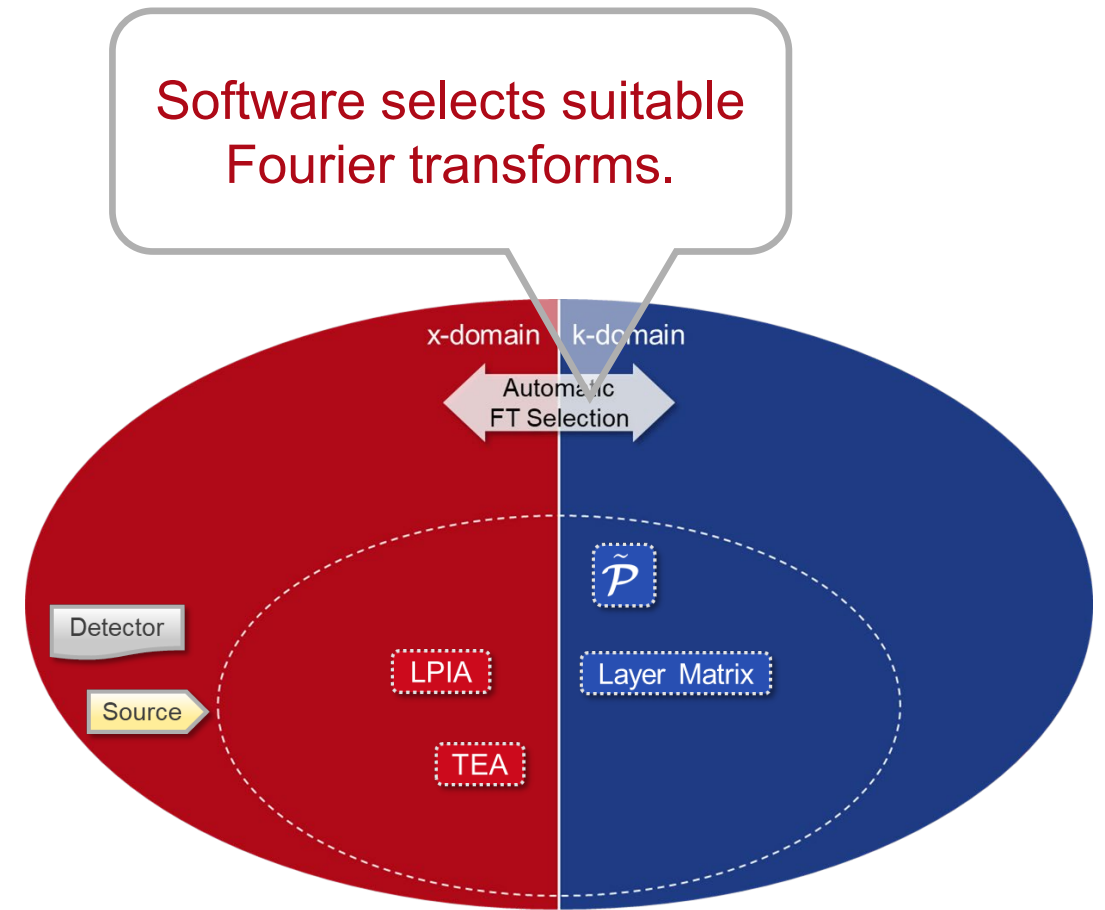
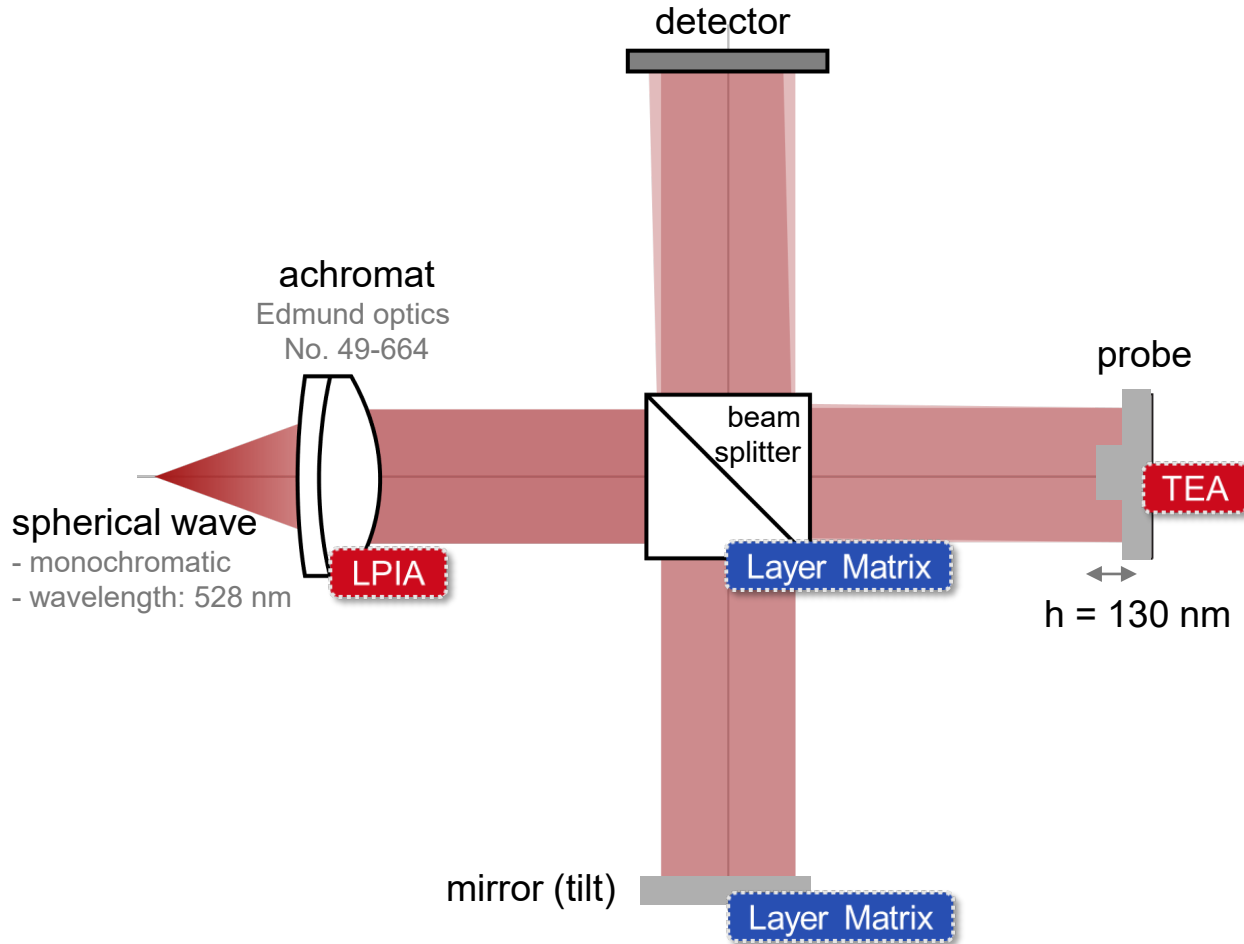
Modeling Michelson Interferometer: Pointwise



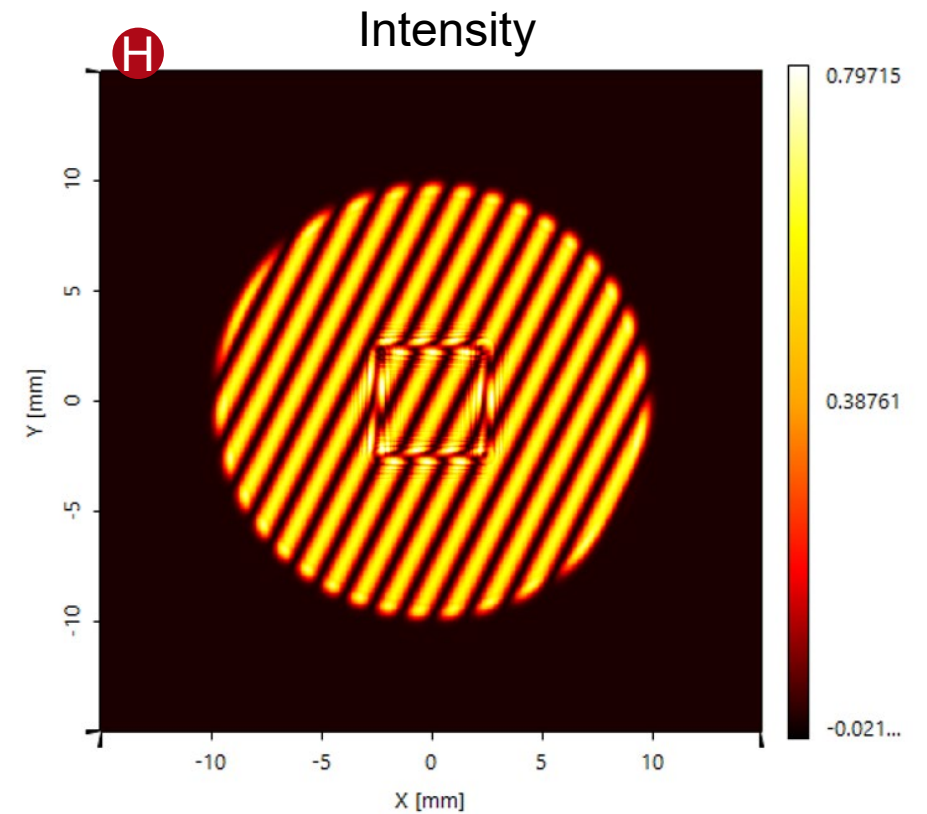
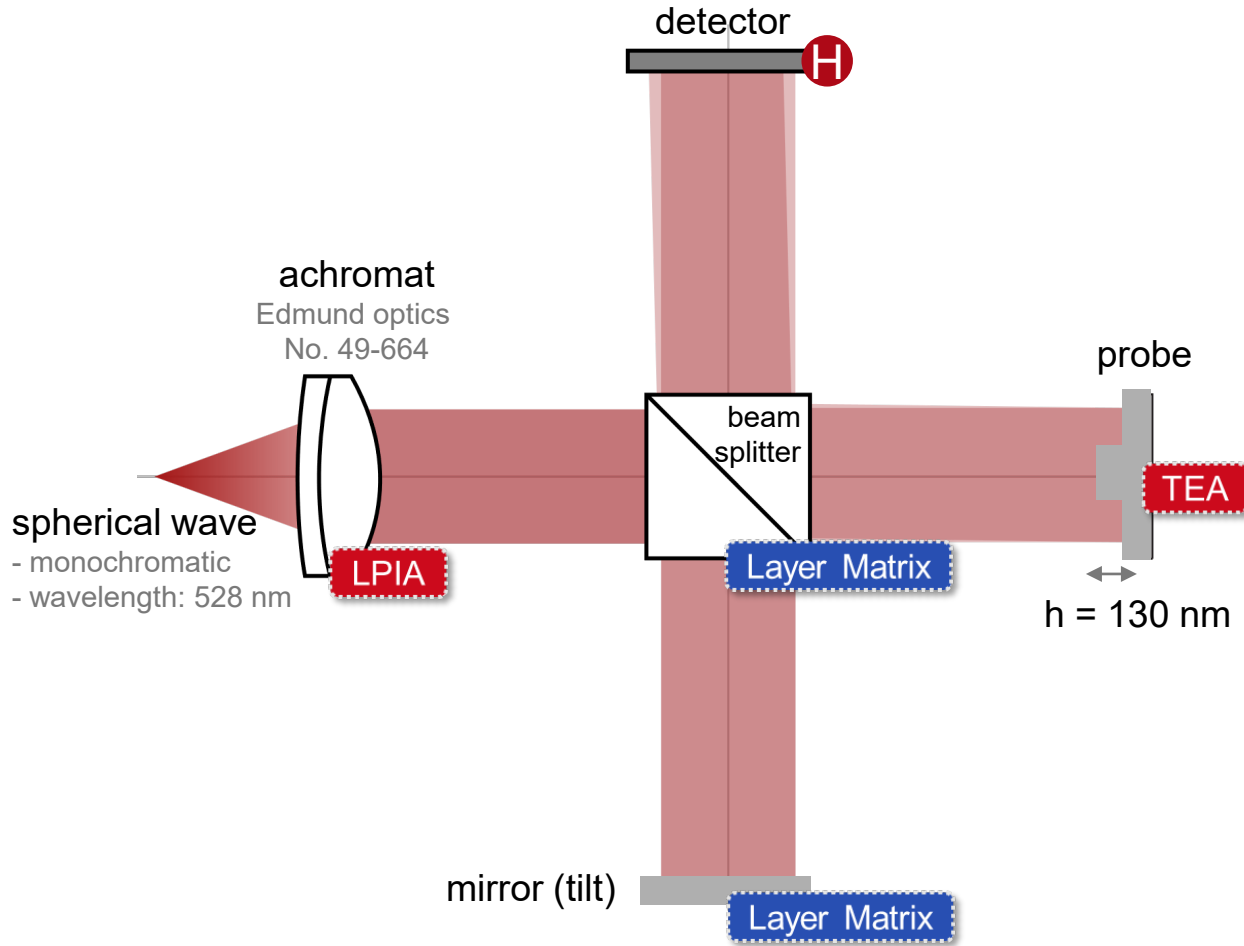
Diffraction at sidewalls!



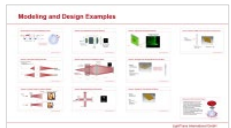
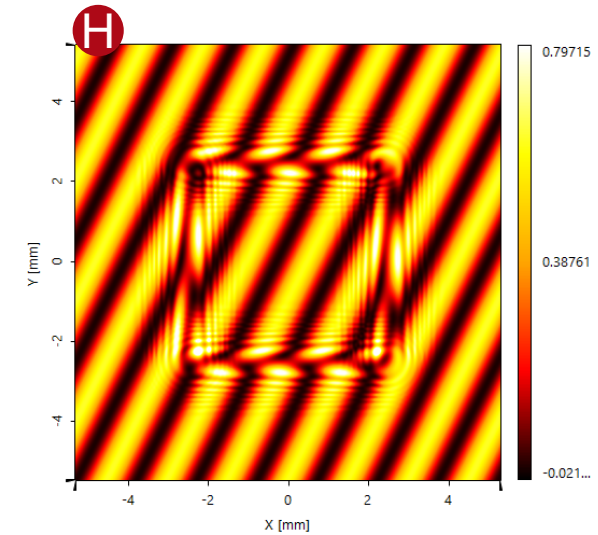
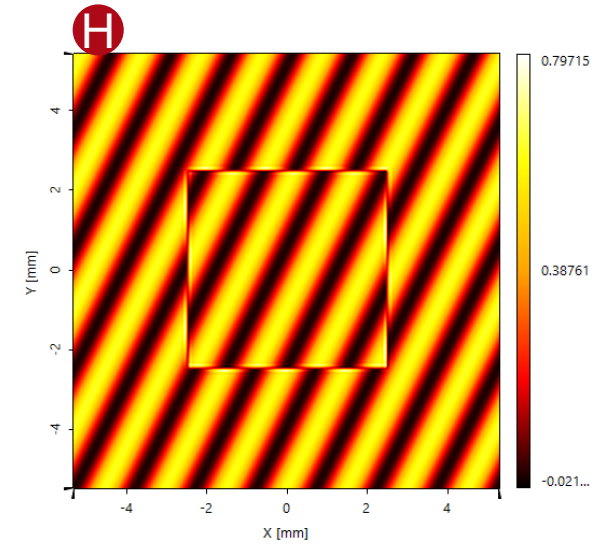
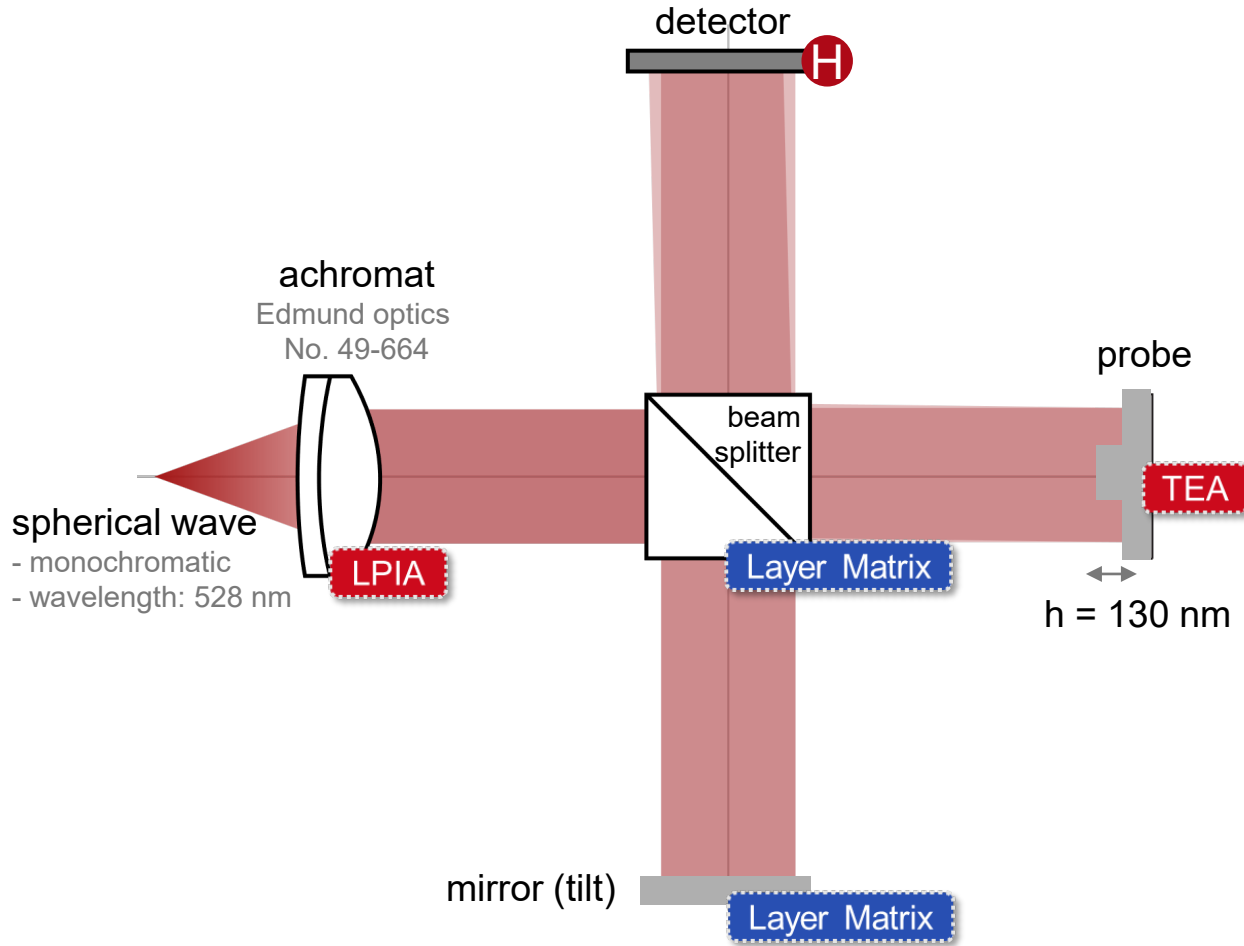
Modeling Michelson Interferometer: Automatic FT Selection



