

Webinar LightTrans International, 13.01.2021

# Diffractive Lenses: Concept, Modeling, Design, and Fabrication Data

Frank Wyrowski and Christian Hellmann



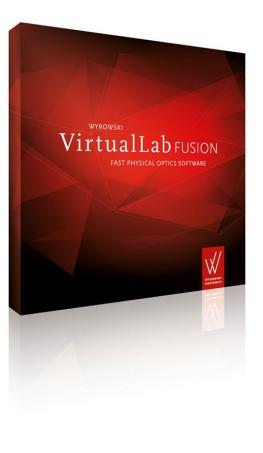
Webinar LightTrans International, 13.01.2021

# **Freeform and Flat Optics**

Frank Wyrowski and Christian Hellmann

#### **Fast Physical Optics Software VirtualLab Fusion**



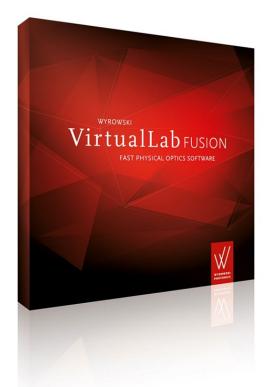


# **Connecting Field Solvers**

**Fast** physical optics modeling and design in VirtualLab Fusion by:

- Connecting specialized field solvers in different regions of the system.
- VirtualLab Fusion is platform for in-built and customized solvers.
- Often as fast as ray tracing and can be even faster than Monte Carlo ray tracing.

Fast physical optics with VirtualLab Fusion provides new insights and innovative solutions in optical modeling and design.



Typical speed of all modeling and design tasks in talk: a few seconds to < 1 min

# **Fast Physical Optics Software VirtualLab Fusion**



#### **Current developments in:**

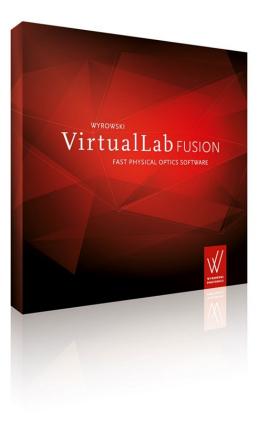
- Flat optics including coatings, gratings, DOEs, diffusers, holograms, metasurfaces, component arrays
- Lenses and freeform optics
- Imaging & beam transformation
- Light shaping & non-imaging optics
- Microscopy and focusing
- Optical metrology and sensors
- Femtosecond pulse systems
- Fiber optics
- Lidar
- Light guides for AR/MR
- Scattering and BSDF

# **Content of Webinar**

The webinar provides insights regarding

- Our R&D and product developments in
  - Physical-optics design
  - Flat and freeform optics
- Related software tools in VirtualLab Fusion
  - Current version
  - Outlook 2021: new techniques and tools

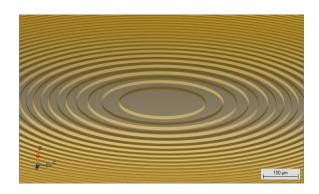
All examples in webinar are done with the in-house version of VirtualLab Fusion!



# **Structure of Webinar**

- Why physical optics in design?
- Optical design in physical optics terms
- Diffractive Optical Elements (DOE)
  - Design
  - Modeling
  - Fabrication data
- Design examples





# **Importance of Physical Optics**

- Optical lens design is dominated by ray optics and specific well-established workflows.
- The inclusion of freeform surfaces has led to some new challenges like broken symmetries and large number of free parameters.
- The inclusion of flat lenses requires a seamless combination with physical-optics modeling.
- We suggest to go a step further: physical optics may give a fresh view and new ideas to optical design beyond conventional routines.



1831 – 1879

```
\nabla \times \boldsymbol{E}(\boldsymbol{r}, \omega) = i\omega\mu_0 \boldsymbol{H}(\boldsymbol{r}, \omega)\nabla \times \boldsymbol{H}(\boldsymbol{r}, \omega) = -i\omega\epsilon_0 \check{\epsilon}_r(\boldsymbol{r}, \omega) \boldsymbol{E}(\boldsymbol{r}, \omega)\nabla \cdot \left(\check{\epsilon}_r(\boldsymbol{r}, \omega) \boldsymbol{E}(\boldsymbol{r}, \omega)\right) = 0\nabla \cdot \boldsymbol{H}(\boldsymbol{r}, \omega) = 0
```

# **Importance of Physical Optics**

- Physical optics may give a fresh view and new ideas to optical design beyond conventional routines:
- Algorithms to design freeform surfaces beyond parametric optimization.
- Systematic inclusion of flat optics components including all desired and detrimental effects.
- Evaluation of the potential and limitations of flat optics.



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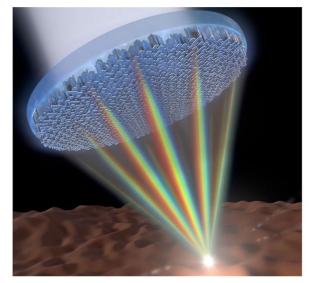
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"Is it possible to replace a bulky glass system by one metalens (flat lens)"?

# 'Metalens' breakthrough may bring a revolution in camera design

Physicists say wafer-thin device can do the job of today's bulky glass lenses.

Jan. 3, 2018, 7:13 PM CET / Updated Jan. 3, 2018, 7:13 PM CE By Rafi Letzter, Live Science January 2018

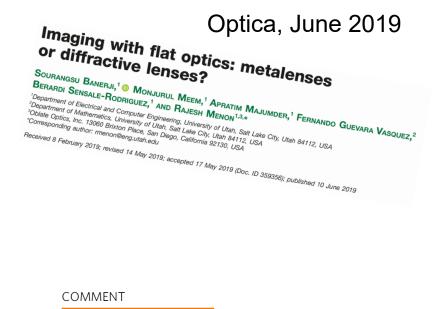


------ This flat metalens can focus nearly the entire visible spectrum of light in the same spot and in high resolution. Jared Sisler / Harvard SEAS

https://www.nbcnews.com/mach/science/

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"Is it possible to replace a bulky glass system by one metalens (flat lens)" ?



https://doi.org/10.1038/s41467-020-15972-9 OPEN

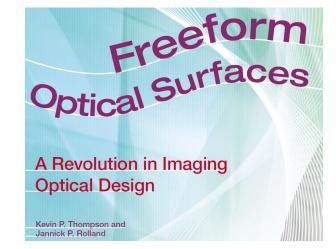
The advantages of metalenses over diffractive lenses

Jacob Engelberg ₀ <sup>1</sup> & Uriel Levy ₀ <sup>1⊠</sup>

Nature Communication, April 2020

- Physical optics may give a fresh view and new ideas to optical design beyond conventional routines:
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OPN Optics & Photonics News, June 2012 June 2012

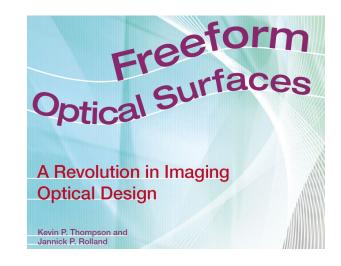
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Strategies and modern tools to investigate and exploit the potential of freeform and flat optics by physical optics. 'Metalens' breakthrough may bring a revolution in camera design

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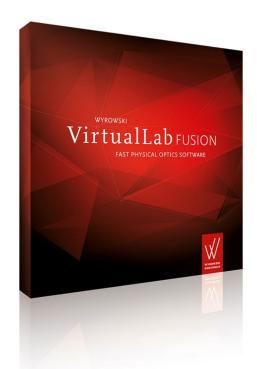
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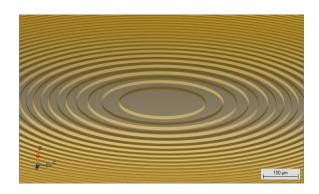


#### VirtualLab Fusion 2021

# **Structure of Webinar**

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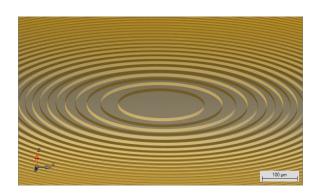




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- Why physical optics in design?
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# **Light Representation in Physical Optics**

- In physical optics light is described by vectorial electromagnetic fields.
- The electric field is denoted by the three components