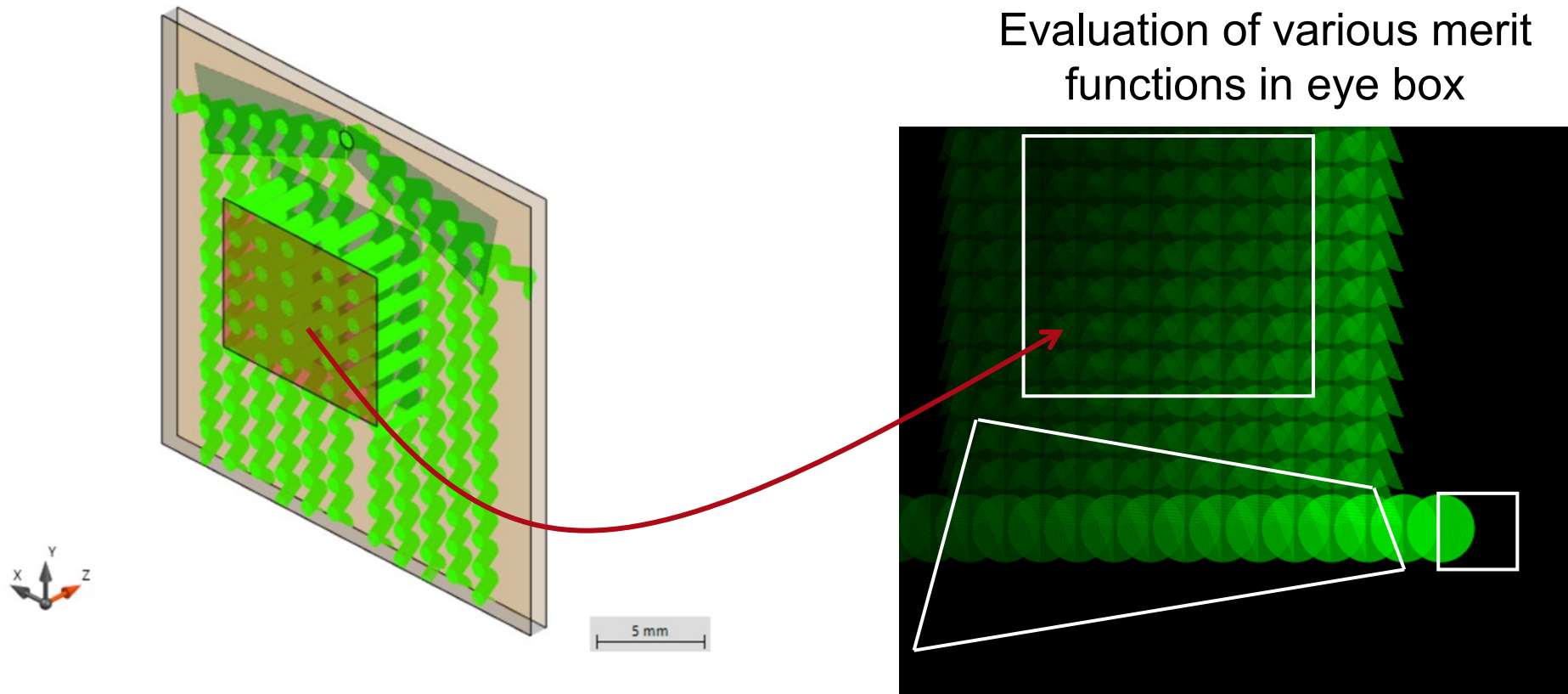
Modeling Michelson Interferometer: Automatic FT Selection



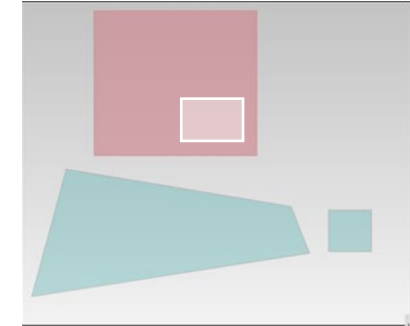
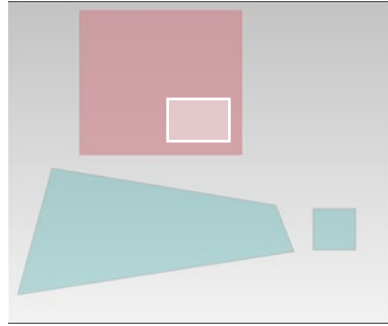
Modeling: PFT vs. Automatic FT Selection



Scenario: Light Guide for Augmented Reality



Intensity Detector: Output View in Eyebbox

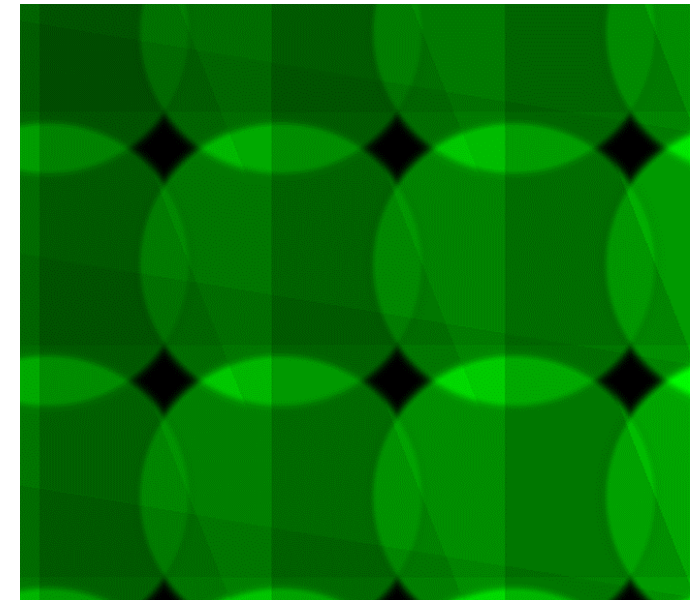
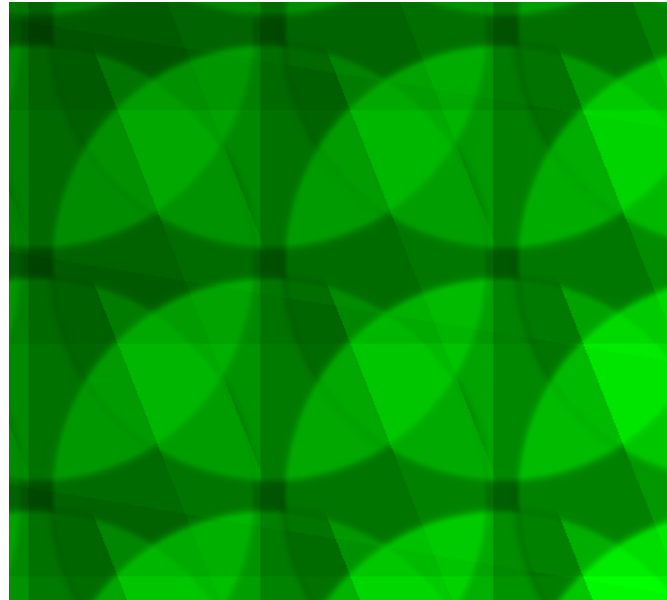


$$E_x^{\text{in}} = 1, E_y^{\text{in}} = 0$$

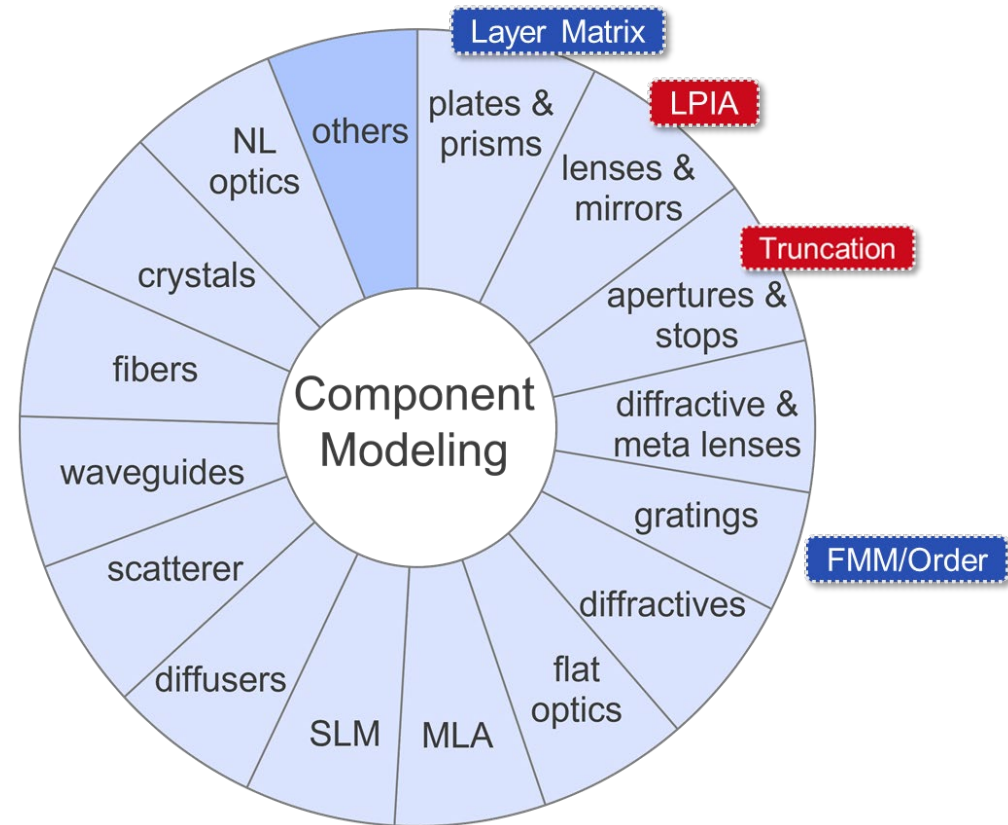
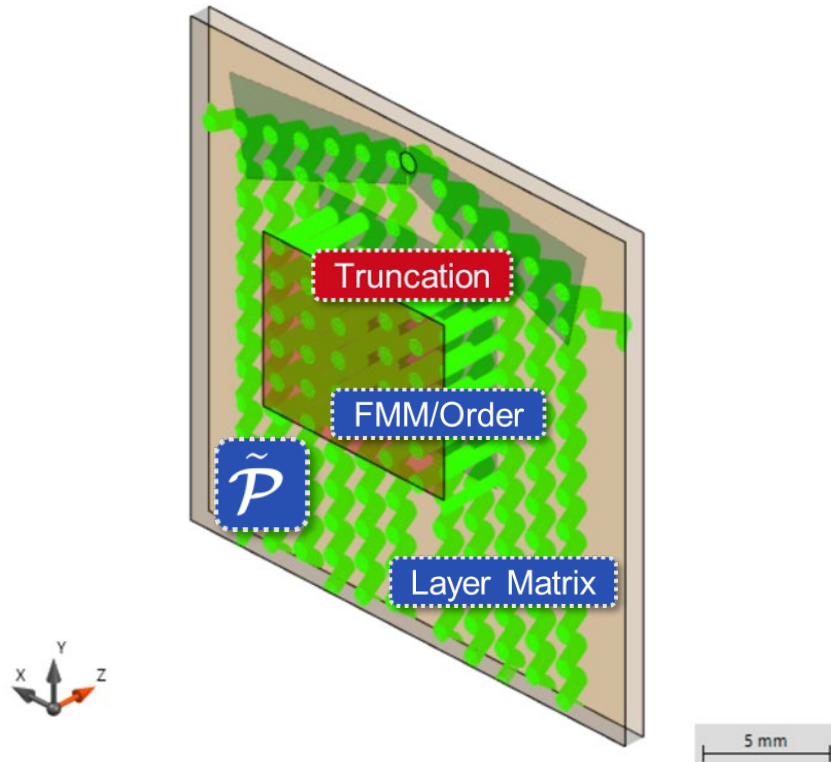
$$\lambda = 530 \text{ nm}$$

$r = 1.5 \text{ mm}$ (left) and 1 mm (right)

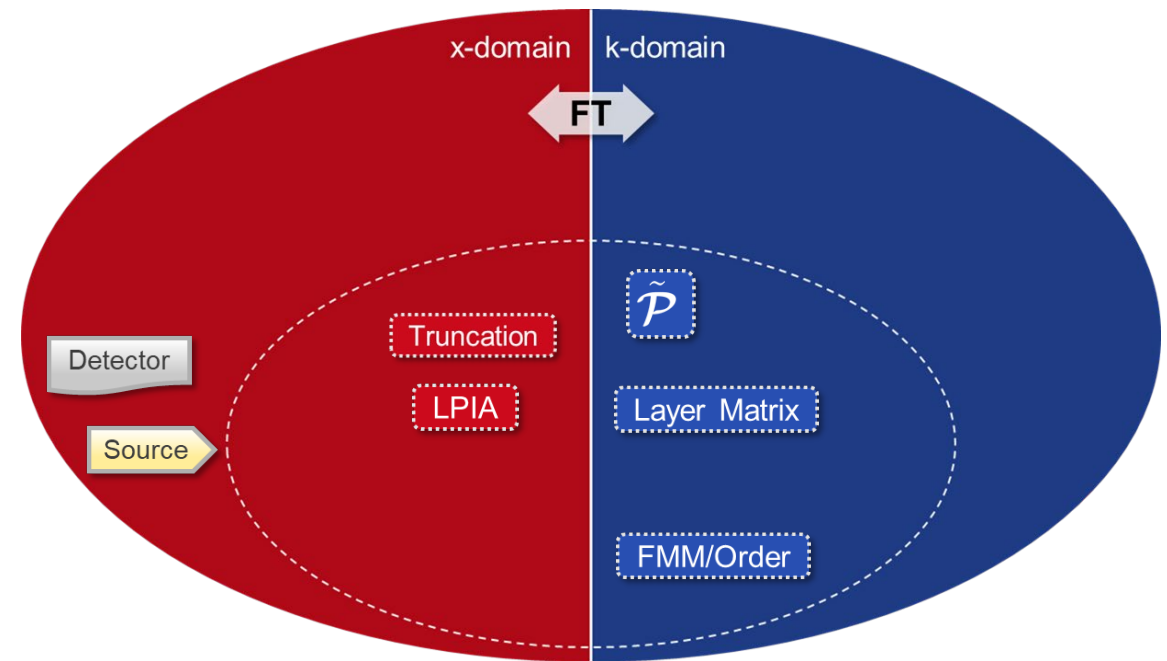
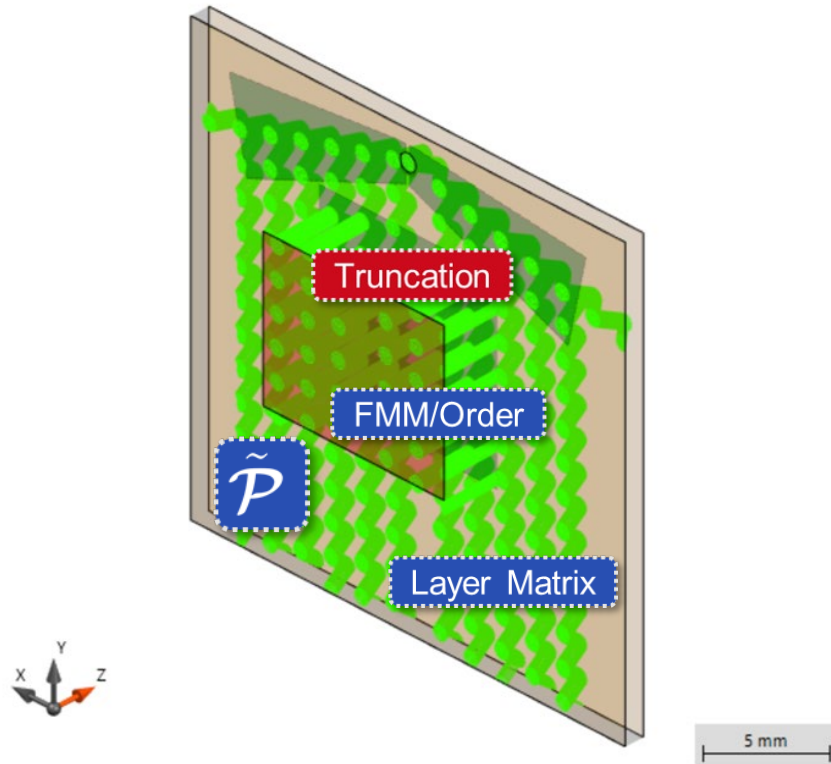
Source beam radius