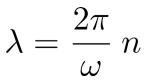
$$oldsymbol{E}(oldsymbol{r},\omega) = egin{pmatrix} E_x(oldsymbol{r},\omega)\ E_y(oldsymbol{r},\omega)\ E_z(oldsymbol{r},\omega) \end{pmatrix} \,.$$

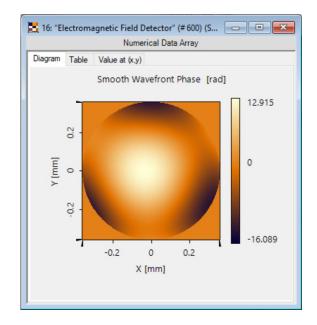
- The components typically possess a common wavefront phase  $\psi({\pmb r},\omega)$  and we write

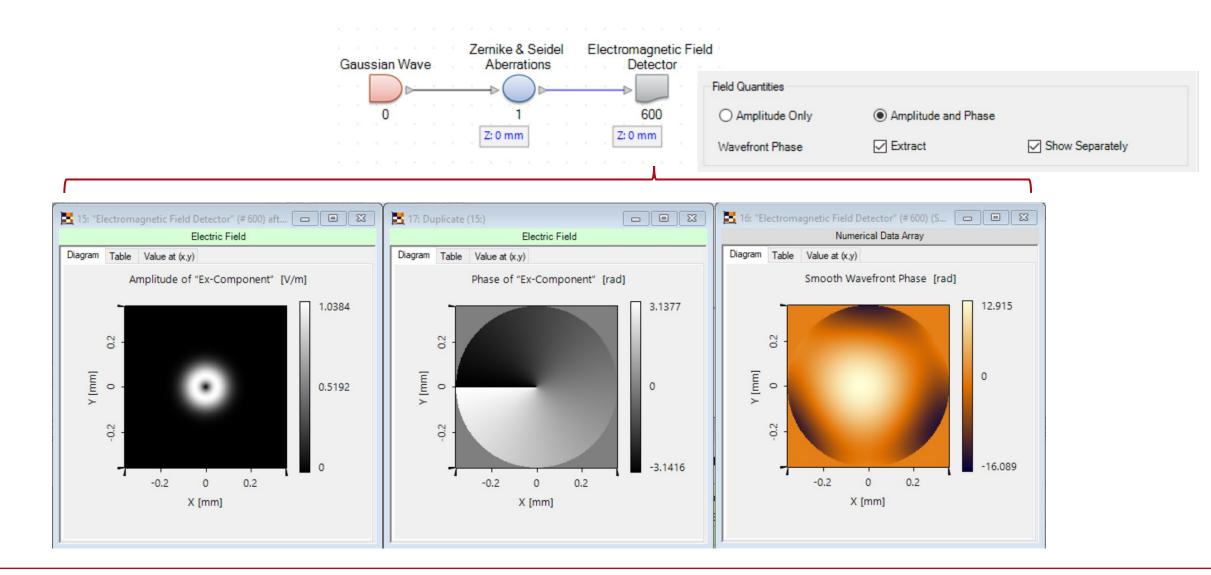
$$oldsymbol{E}(oldsymbol{r},\omega) = oldsymbol{U}(oldsymbol{r},\omega) \exp\left(\mathrm{i}\psi(oldsymbol{r},\omega)
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ight),$$

with  $(\ell = x, y, z)$ 

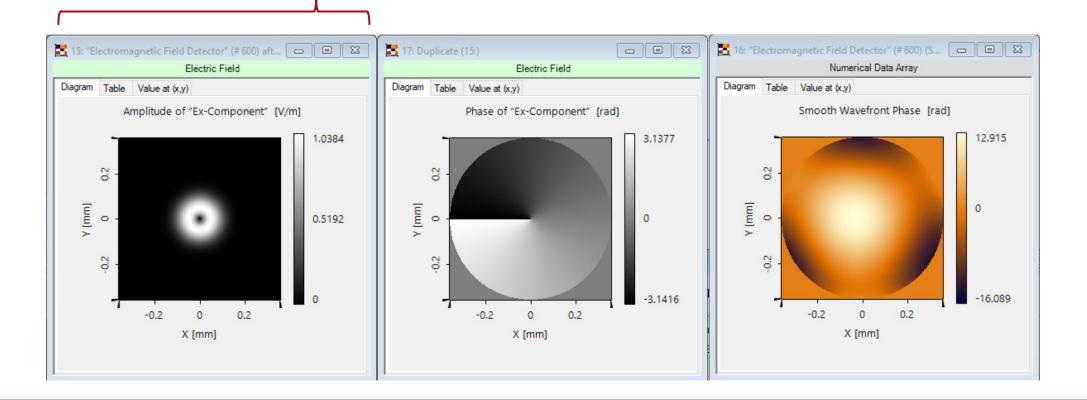
$$\psi(\boldsymbol{r},\omega) = \arg \left( E_{\ell}(\boldsymbol{r},\omega) \right) - \arg \left( U_{\ell}(\boldsymbol{r},\omega) \right).$$



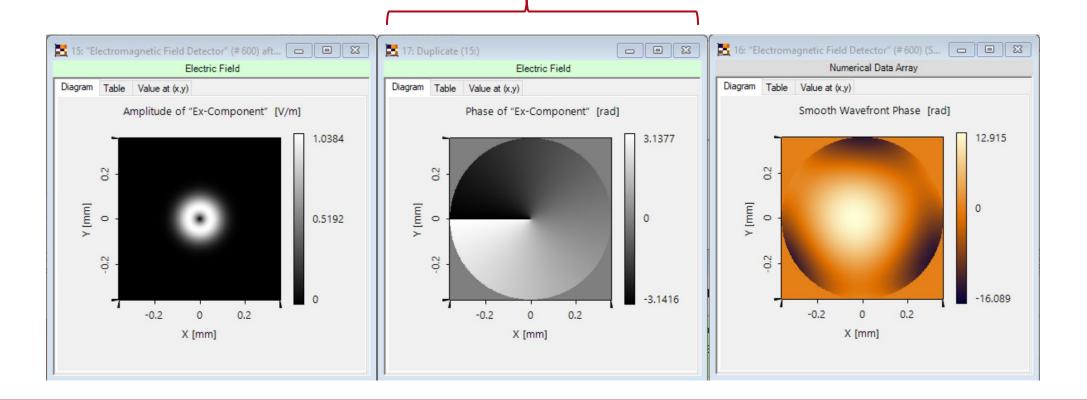




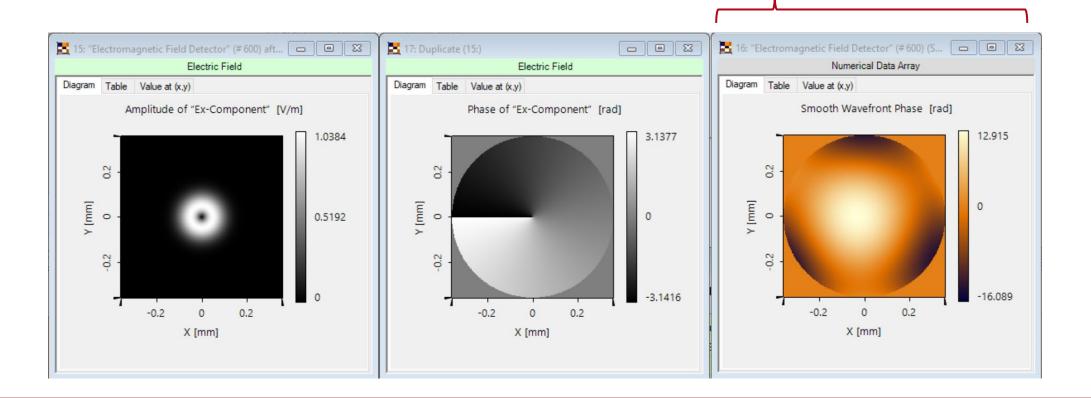
 $E_x(\boldsymbol{\rho}) = |U_x(\boldsymbol{\rho})| \exp\left(\mathrm{i} \arg(U_x)(\boldsymbol{\rho})\right) \exp\left(\mathrm{i} \psi(\boldsymbol{r},\omega)\right)$ 



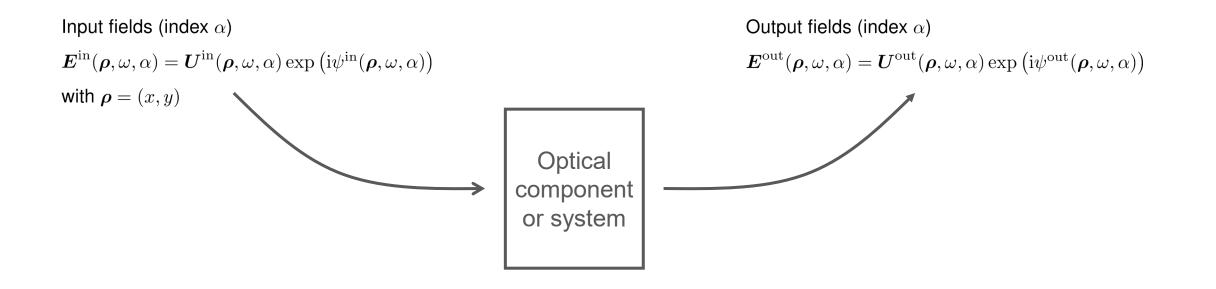
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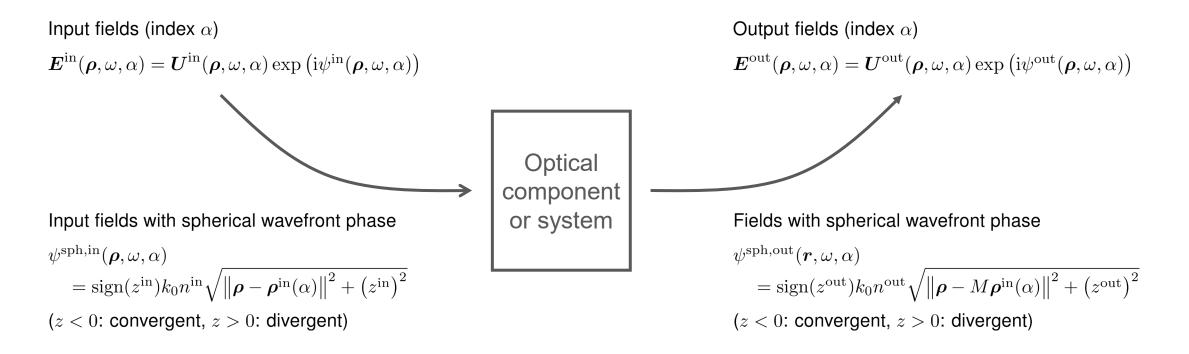
### **Design Scenarios: Field Transformation**



#### Scenarios:

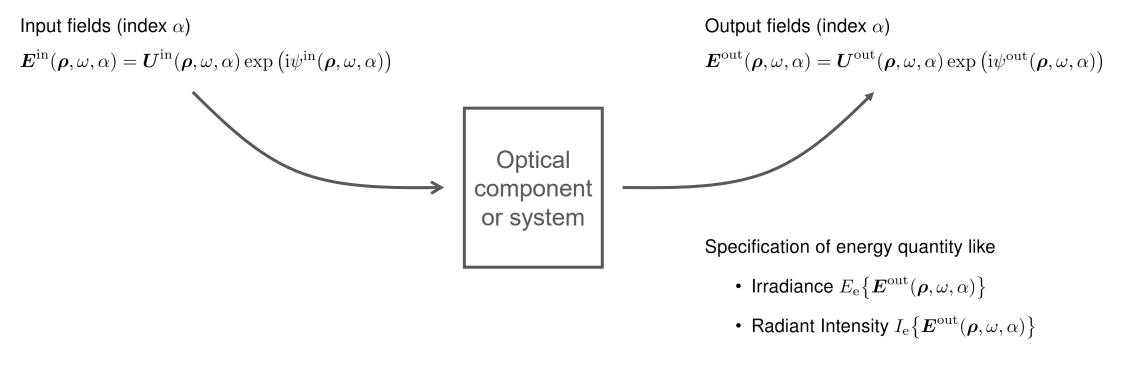
Single-field design One input and output field only ( $\alpha = 1$ ; skipped) Multi-field design Set of input and output fields ( $\alpha \in \mathbb{N}$ ) Monochromatic or polychromatic design

# **Design Scenarios: Imaging**



#### Scenario:

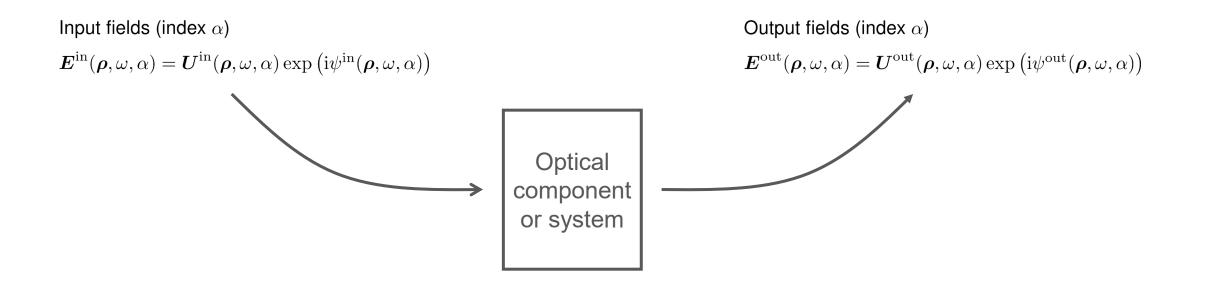
Multi-field design FOV: Set of input and output fields ( $\alpha \in \mathbb{N}$ ) Monochromatic or polychromatic design



#### Scenarios:

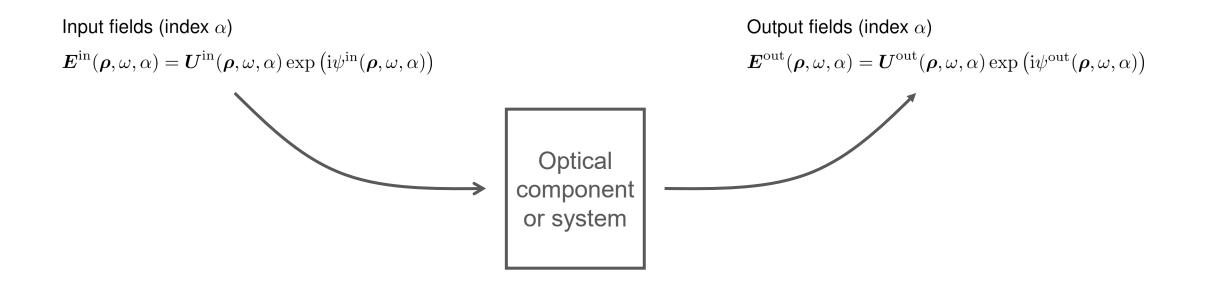
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# **Manipulation of Input Fields by System**



How to achieve the specified transformations with sufficient accuracy?

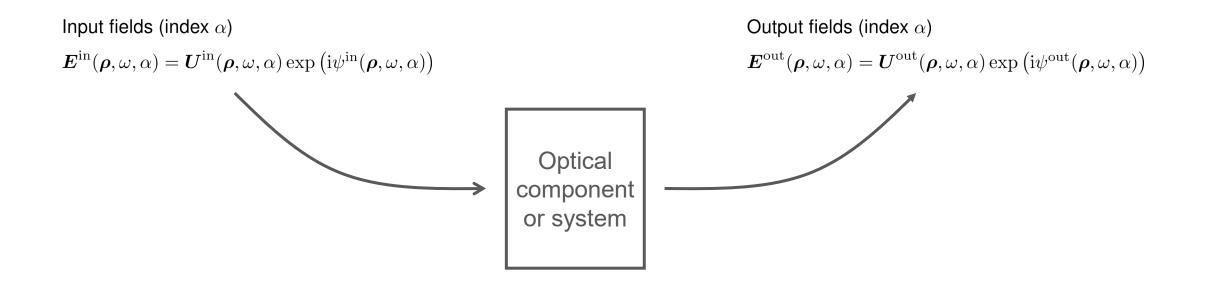
### **Manipulation of Input Fields by System**



Major manipulations of fields on their way through system:

- Wavefront phase control:  $\psi^{in} \to \ldots \psi_j \ldots \to \psi^{out}$
- Irradiance shaping:  $E_{e}^{in} \rightarrow \ldots E_{e,j} \ldots \rightarrow E_{e}^{out}$