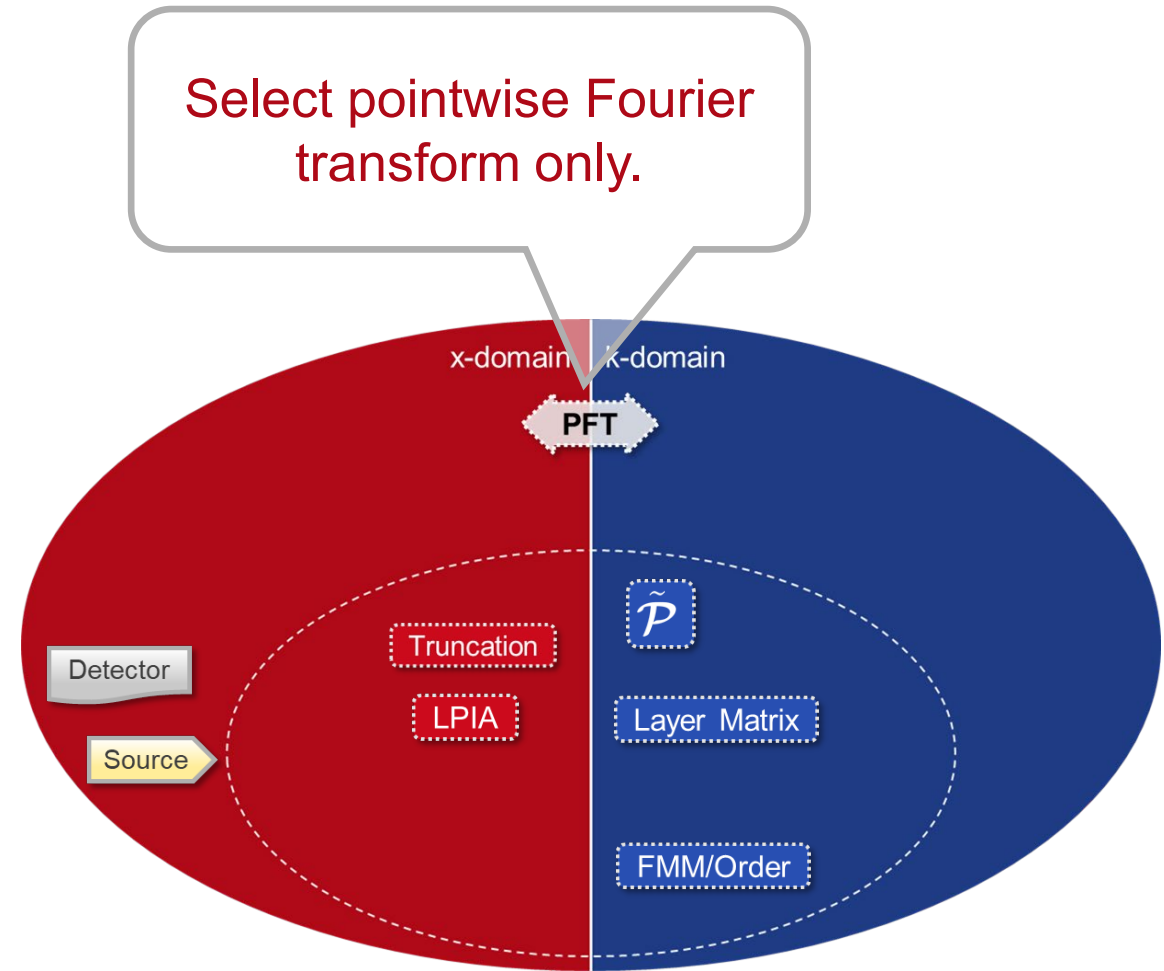
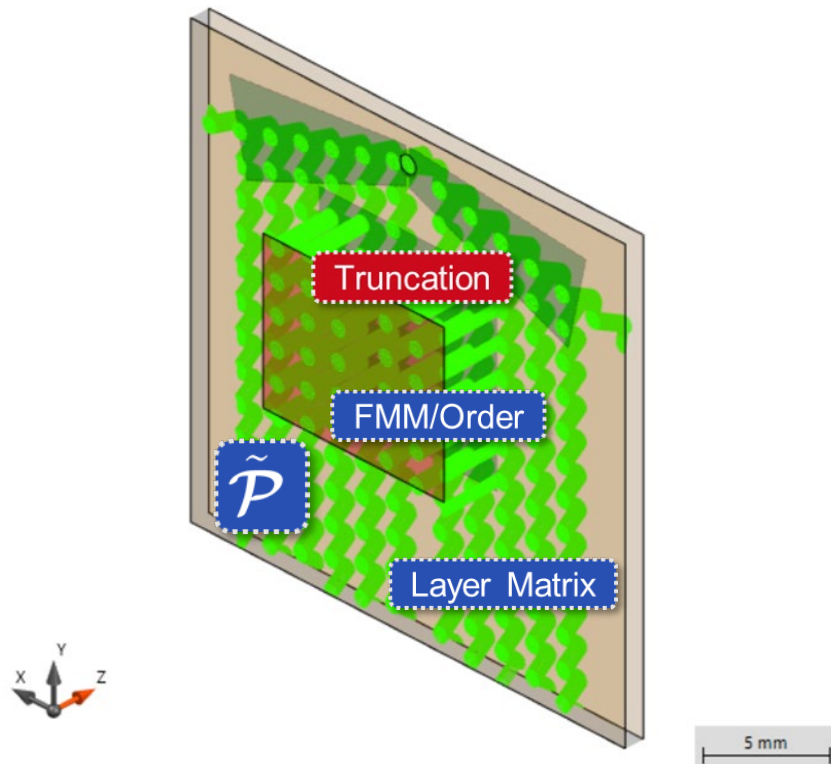
Light Guide for Augmented Reality: Modeling



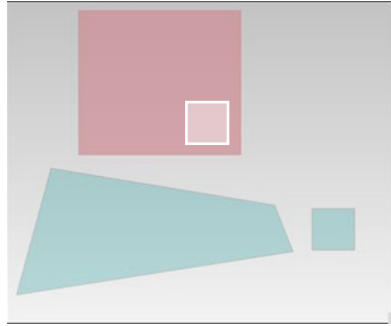
Light Guide for Augmented Reality: Modeling



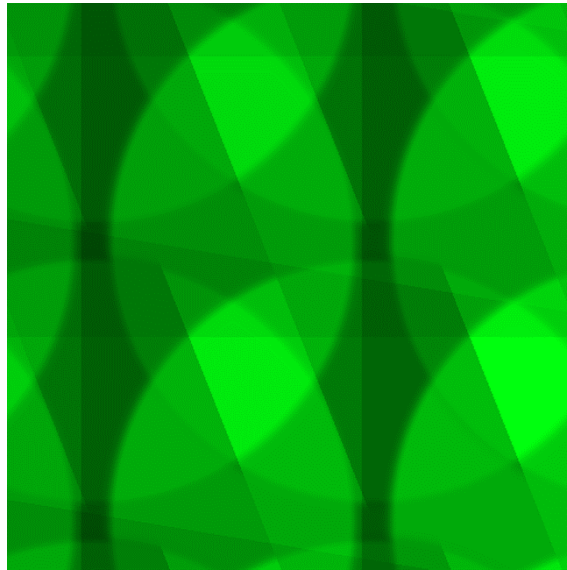
Light Guide for Augmented Reality: Pointwise Modeling



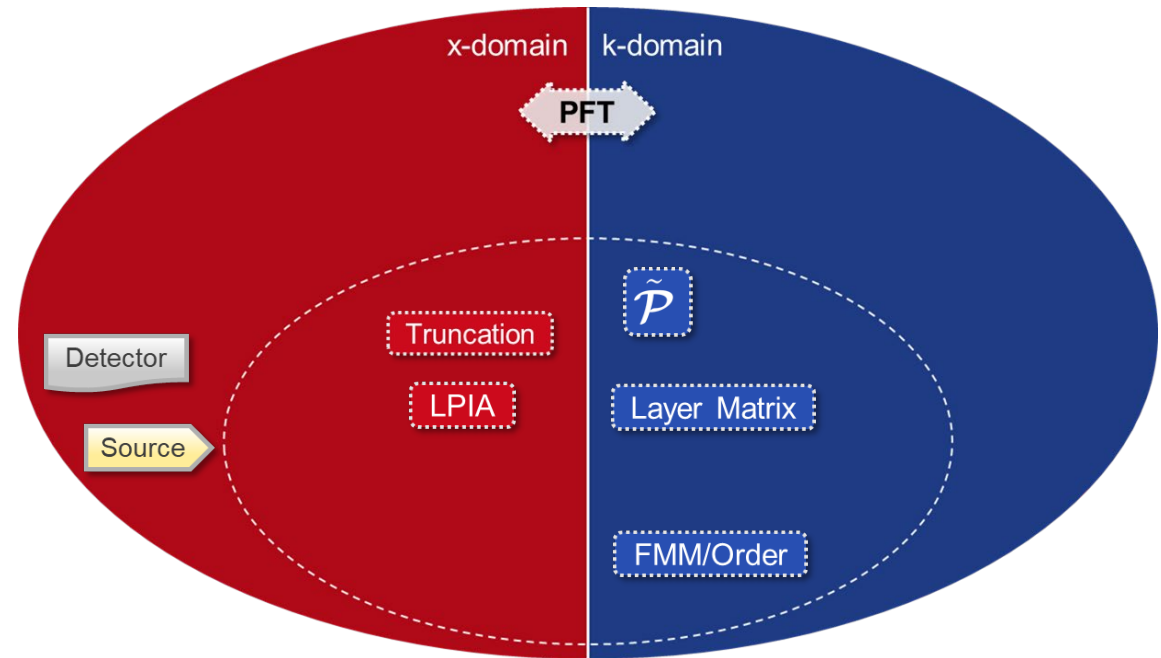
Intensity Detector: Eyebow



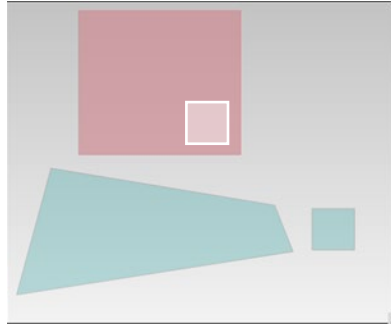
$E_x^{\text{in}} = 1, E_y^{\text{in}} = 0$
 $\lambda = 530 \text{ nm}$
 $\Delta\lambda = 0 \text{ nm}$
 $r = 1.5 \text{ mm}$



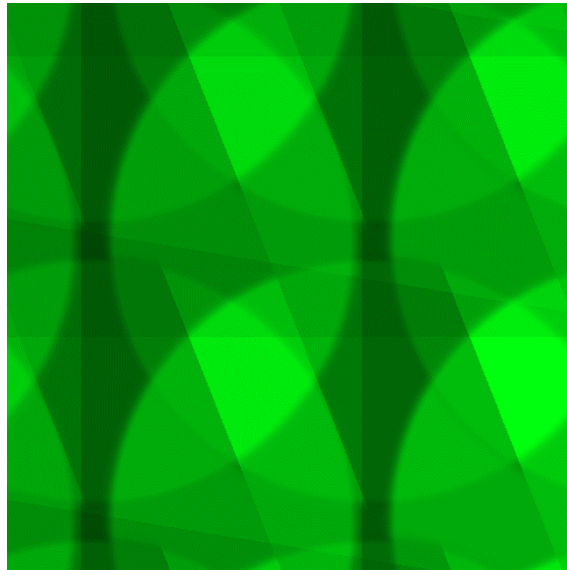
PFT



Intensity Detector: Eyebow

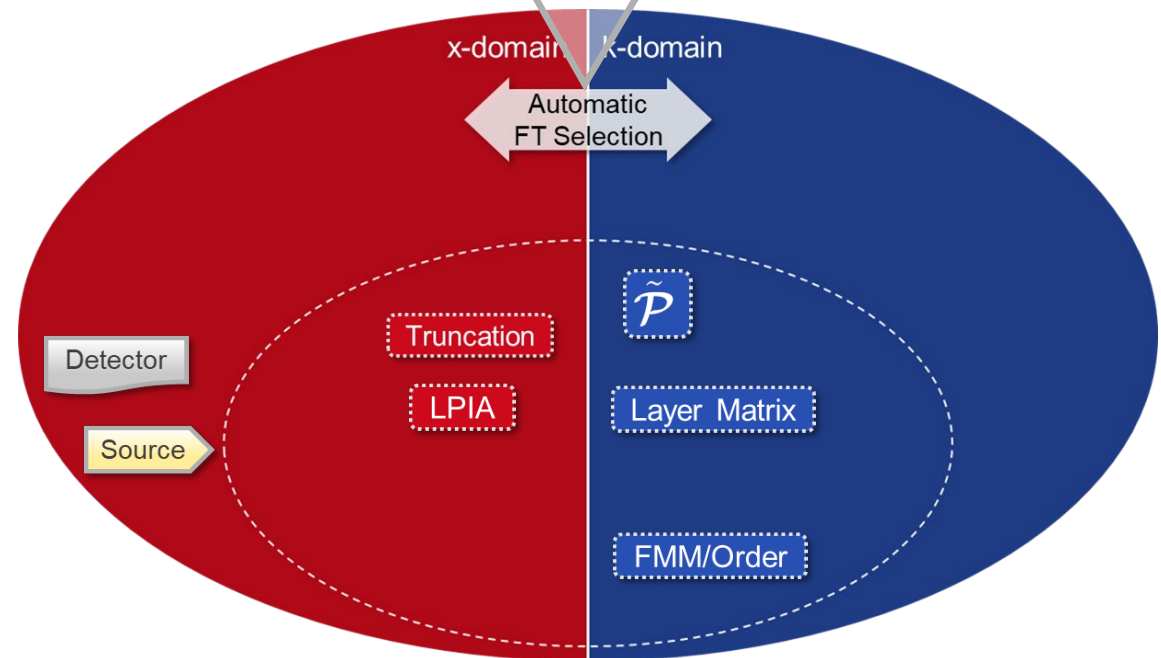


$E_x^{\text{in}} = 1, E_y^{\text{in}} = 0$
 $\lambda = 530 \text{ nm}$
 $\Delta\lambda = 0 \text{ nm}$
 $r = 1.5 \text{ mm}$

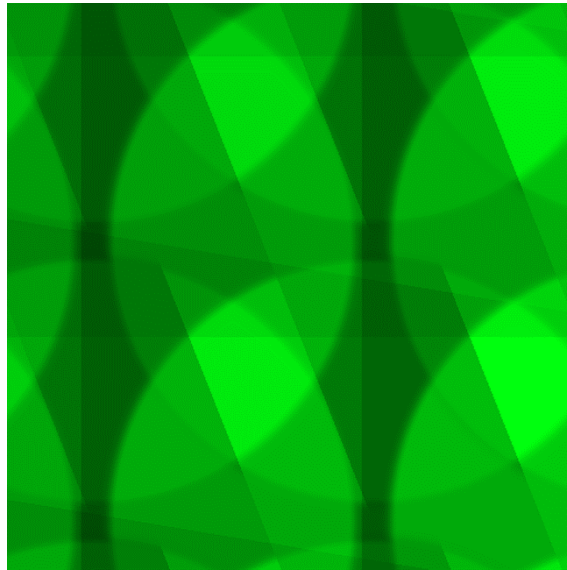
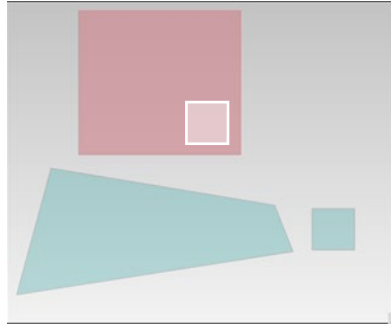


PFT

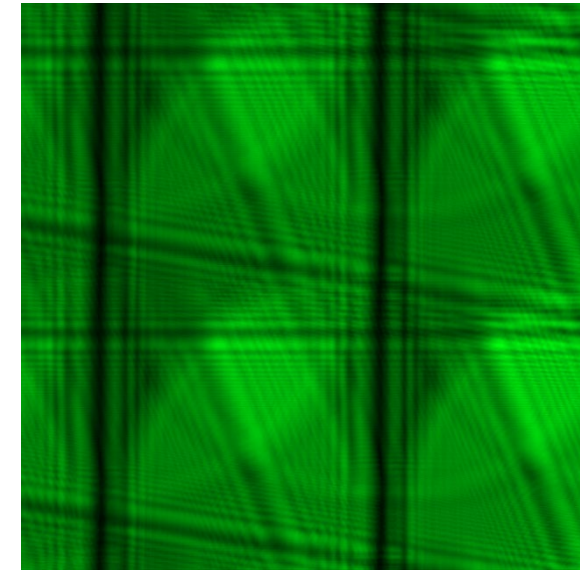
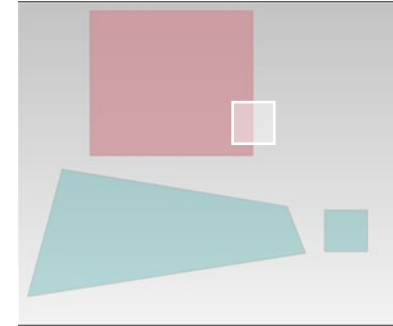
Software selects suitable Fourier transforms.