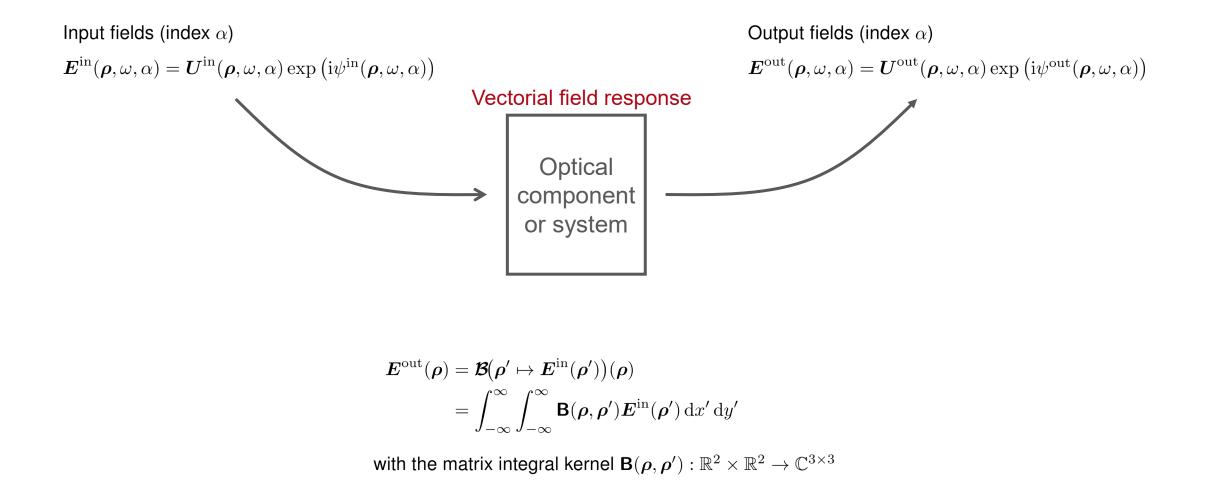
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### **Field Response Operator: Integral**



Input fields (index  $\alpha$ ) Output fields (index  $\alpha$ )  $\boldsymbol{E}^{\text{in}}(\boldsymbol{\rho},\omega,\alpha) = \boldsymbol{U}^{\text{in}}(\boldsymbol{\rho},\omega,\alpha) \exp\left(\mathrm{i}\psi^{\text{in}}(\boldsymbol{\rho},\omega,\alpha)\right)$  $\boldsymbol{E}^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha) = \boldsymbol{U}^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha) \exp\left(\mathrm{i}\psi^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha)\right)$ Vectorial field response  $oldsymbol{E}^{ ext{out}}(oldsymbol{
ho})$  $E^{\mathrm{in}}(
ho')$  $E^{\mathrm{out}}(oldsymbol{
ho}) = \mathcal{B}(oldsymbol{
ho}' \mapsto E^{\mathrm{in}}(oldsymbol{
ho}'))(oldsymbol{
ho})$  $= \int \int_{\mathbf{V}in} \mathbf{B}(\boldsymbol{\rho}, \boldsymbol{\rho}') \boldsymbol{E}^{in}(\boldsymbol{\rho}') \, \mathrm{d}x' \, \mathrm{d}y'$ 

with the matrix integral kernel  ${f B}(oldsymbol{
ho},oldsymbol{
ho}'):\mathbb{R}^2 imes\mathbb{R}^2 o\mathbb{C}^{3 imes 3}$ 

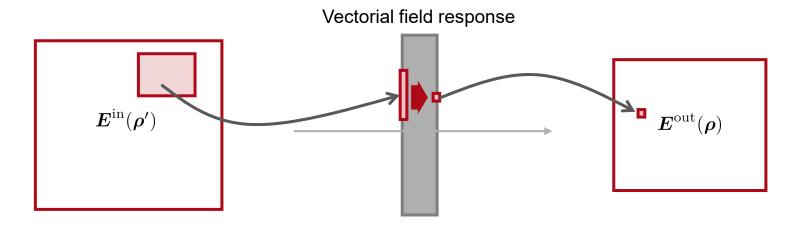
# **Field Response Operator: Local Integration Sufficient**

Input fields (index  $\alpha$ )

 $\boldsymbol{E}^{\rm in}(\boldsymbol{\rho},\omega,\alpha) = \boldsymbol{U}^{\rm in}(\boldsymbol{\rho},\omega,\alpha) \exp\left(\mathrm{i}\psi^{\rm in}(\boldsymbol{\rho},\omega,\alpha)\right)$ 

Output fields (index  $\alpha$ )

$$\boldsymbol{E}^{\mathrm{out}}(\boldsymbol{\rho},\omega,\alpha) = \boldsymbol{U}^{\mathrm{out}}(\boldsymbol{\rho},\omega,\alpha) \exp\left(\mathrm{i}\psi^{\mathrm{out}}(\boldsymbol{\rho},\omega,\alpha)\right)$$



$$egin{aligned} &m{E}^{ ext{out}}(m{
ho}) = m{\mathcal{B}}\!ig(m{
ho}' \mapsto m{E}^{ ext{in}}(m{
ho}')ig)(m{
ho}) \ &= \int \int_{X \subset X^{ ext{in}}} m{B}(m{
ho},m{
ho}')m{E}^{ ext{in}}(m{
ho}')\,\mathrm{d}x'\,\mathrm{d}y \end{aligned}$$

with the matrix integral kernel  $\mathbf{B}(oldsymbol{
ho},oldsymbol{
ho}'):\mathbb{R}^2 imes\mathbb{R}^2 o\mathbb{C}^{3 imes 3}$ 

### **Field Response Operator: Pointwise**

Input fields (index  $\alpha$ ) Output fields (index  $\alpha$ )  $\boldsymbol{E}^{\text{in}}(\boldsymbol{\rho},\omega,\alpha) = \boldsymbol{U}^{\text{in}}(\boldsymbol{\rho},\omega,\alpha) \exp\left(\mathrm{i}\psi^{\text{in}}(\boldsymbol{\rho},\omega,\alpha)\right)$  $\boldsymbol{E}^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha) = \boldsymbol{U}^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha) \exp\left(\mathrm{i}\psi^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha)\right)$ Vectorial field response •  $E^{\mathrm{out}}(\boldsymbol{
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with the matrix integral kernel  $\mathbf{B}(\bm{\rho},\bm{\rho}'):\mathbb{R}^2\times\mathbb{R}^2\to\mathbb{C}^{3\times3}$ 

# **Field Response Operator: Pointwise**

Input fields (index  $\alpha$ )  $E^{in}(\rho, \omega, \alpha) = U^{in}(\rho, \omega, \alpha) \exp (i\psi^{in}(\rho, \omega, \alpha))$ Vectorial field response  $E^{in}(\rho')$   $E^{out}(\rho)$  $E^{out}(\rho)$ 

Field response:  $\underline{B}(\rho')E^{\mathrm{in}}(\rho')\mapsto E^{\mathrm{out}}(\rho)$ 

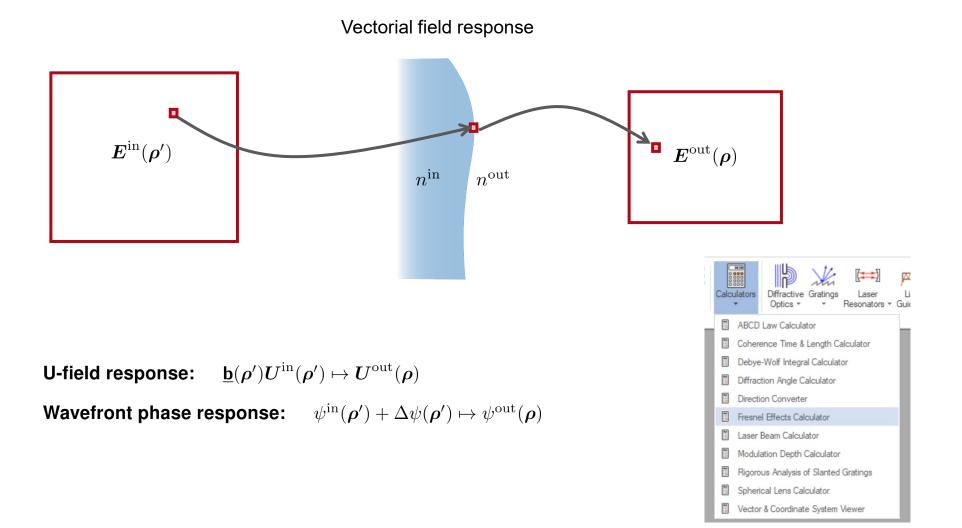
with the field response matrix  $\underline{\mathbf{B}}(oldsymbol{
ho}):\mathbb{R}^2
ightarrow\mathbb{C}^{3 imes 3}$ 

### **Field Response Operator: Pointwise**

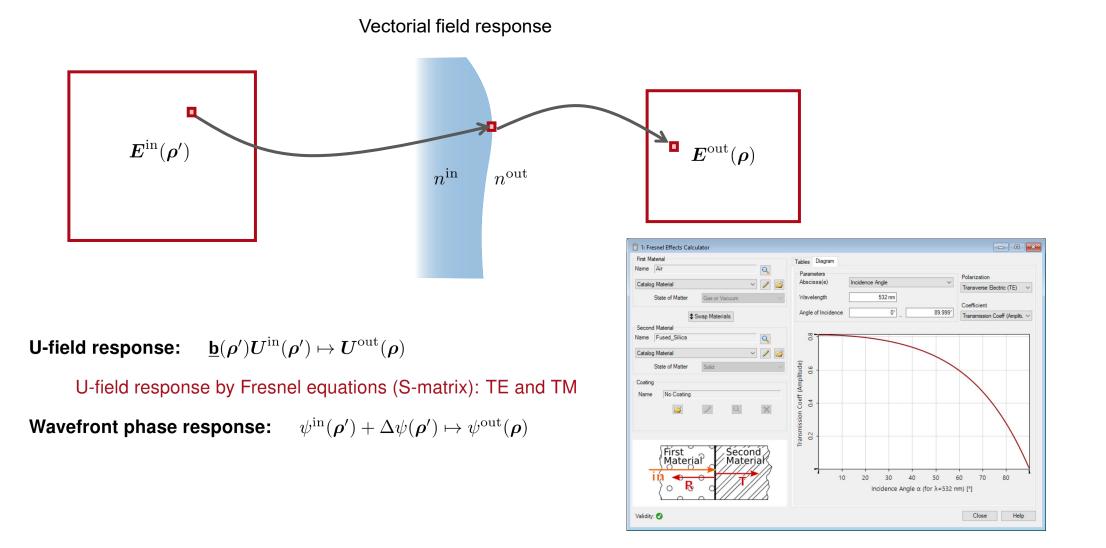
Input fields (index  $\alpha$ ) Output fields (index  $\alpha$ )  $\boldsymbol{E}^{\mathrm{in}}(\boldsymbol{\rho},\omega,\alpha) = \boldsymbol{U}^{\mathrm{in}}(\boldsymbol{\rho},\omega,\alpha) \exp\left(\mathrm{i}\psi^{\mathrm{in}}(\boldsymbol{\rho},\omega,\alpha)\right)$  $\boldsymbol{E}^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha) = \boldsymbol{U}^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha) \exp\left(\mathrm{i}\psi^{\text{out}}(\boldsymbol{\rho}, \omega, \alpha)\right)$ Vectorial field response  $oldsymbol{E}^{\mathrm{in}}(oldsymbol{
ho}')$  $\bullet$   $E^{\text{out}}(\boldsymbol{\rho})$  $\underline{\mathbf{b}}({oldsymbol 
ho}') {oldsymbol U}^{\mathrm{in}}({oldsymbol 
ho}') \mapsto {oldsymbol U}^{\mathrm{out}}({oldsymbol 
ho})$ U-field response:

Wavefront phase response:  $\psi^{in}(\rho') + \Delta \psi(\rho') \mapsto \psi^{out}(\rho)$ 

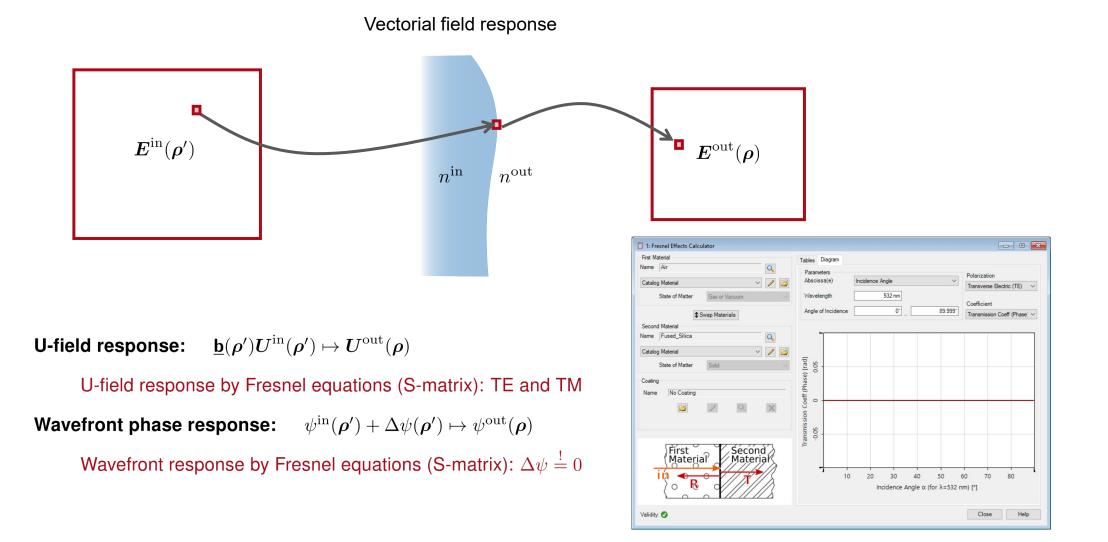
#### **Field Response Operator: Freeform Surfaces**



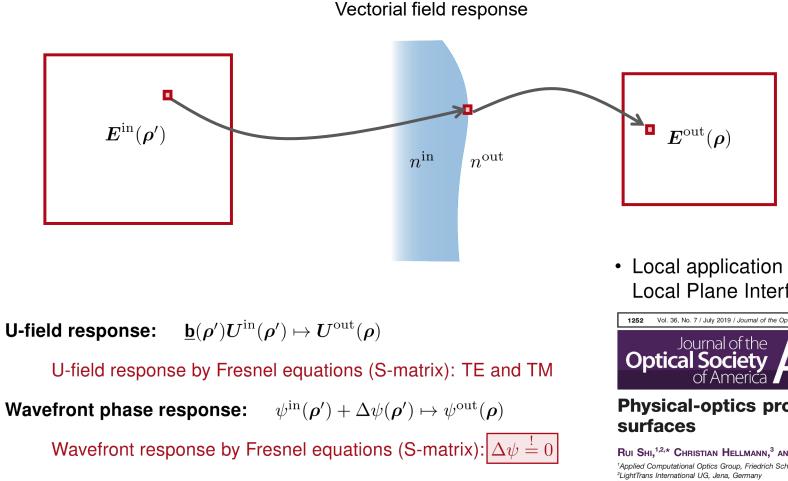
#### **Field Response Operator: Freeform Surfaces**



#### **Field Response Operator: Freeform Surfaces**



### Field Response Operator: Freeform Surfaces



 Local application of S-matrix for curved surfaces: Local Plane Interface Approximation (LPIA).