Intensity Detector: Eyebox



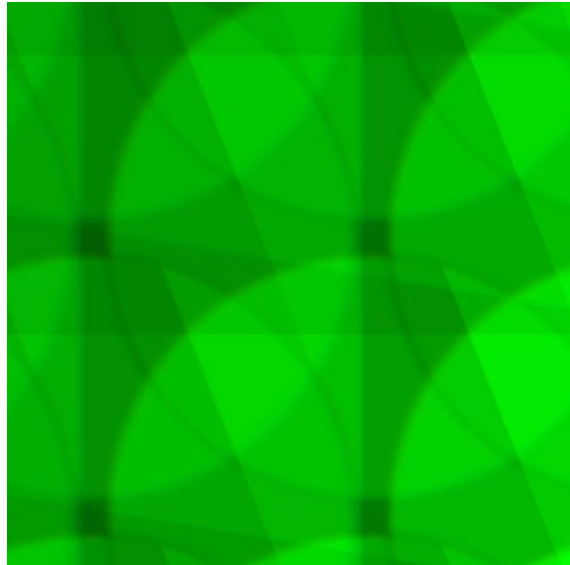
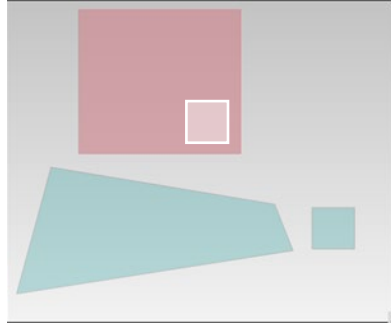
PFT



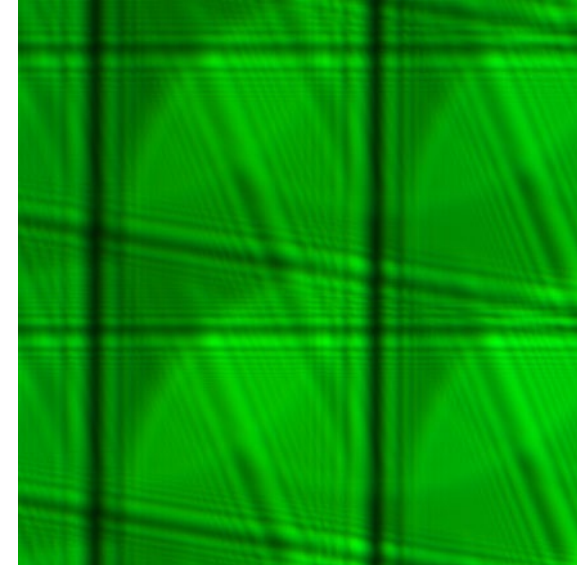
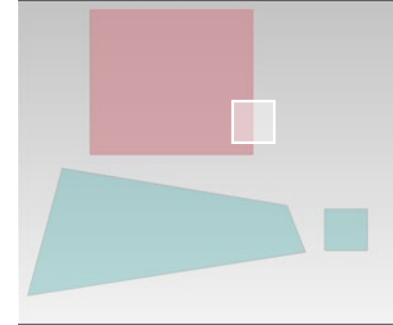
Automatic FT selection

$E_x^{\text{in}} = 1, E_y^{\text{in}} = 0$
 $\lambda = 530 \text{ nm}$
 $\Delta\lambda = 0 \text{ nm}$
 $r = 1.5 \text{ mm}$

Intensity Detector: Eyebox (Partial Coherent)

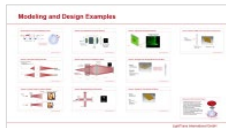


PFT



Automatic FT selection

$E_x^{\text{in}} = 1, E_y^{\text{in}} = 0$
 $\lambda = 530 \text{ nm}$
 $\Delta\lambda = 1 \text{ nm}$
 $r = 1.5 \text{ mm}$



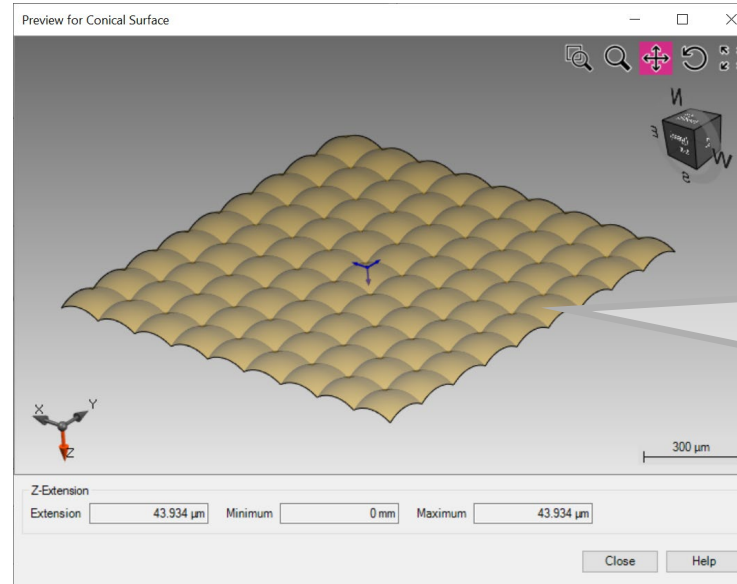
Scenario: Propagate Light Through Microlens Array (MLA)

Light Source:

- Plane wave
- Wavelength: 640 nm
- Linearly polarized (Ex)

Microlens Array:

- Conical surface
- Array: 9x9
- Pitch: 150 μm x 150 μm
- Radius of curvature: 150 μm
- Substrate: BK7
- Thickness: 1 mm



Diffraction effects at boundaries should be included in modeling.



Scenario: Propagate Light Through Microlens Array (MLA)

Light Source:

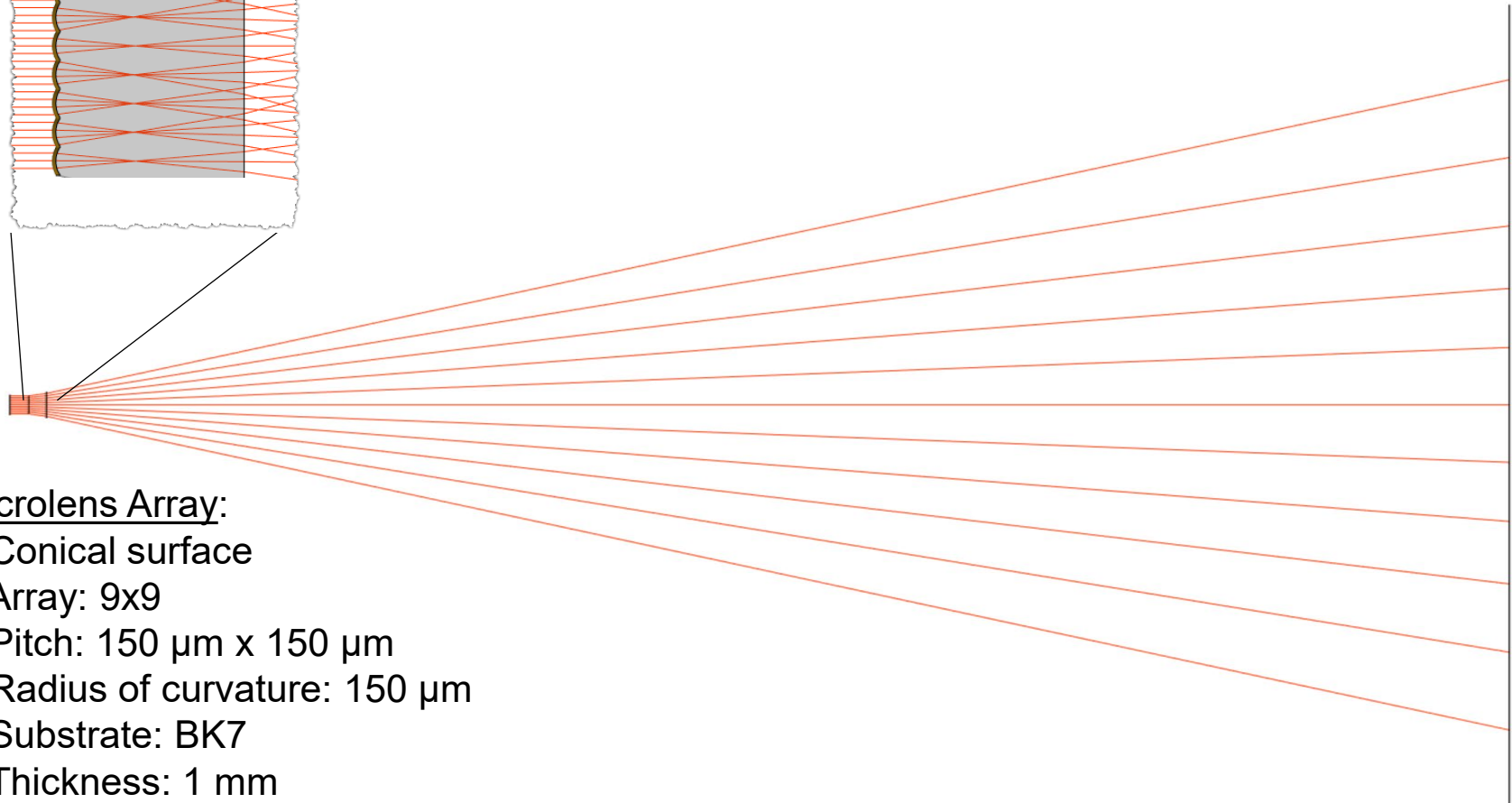
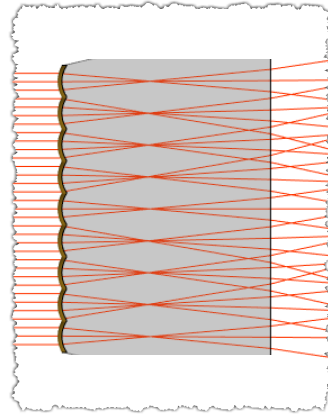
- Plane wave
- Wavelength: 640 nm
- Linearly polarized (Ex)

Microlens Array:

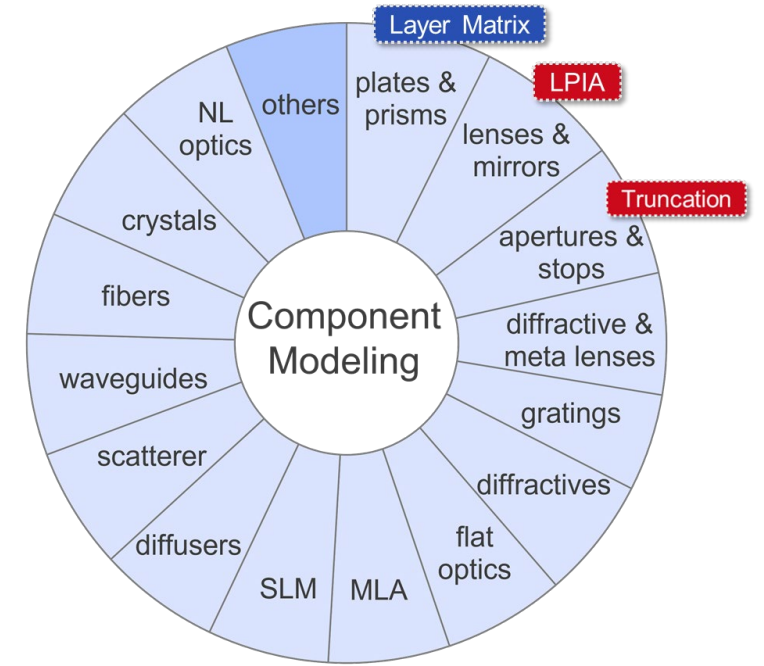
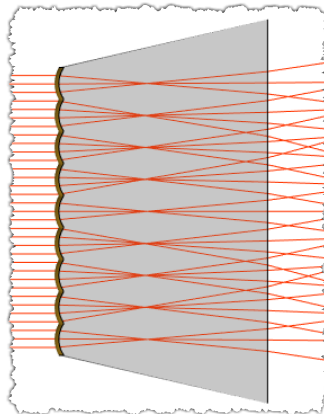
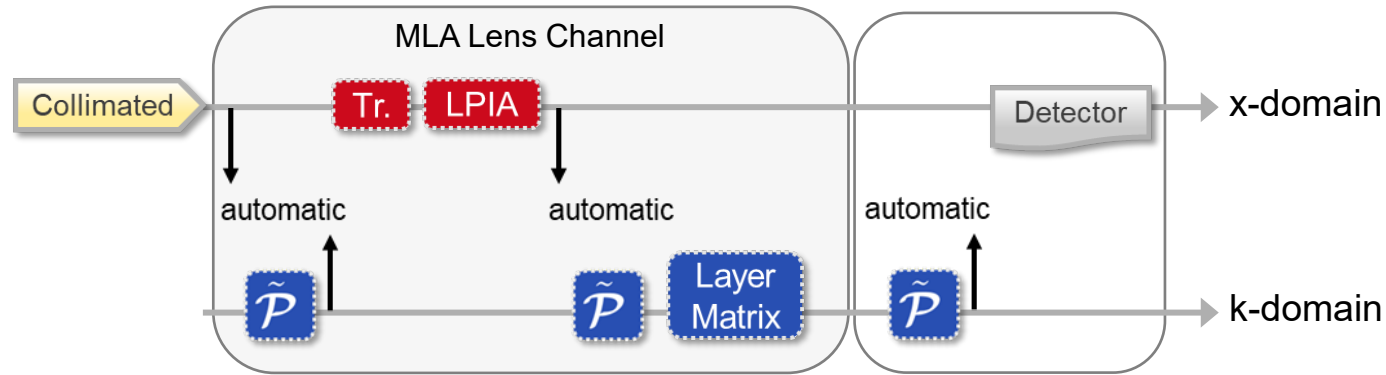
- Conical surface
- Array: 9x9
- Pitch: 150 μm x 150 μm
- Radius of curvature: 150 μm
- Substrate: BK7
- Thickness: 1 mm

Detector:

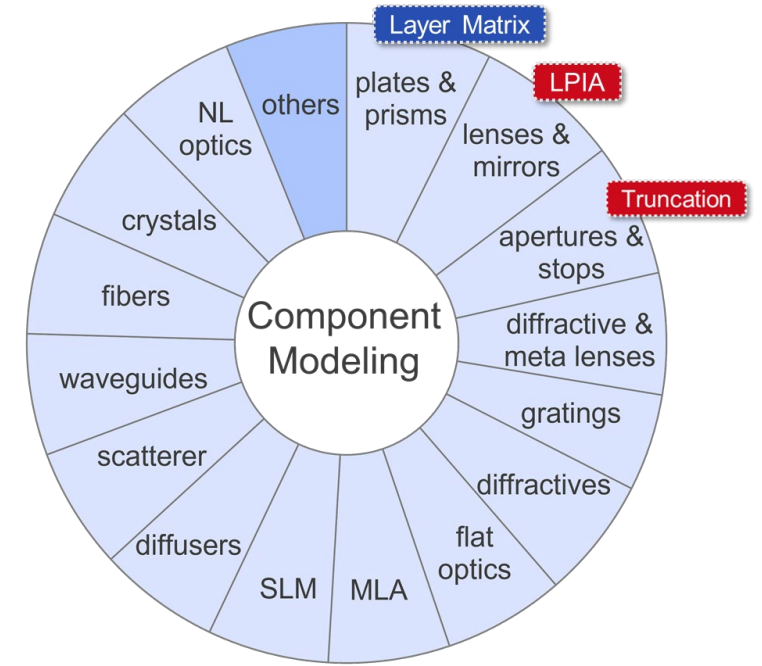
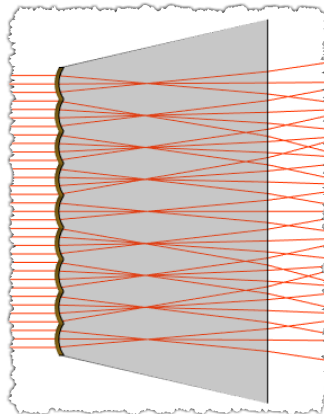
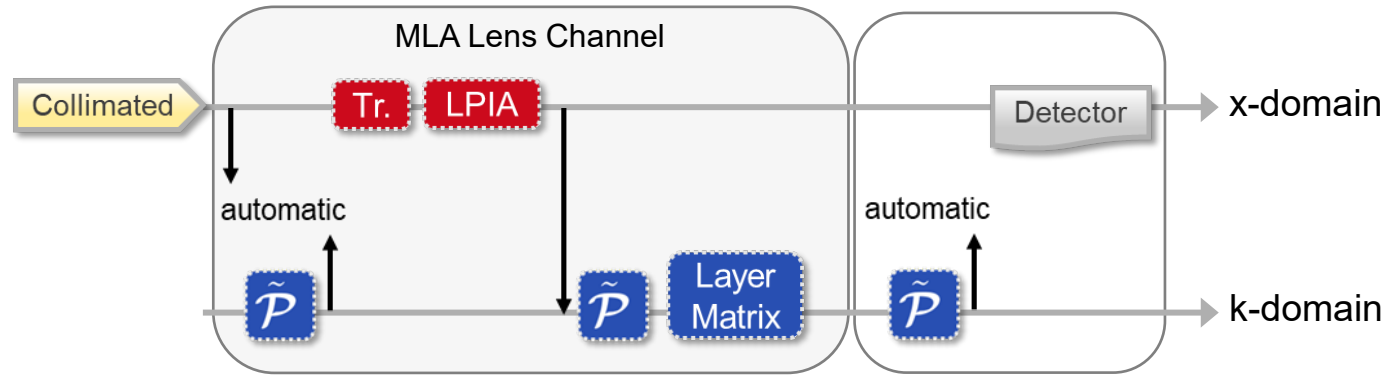
- Distance: 1 m
- Size: 700 mm x 700 mm