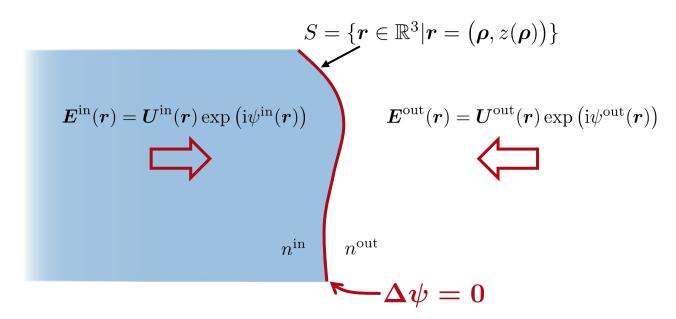
#### Physical-optics propagation through curved

#### RUI SHI,<sup>1,2,\*</sup> CHRISTIAN HELLMANN,<sup>3</sup> AND FRANK WYROWSKI<sup>1</sup>

<sup>1</sup>Applied Computational Optics Group, Friedrich Schiller University Jena, Jena, Germany <sup>3</sup>Wvrowski Photonics UG, Jena, Germanv \*Corresponding author: rui.shi@uni-jena.de



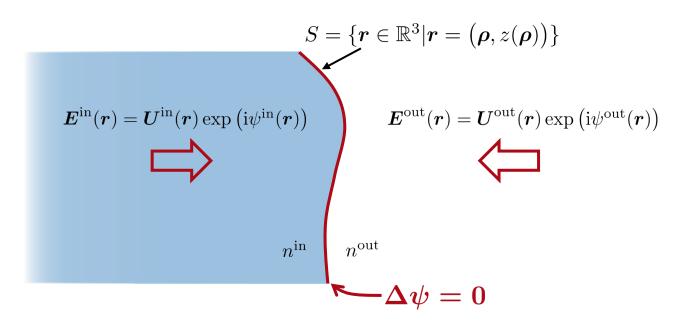
#### **Freeform Surface Design: Inverse Propagation**



Calculate the surface  $S \subset \mathbb{R}^3$  on which:

$$\psi^{\text{out}}(\boldsymbol{r}\in S) - \psi^{\text{in}}(\boldsymbol{r}\in S) = \Delta\psi(\boldsymbol{r}\in S) \stackrel{!}{=} 0$$

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VirtualLab Fusion provides an algorithm to calculate the freeform surface for any type of specified wavefront phase transformation.

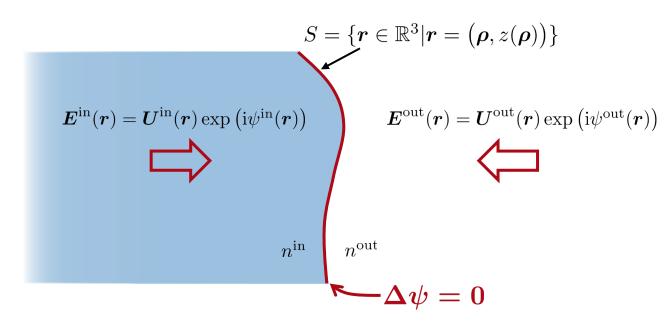


VirtualLab Fusion 2021

Available surface representations include

- Point cloud & B-Splines
- Zernike polynomials (recursive)
- Forbes polynomials
- Aspherical polynomial series
- Polynomial series

#### **Freeform Surface Design: Inverse Propagation**



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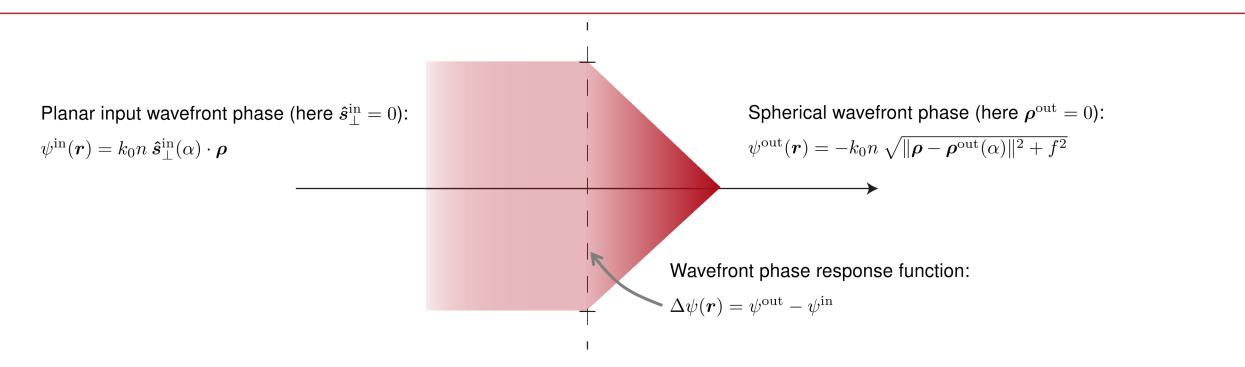


VirtualLab Fusion 2021

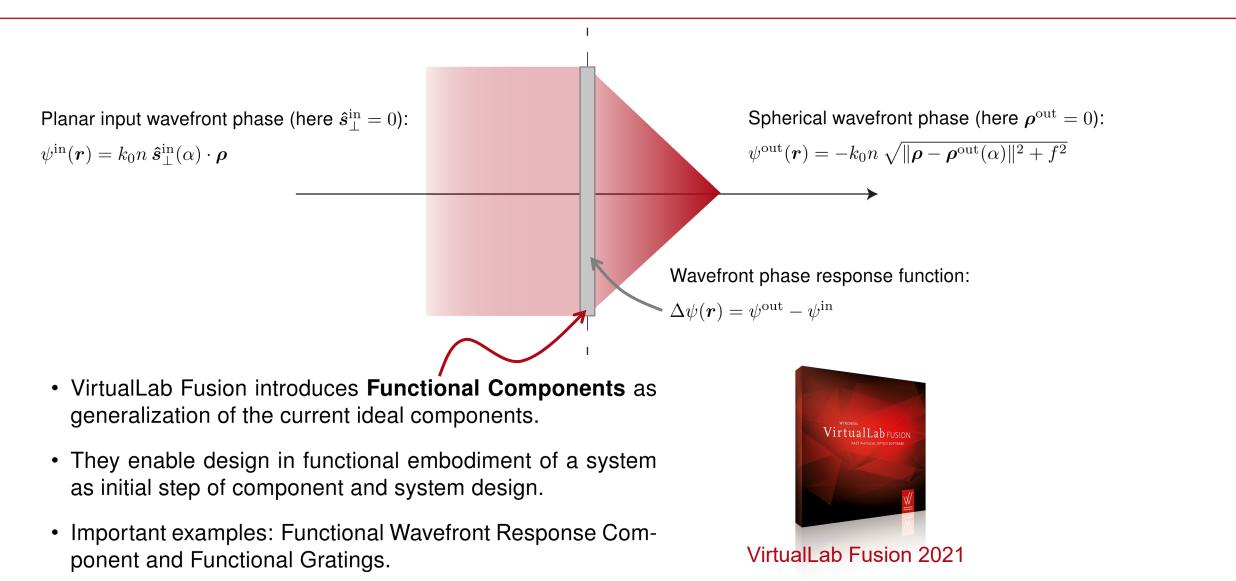
- The algorithm directly calculates the surface by inverse propagation techniques.
- No parametric optimization is involved.
- Thus, a high number of freeform surface parameters is not critical.