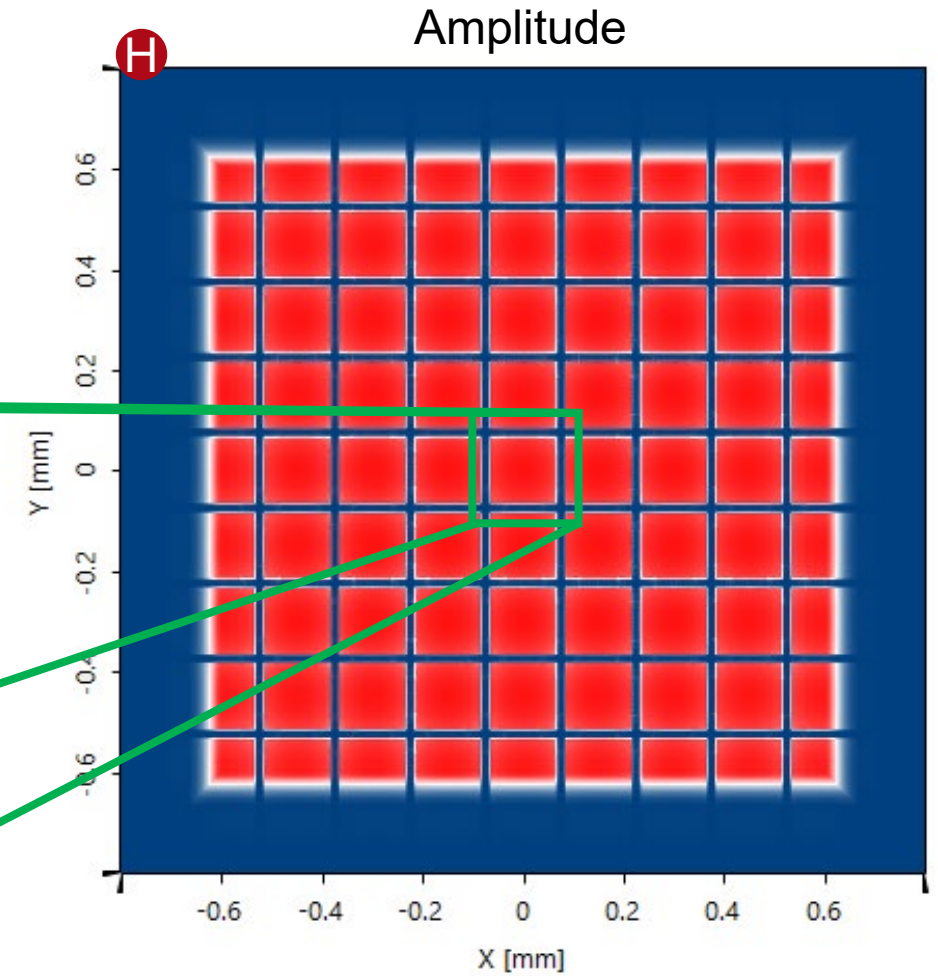
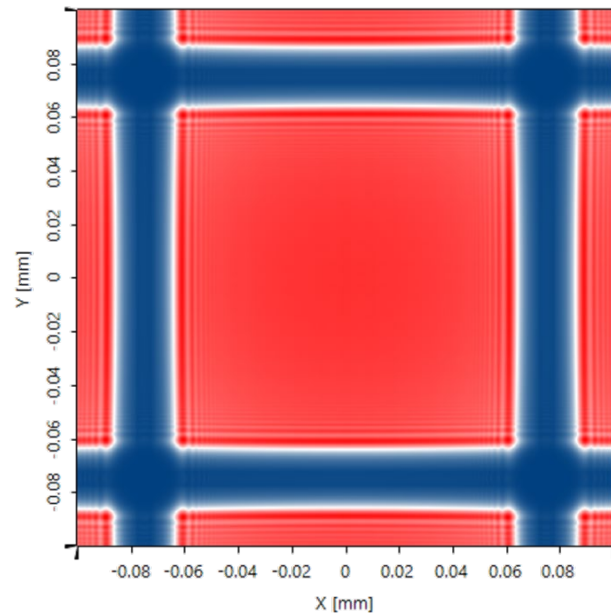
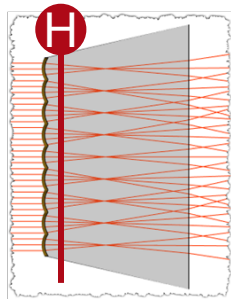
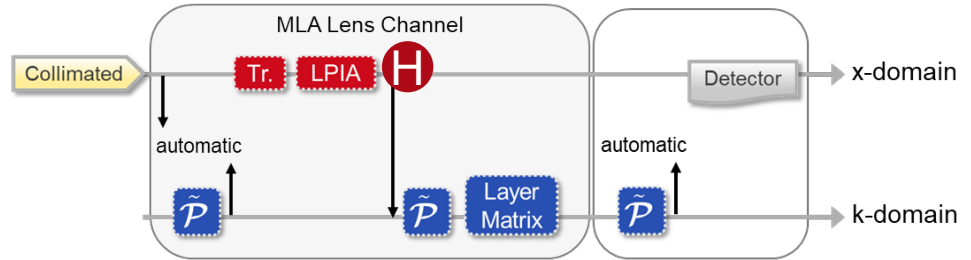
MLA Modeling by Lens Channels



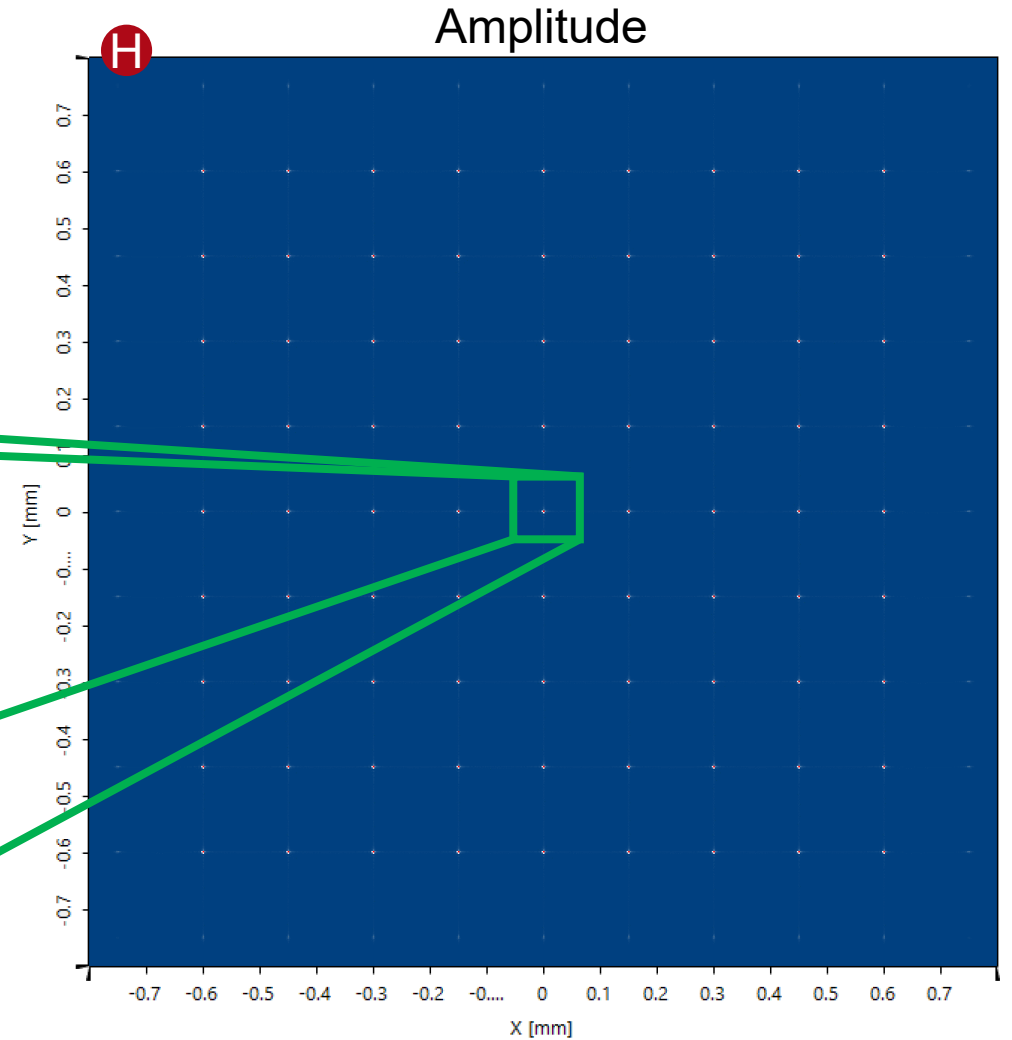
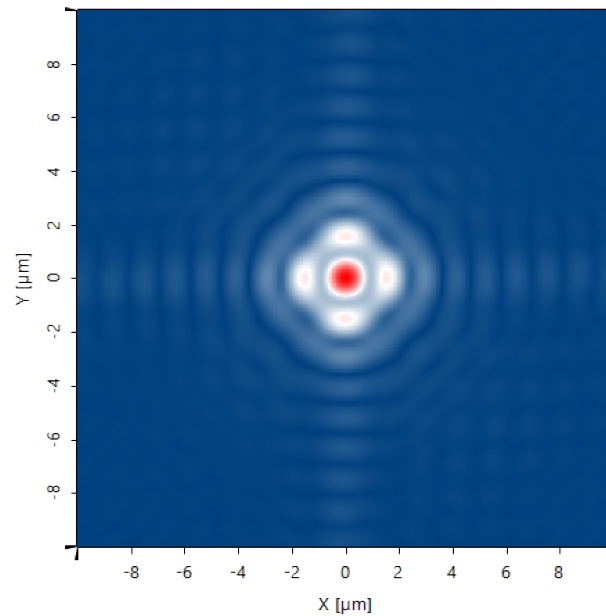
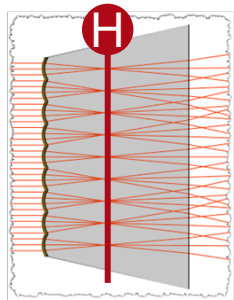
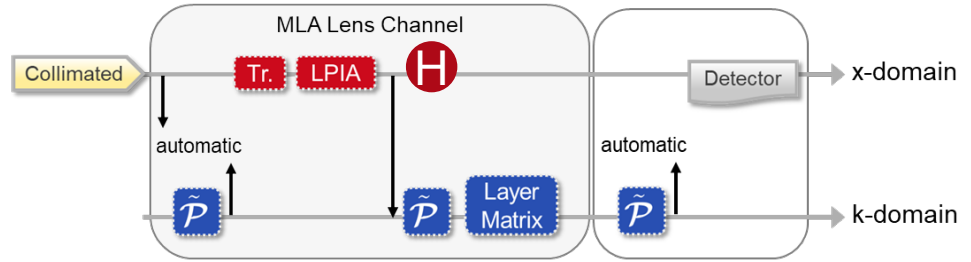
MLA Modeling by Lens Channels



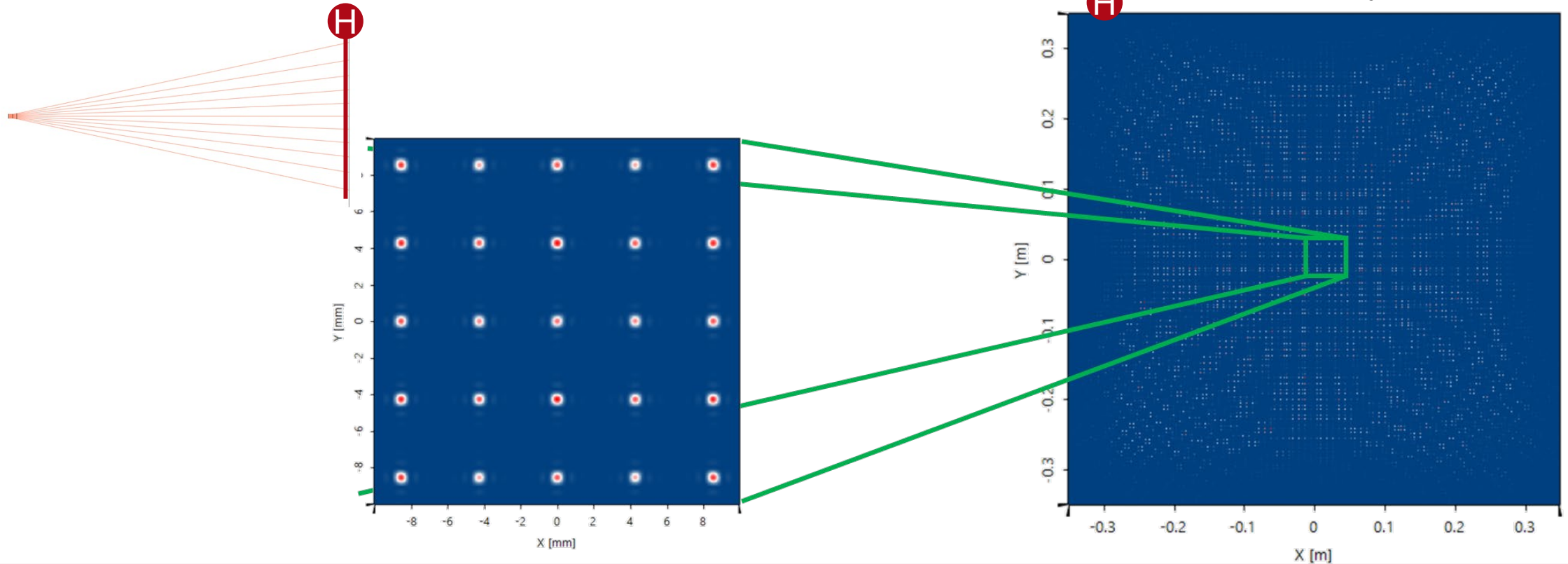
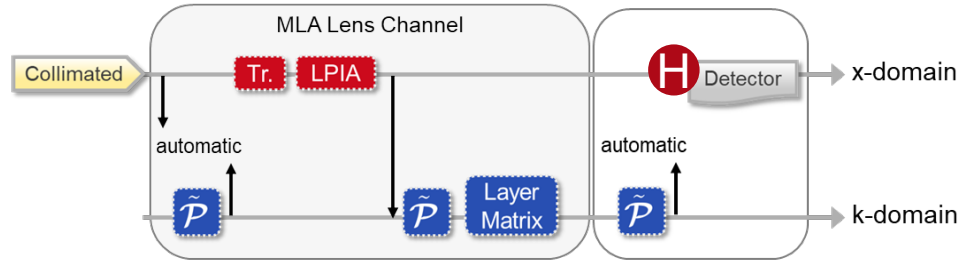
MLA Modeling: Near Field



MLA Modeling: Foci Plane



MLA Modeling: Far Field Intensity



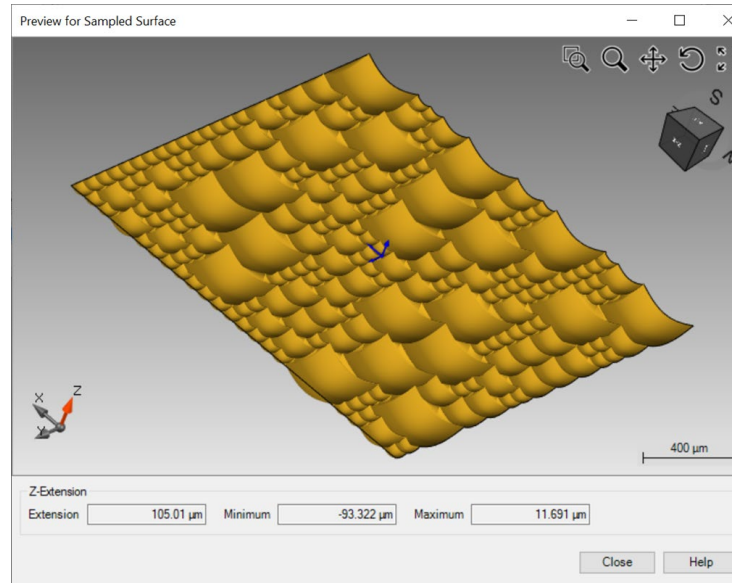
Scenario: Evaluate Far Field Intensity of Diffuser

Light Source:

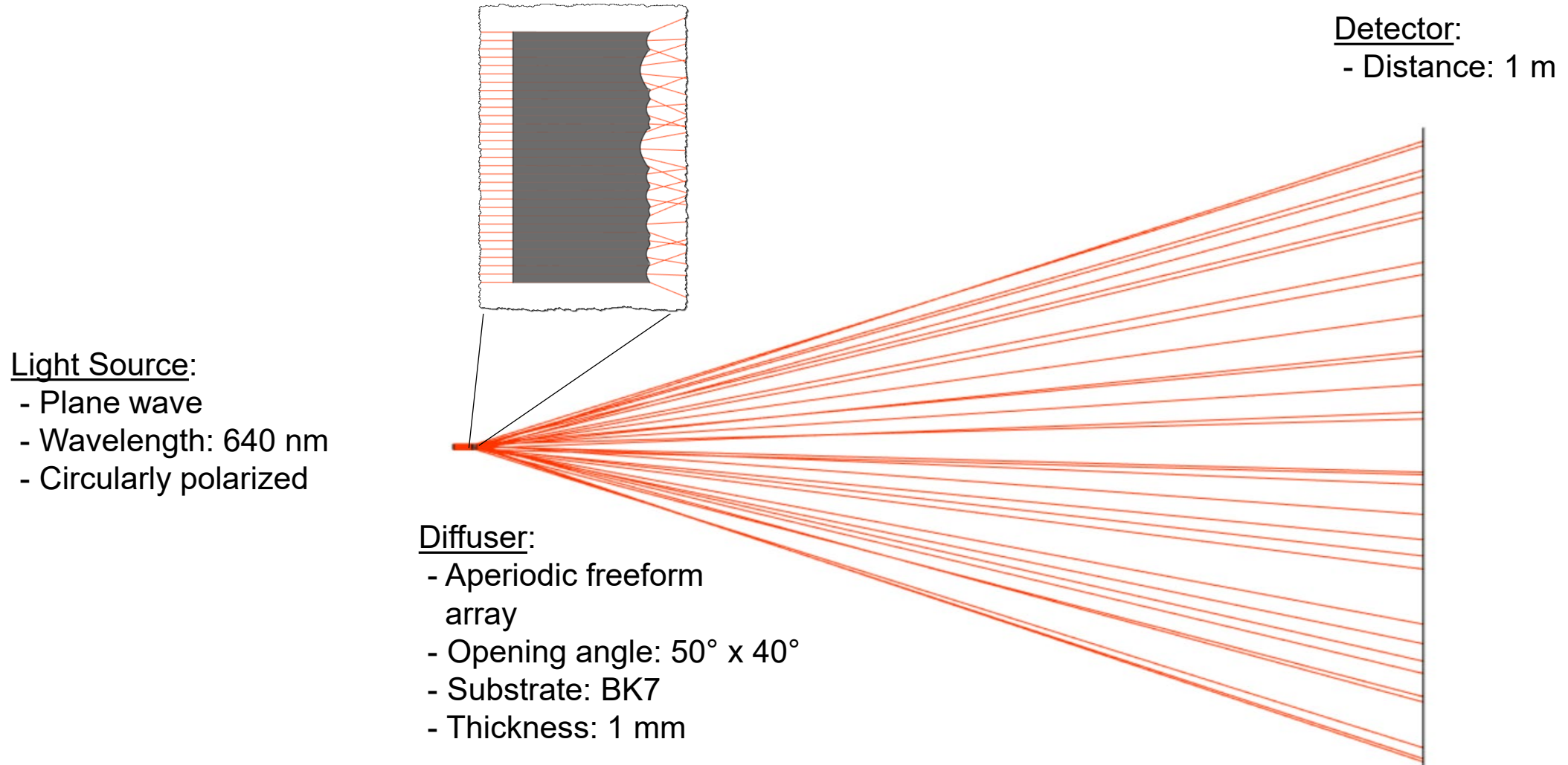
- Plane wave
- Wavelength: 640 nm
- Circularly polarized

Diffuser:

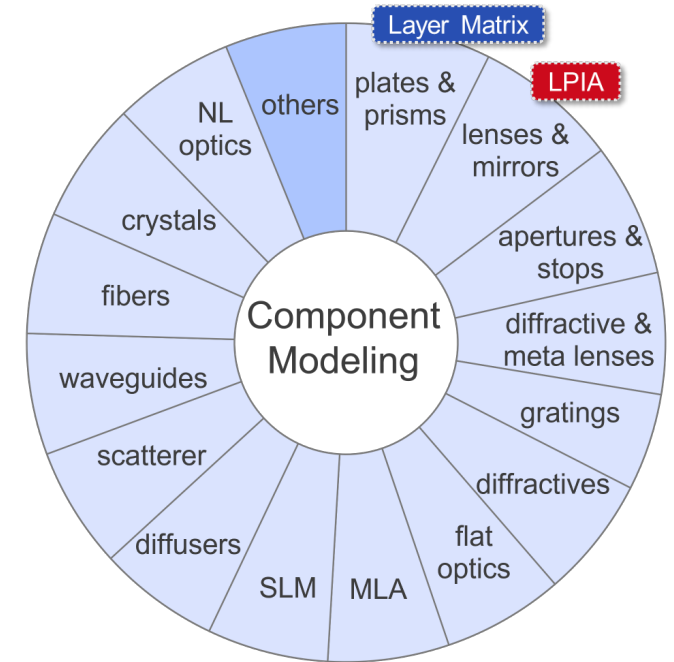
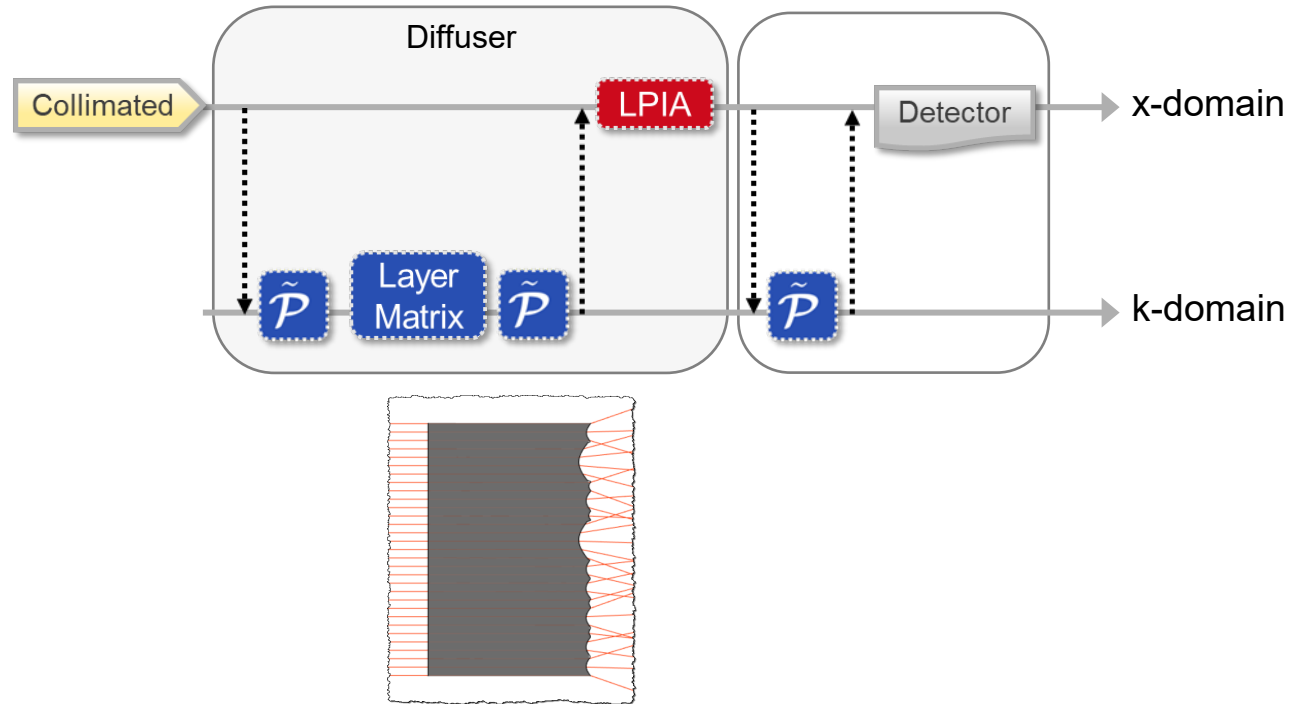
- Aperiodic freeform array
- Opening angle: $50^\circ \times 40^\circ$
- Substrate: BK7
- Thickness: 1 mm



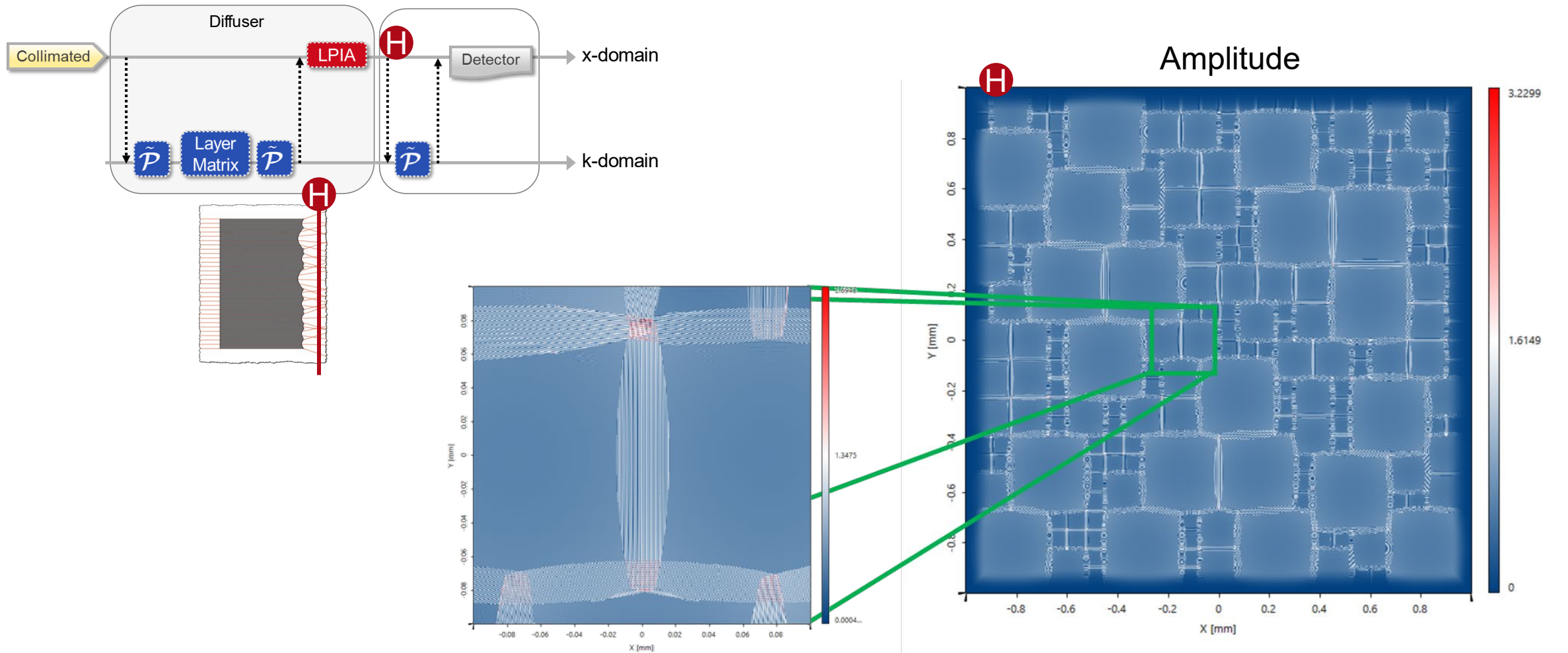
Scenario: Evaluate Far Field Irradiance of Diffuser



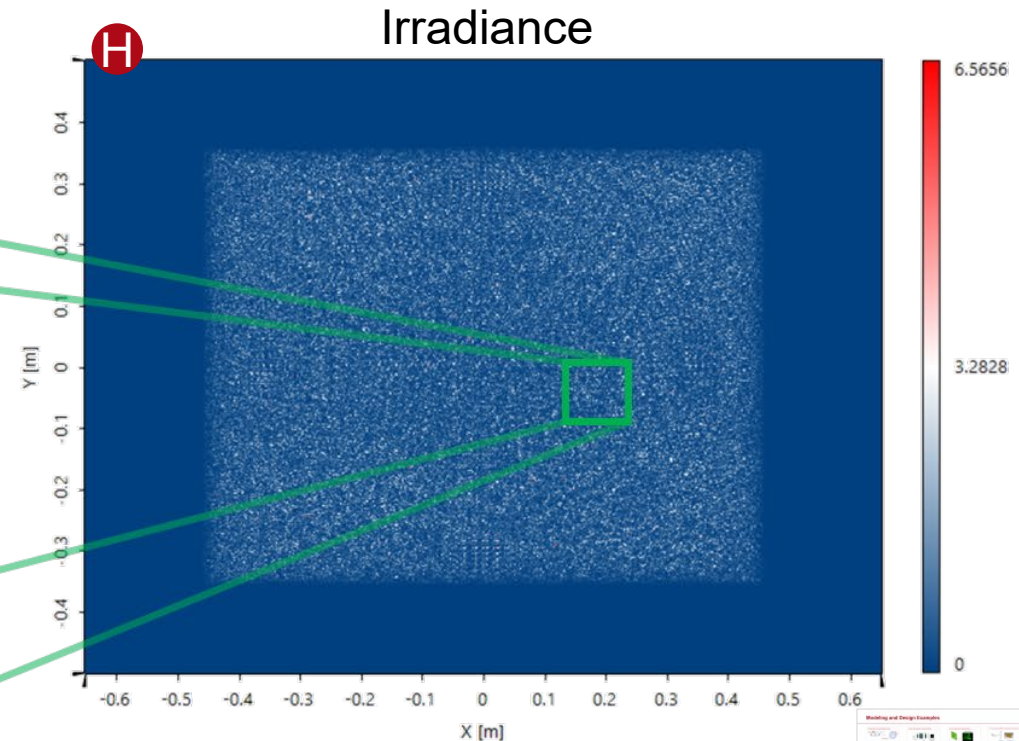
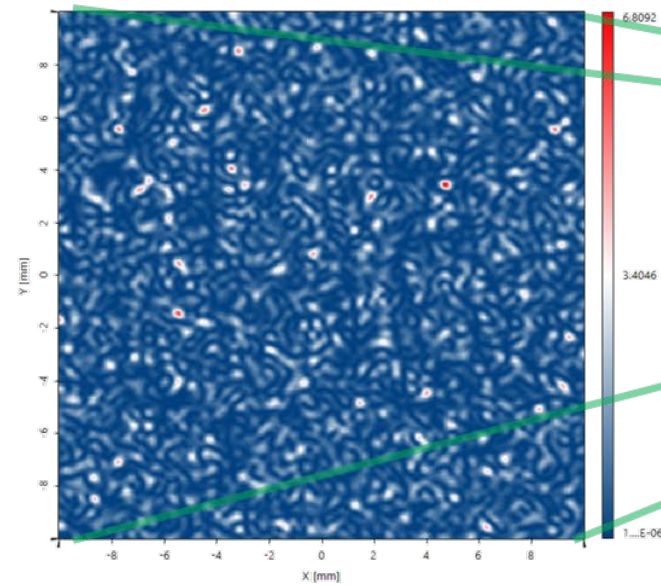
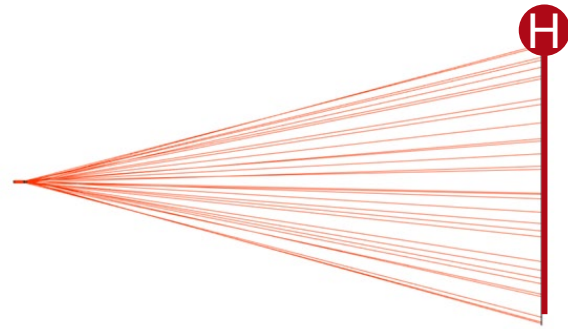
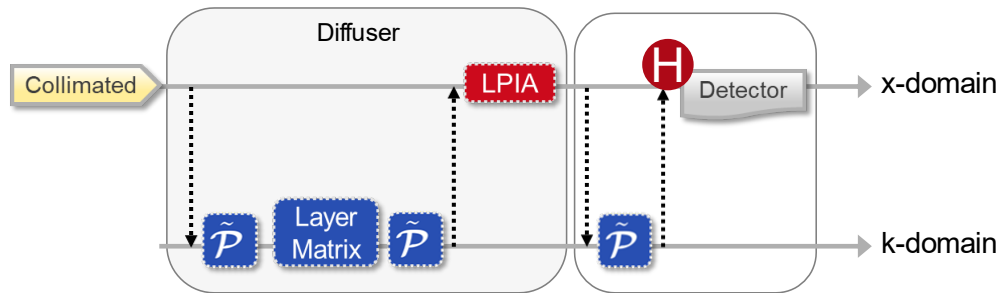
Pointwise Diffuser Modeling



Pointwise Diffuser Modeling: Near Field



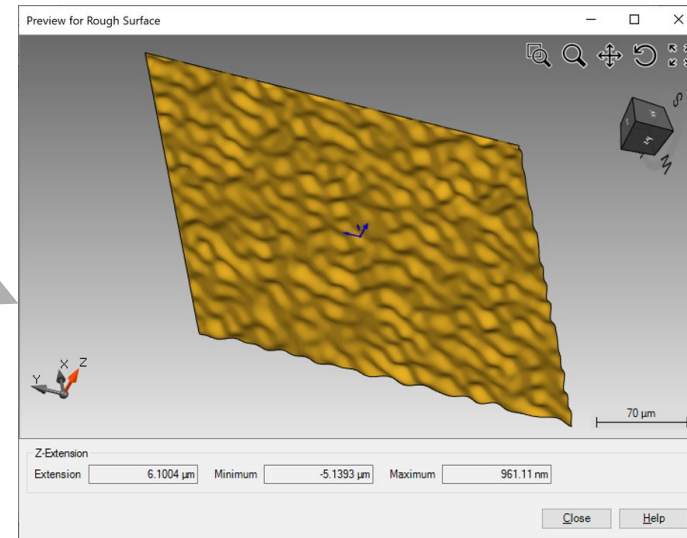
Pointwise Diffuser Modeling: Far Field Irradiance



Scenario: Calculation of BSDF and Far Field Irradiance of Rough Surface

Input field:

- Plane wave
- Wavelength: 640 nm
- Linearly polarized (Ex)

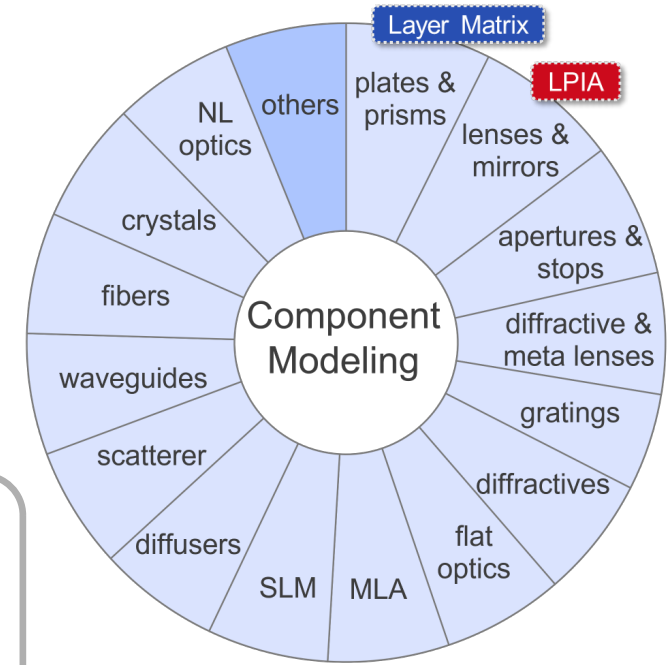
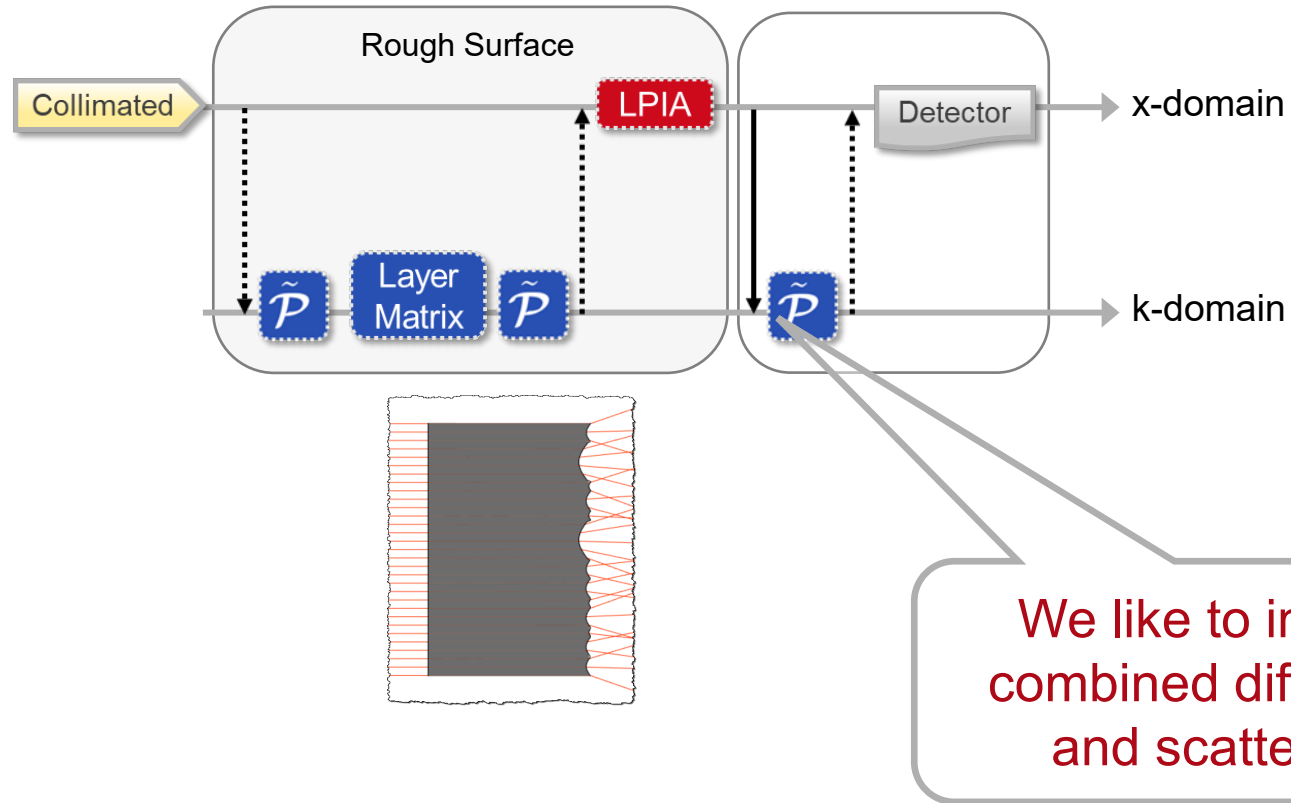


Rough Surface:

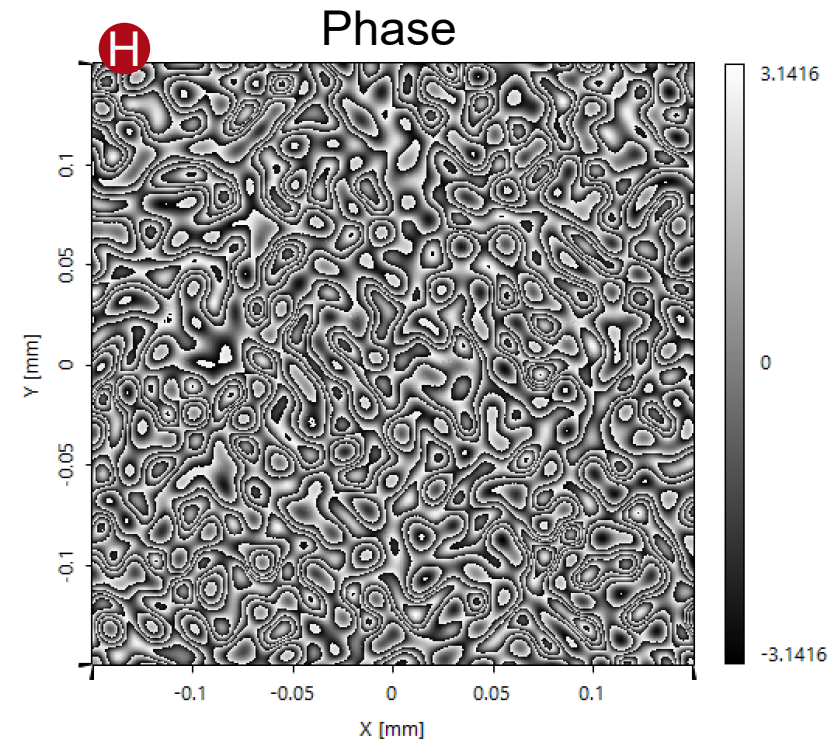
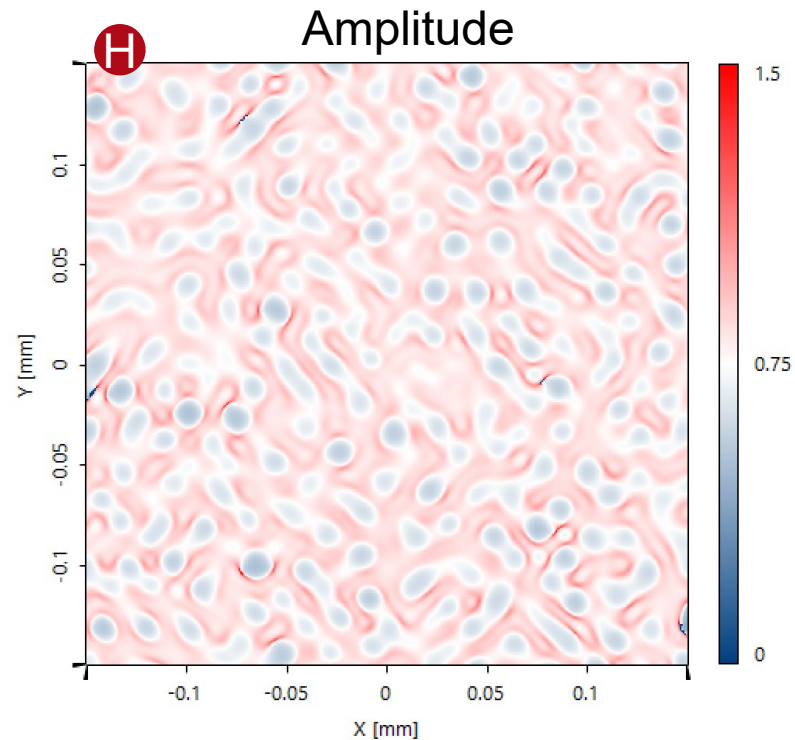
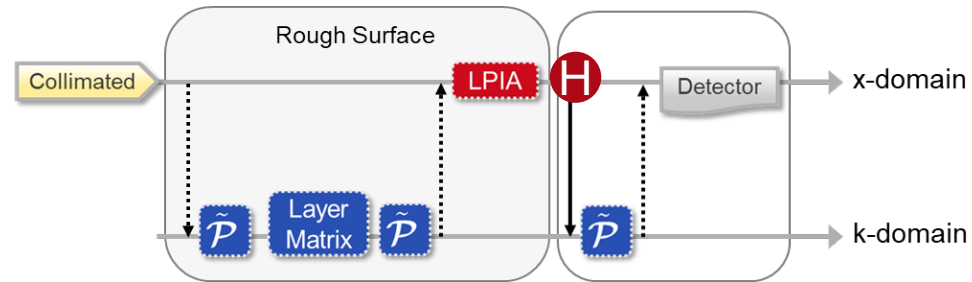
- Size: 320 μm x 320 μm
- Substrate: BK7

Thickness: 6.1 μm

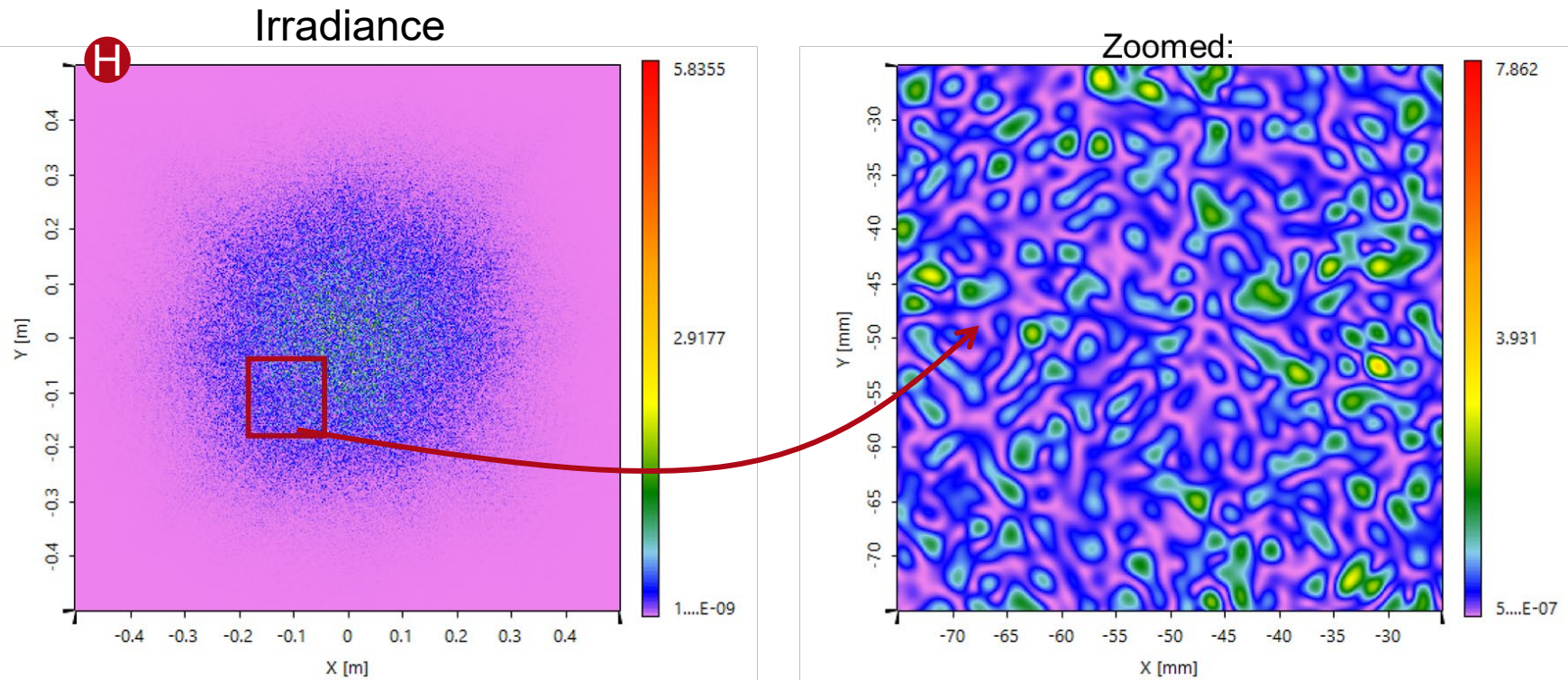
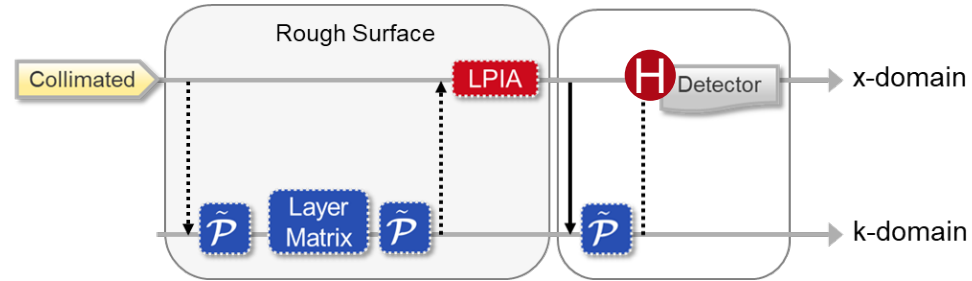
Non-Pointwise Rough Surface Modeling



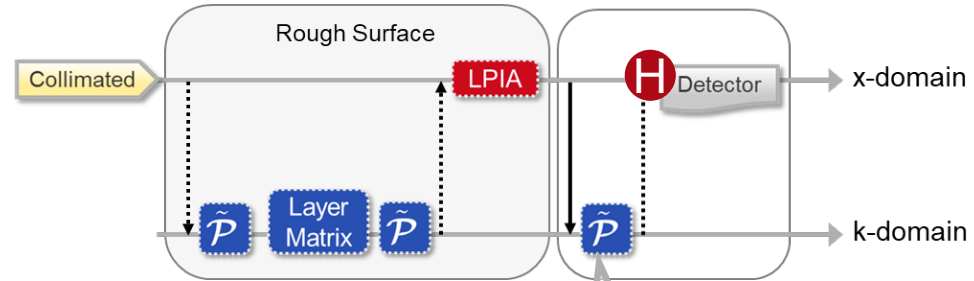
Rough Surface Modeling: Near Field



Rough Surface Modeling: Far Field



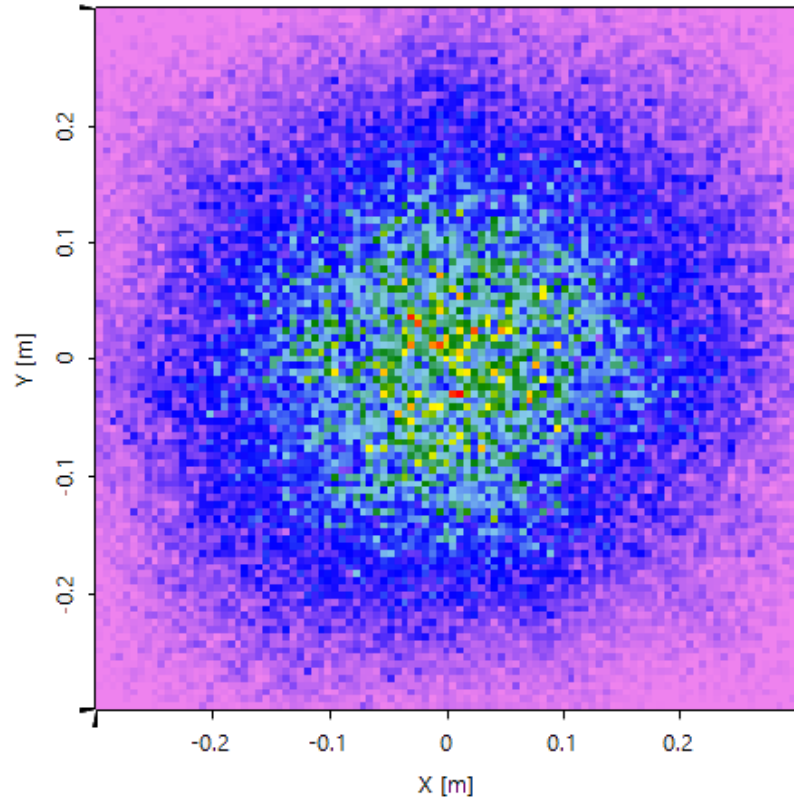
Rough Surface Modeling: Far Field



Modeling enables
determination of BSDF
of the rough surface!

Far Field Modeling: Monte Carlo vs. Physical Optics Modeling

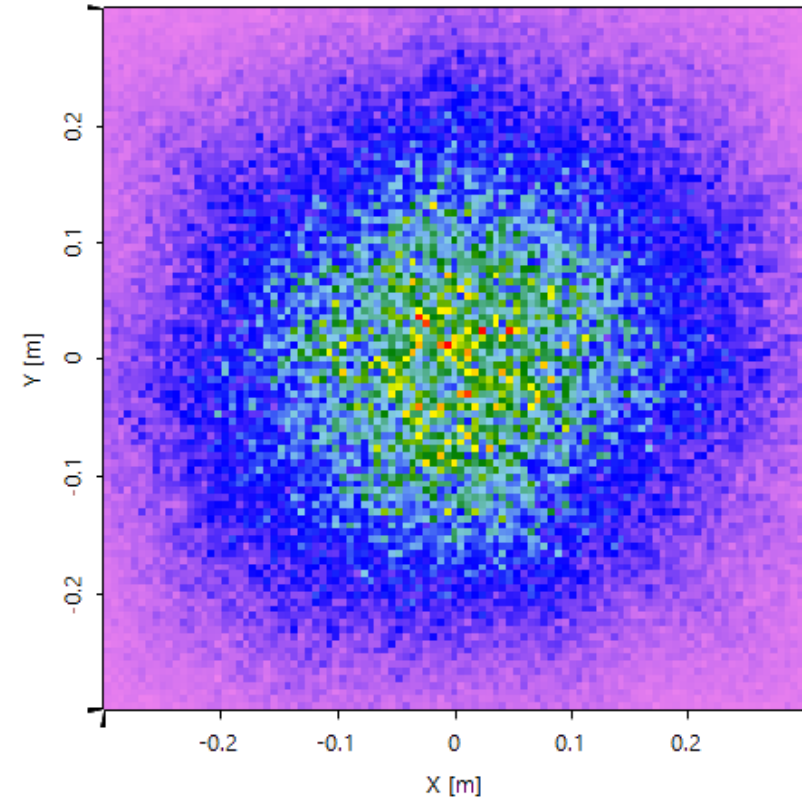
Detector resolution: **101 x 101**



Monte Carlo

Number samples: 437.000

Simulation time: **10 seconds**



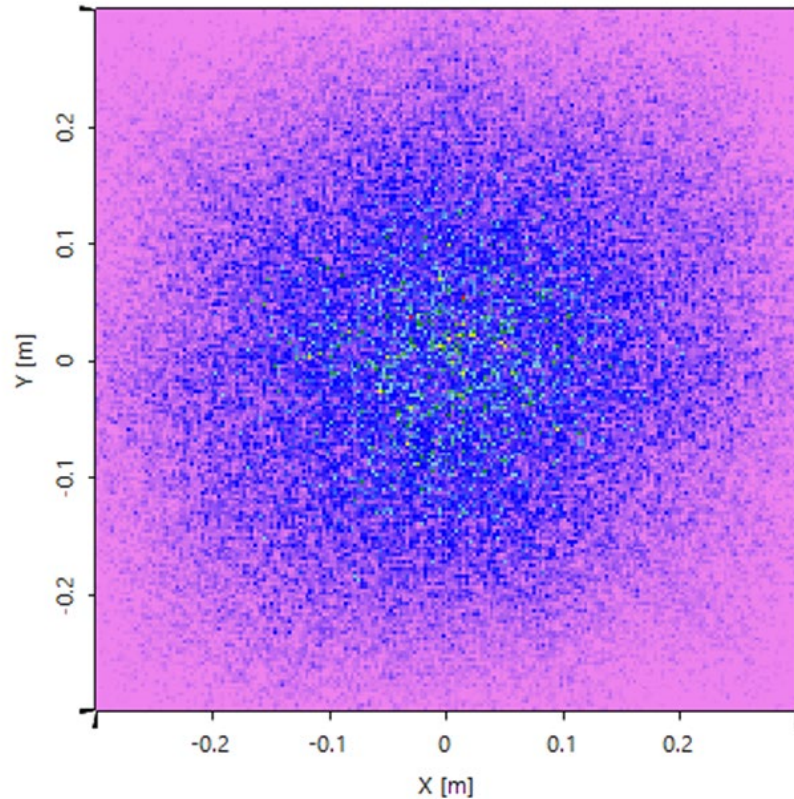
Physical Optics

Number samples: 27.000

Simulation time: **5 seconds**

Far Field Modeling: Monte Carlo vs. Physical Optics Modeling

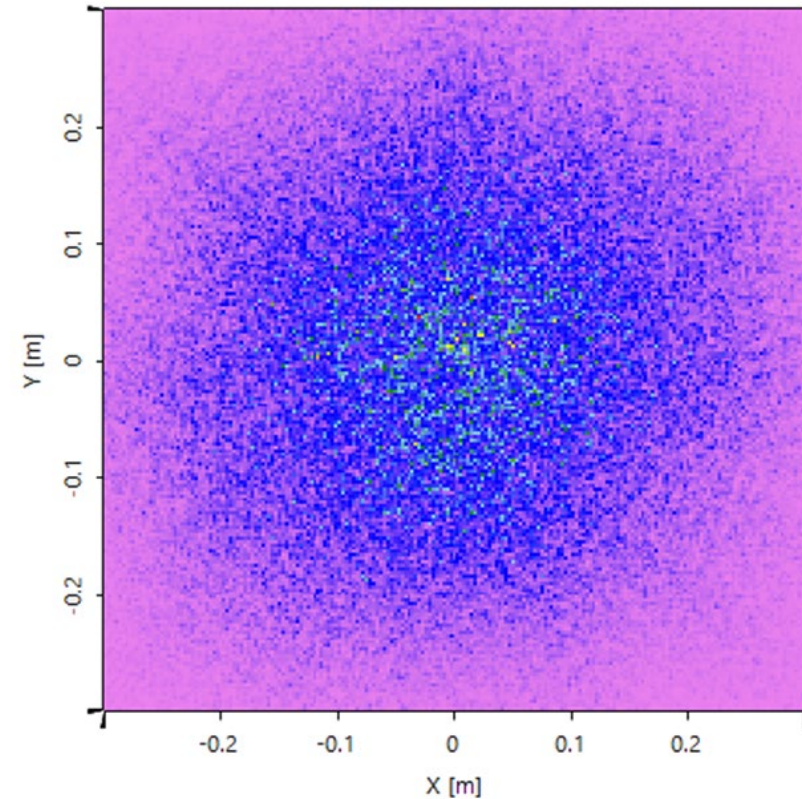
Detector resolution: **201 x 201**



Monte Carlo

Number samples: 1.334.000

Simulation time: **27 seconds**



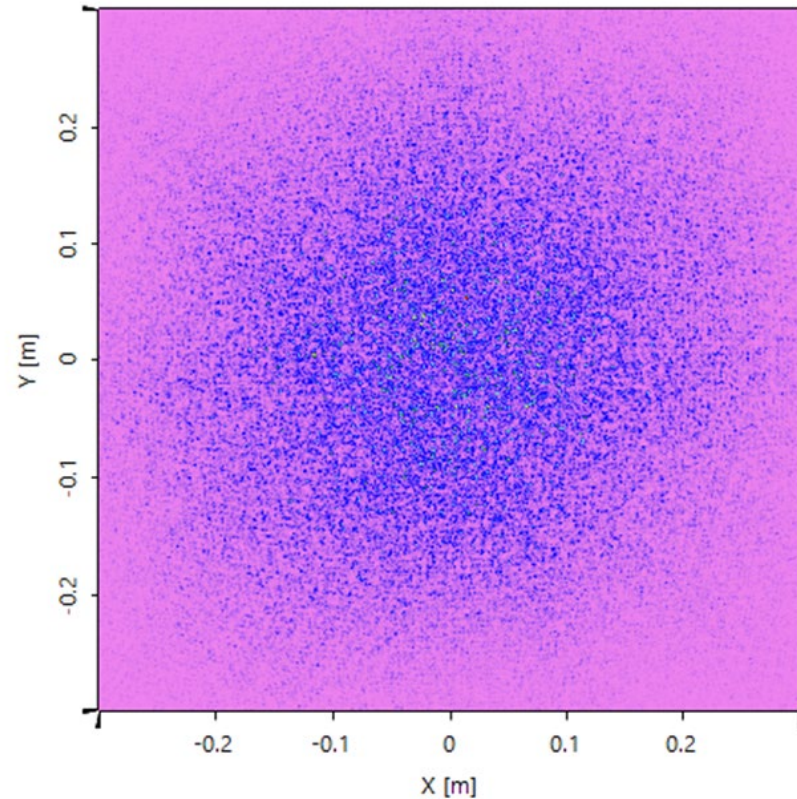
Physical Optics

Number samples: 27.000

Simulation time: **5 seconds**

Far Field Modeling: Monte Carlo vs. Physical Optics Modeling

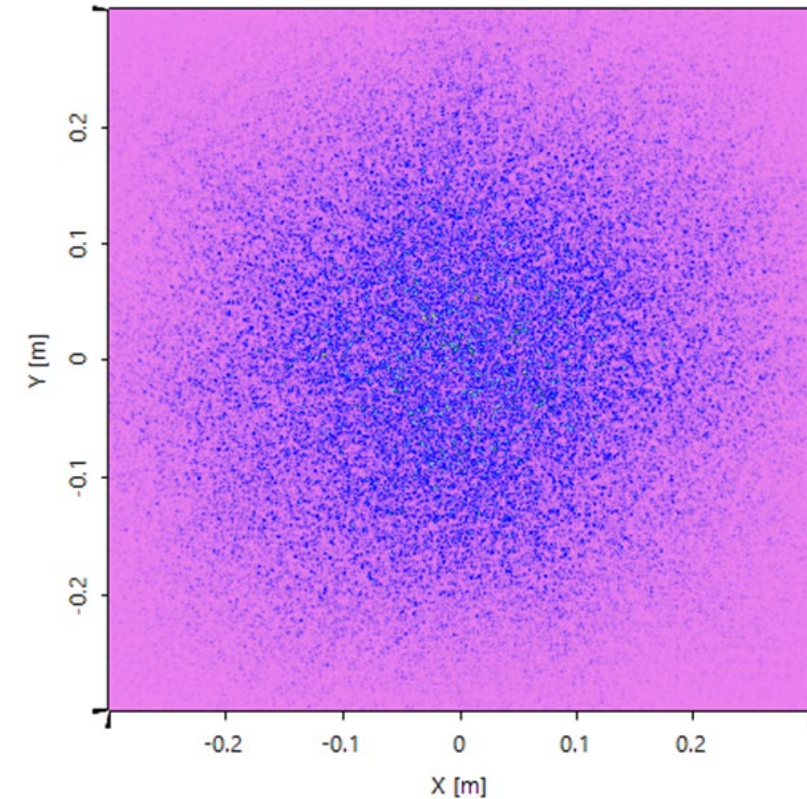
Detector resolution: **401 x 401**



Monte Carlo

Number samples: 3.924.000

Simulation time: **77 seconds**



Physical Optics

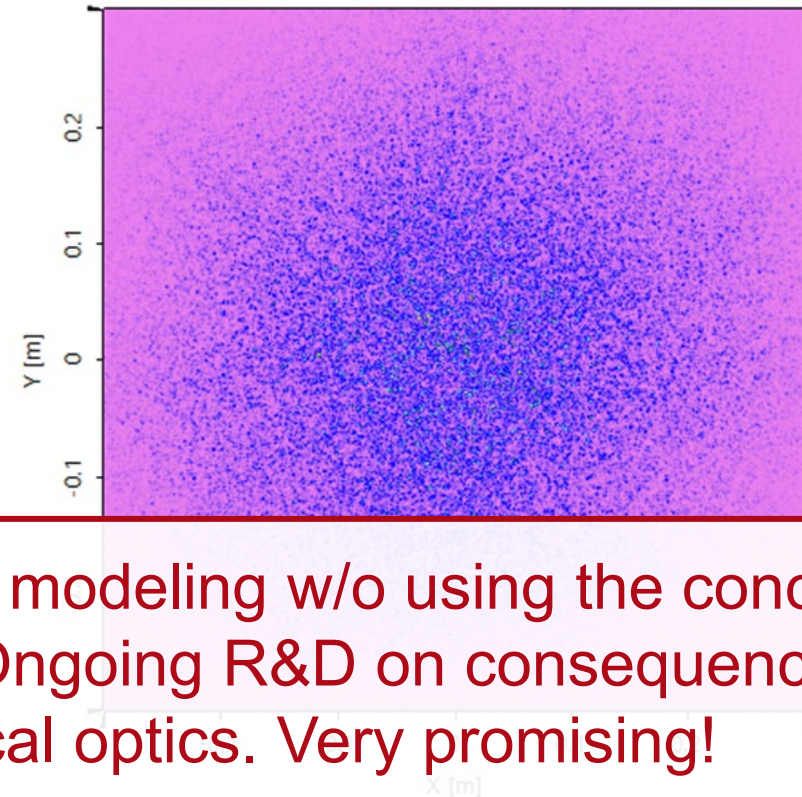
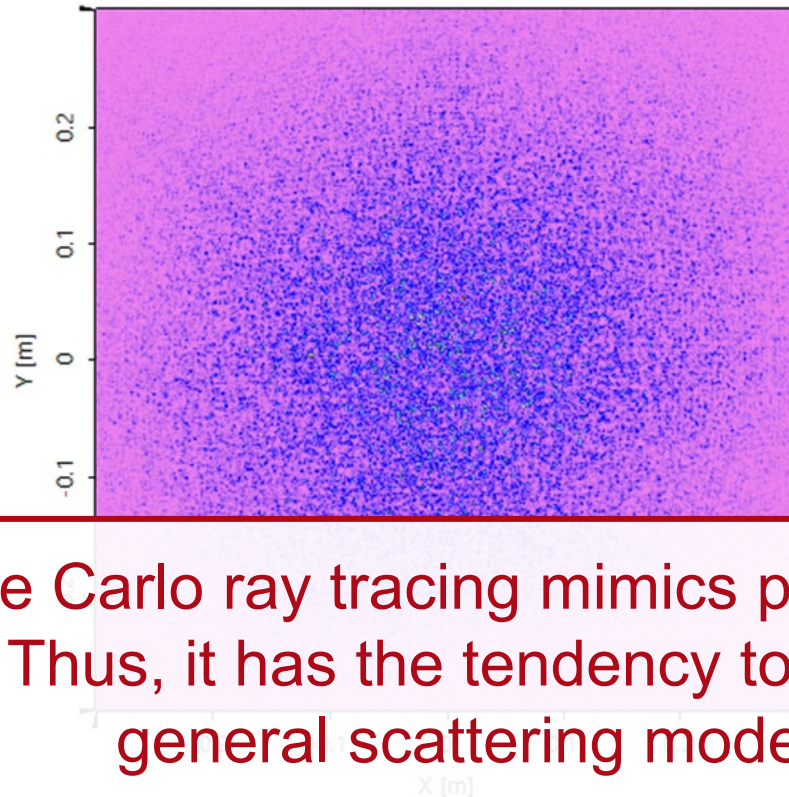
Number samples: 27.000

Simulation time: **5 seconds**



Far Field Modeling: Monte Carlo vs. Physical Optics Modeling

Detector resolution: **401 x 401**



Monte Carlo ray tracing mimics physical optics modeling w/o using the concept of FFT. Thus, it has the tendency to be not fast. Ongoing R&D on consequences for general scattering modeling by physical optics. Very promising!

Monte Carlo

Number samples: 3.924.000

Simulation time: 77 seconds

Physical Optics

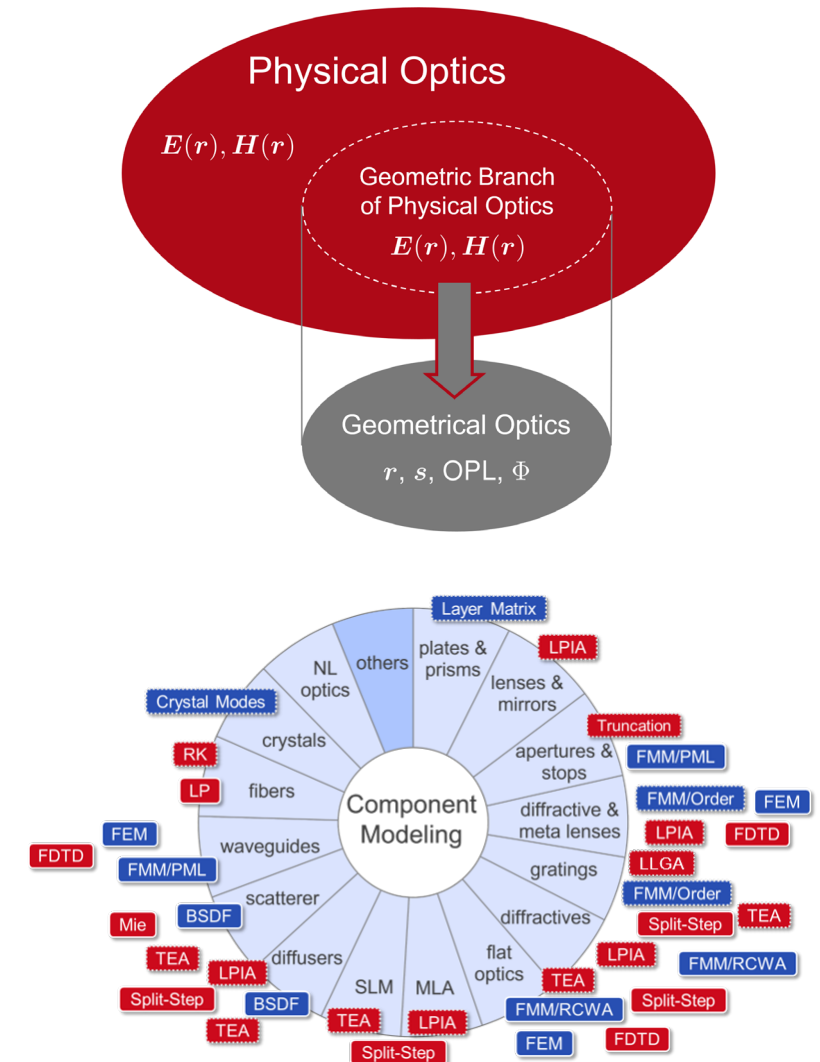
Number samples: 27.000

Simulation time: 5 seconds



Conclusions for Next Generation Software

- **Pointwise physical optics** modeling is included.
- Provide an open platform for connecting many physical optics modeling techniques: **connecting solvers – rigorous and approximated ones.**
- **Ray optics** is easily accessible **special mode of operation of physical optics.**
- CAD components and solvers are combined.
- Modeling of sources, components, and detectors can be customized to **unleash the flexibility and power of physical optics modeling.**
- Parametric optimization should be accompanied by inverse and other design approaches.



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