# **Example Focusing**

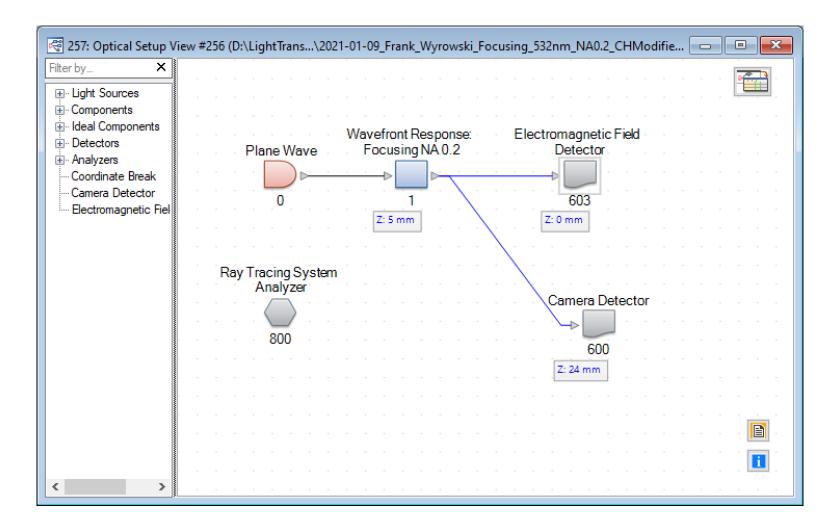
# **Focusing Lens: Scenario**



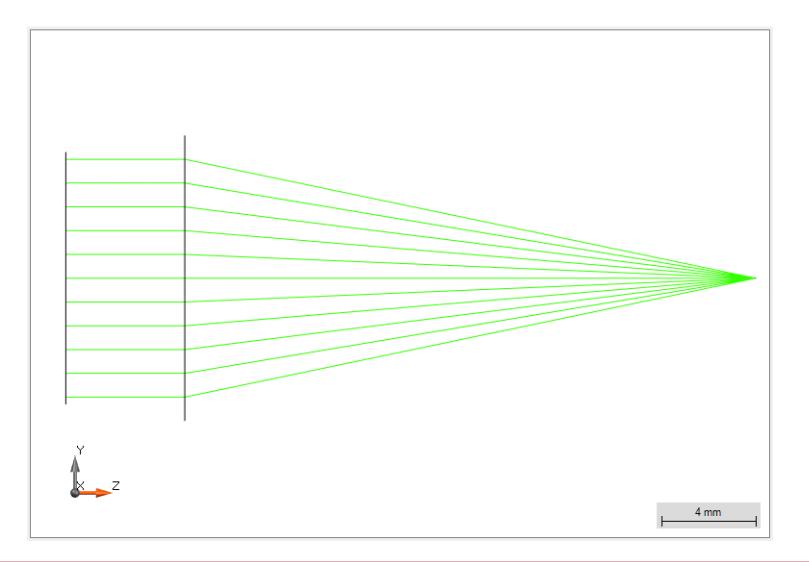
# **Focusing Lens: Functional Design**



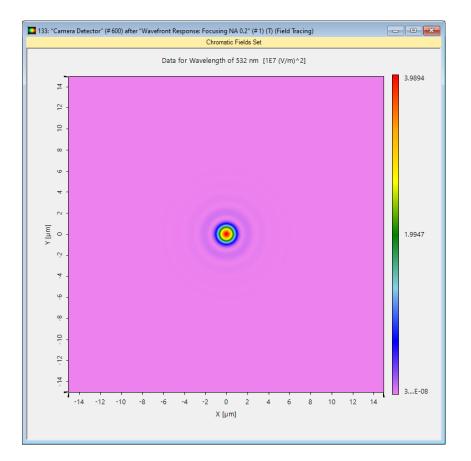
#### **Functional Design: Focusing (NA = 0.2)**



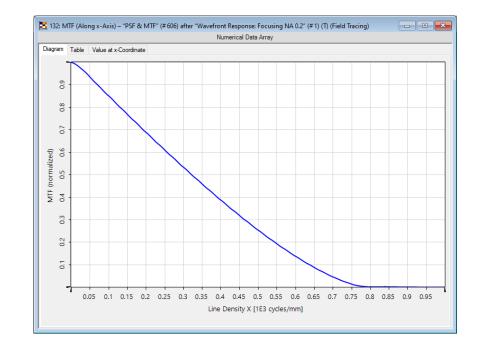
#### **Functional Design: Focusing (NA = 0.2) – Ray Tracing**



# **Functional Design: Focusing (NA = 0.2) – Field Tracing**

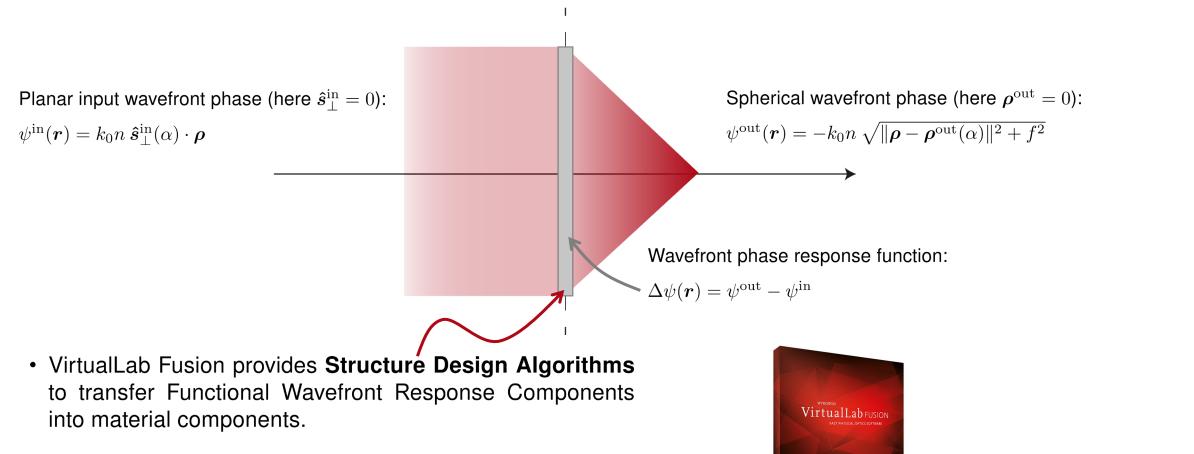


Field in Focus (False Color)



MTF

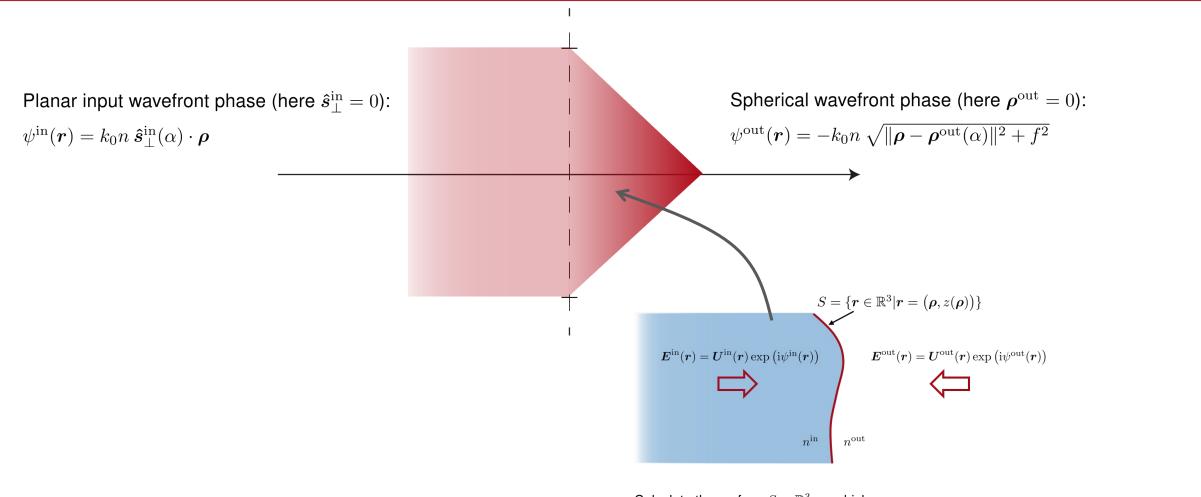
# **Focusing Lens: Structural Design**



• Example types: smooth surfaces (freeform), DOE, meta surfaces, segmented surfaces (generalized Fresnel lenses), modulated volume gratings.

VirtualLab Fusion 2021

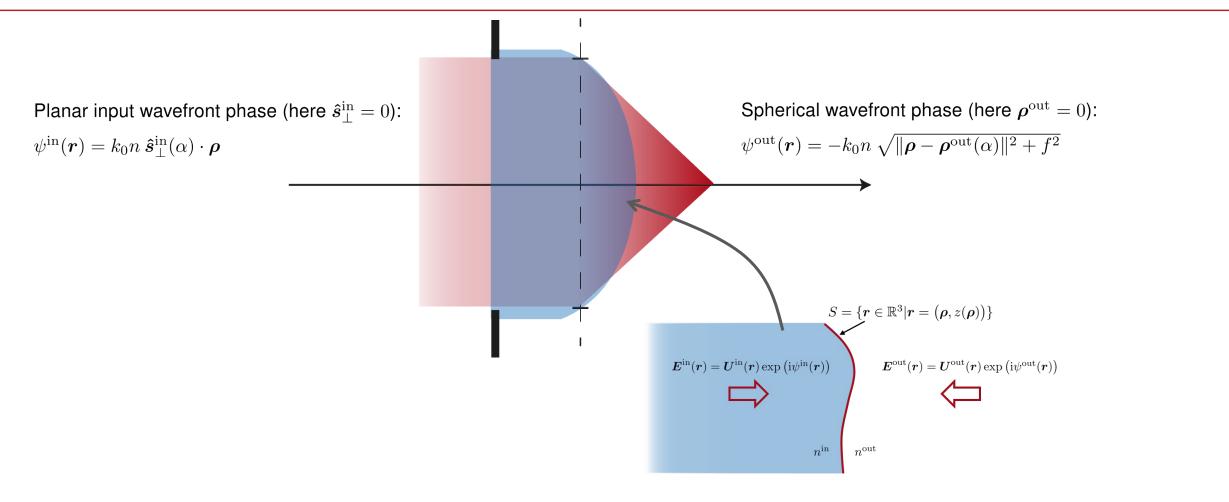
# **Focusing Lens: Surface Design**



Calculate the surface  $S \subset \mathbb{R}^3$  on which:

 $\psi^{\text{out}}(\boldsymbol{r}\in S) - \psi^{\text{in}}(\boldsymbol{r}\in S) = \Delta\psi(\boldsymbol{r}\in S) \stackrel{!}{=} 0$ 

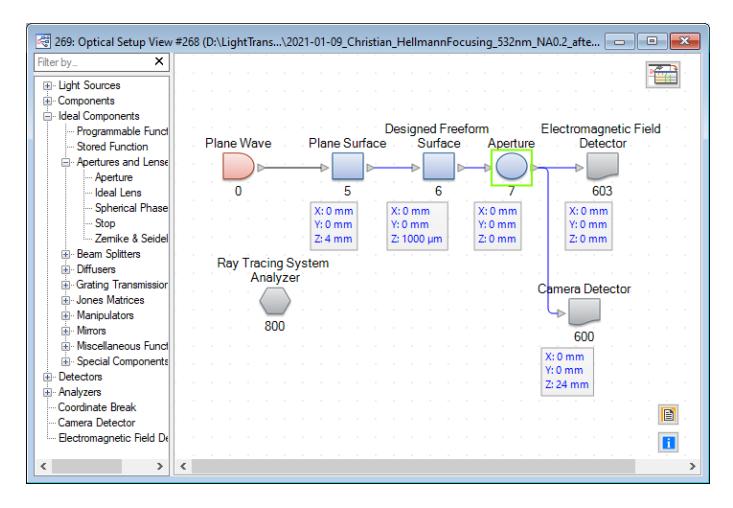
# **Focusing Lens: Surface Design**



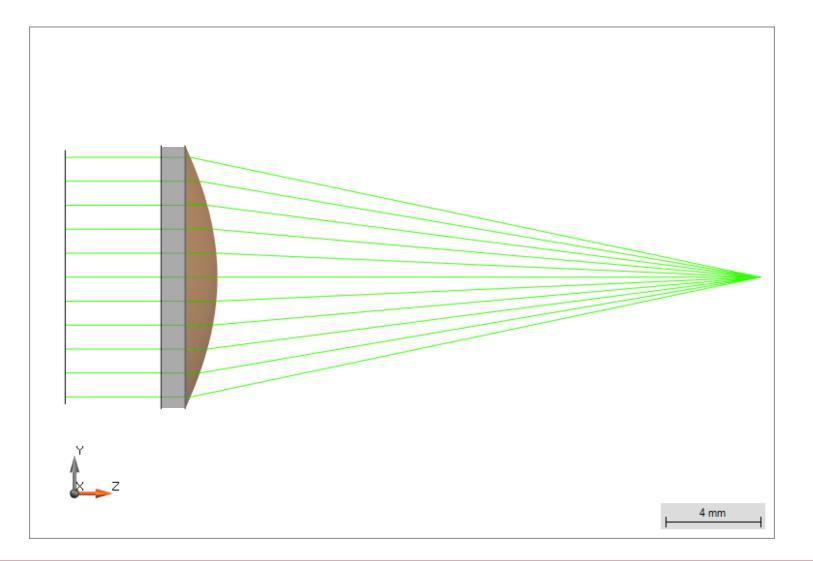
Calculate the surface  $S \subset \mathbb{R}^3$  on which:

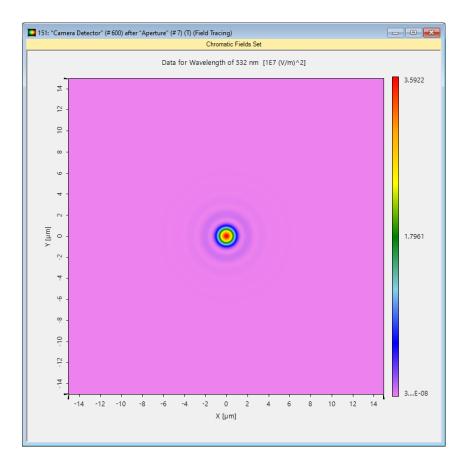
 $\psi^{\text{out}}(\boldsymbol{r}\in S) - \psi^{\text{in}}(\boldsymbol{r}\in S) = \Delta\psi(\boldsymbol{r}\in S) \stackrel{!}{=} 0$ 

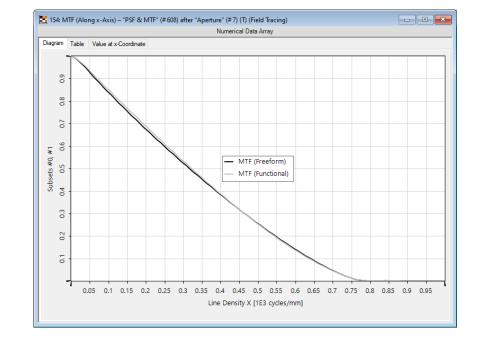
#### **Structural Design Focusing (NA = 0.2): Lens**



#### Focusing (NA = 0.2) Lens: Ray Tracing



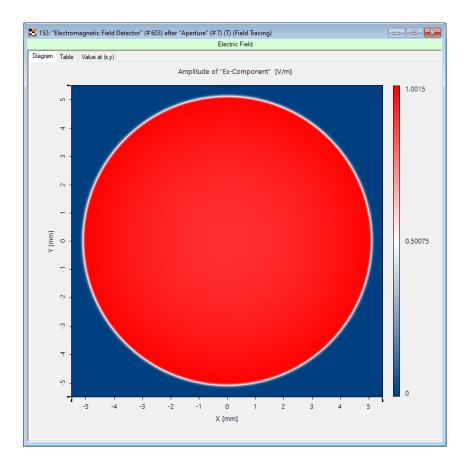


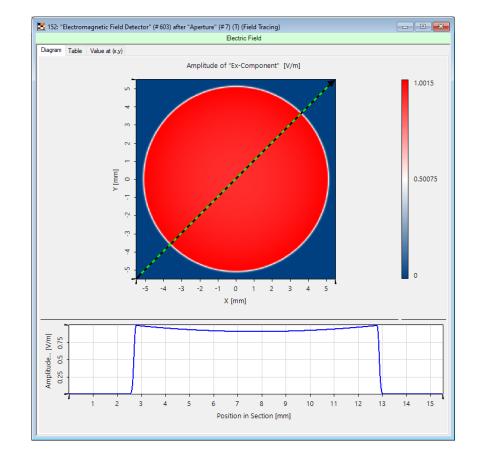


Energy Density in Focus (False Color)

MTF

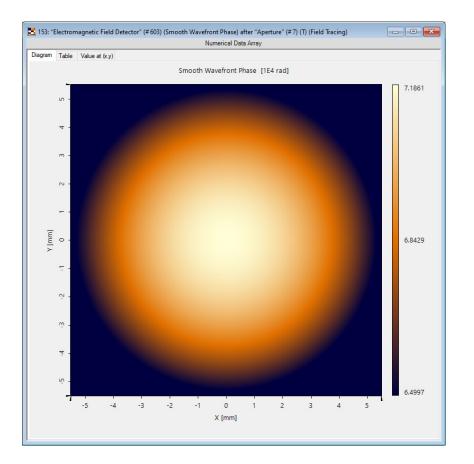
Efficiency: 91.1% (efficiency after first plane: 96.5%)



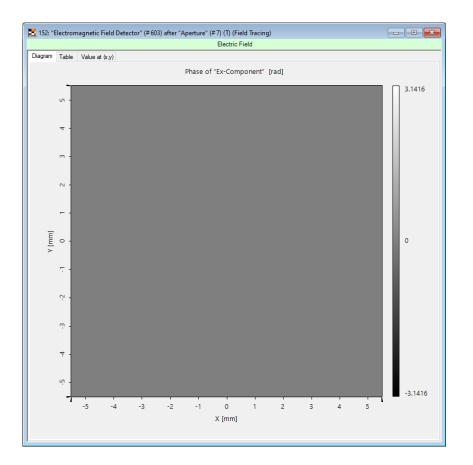


#### Amplitude after lens

Amplitude after lens

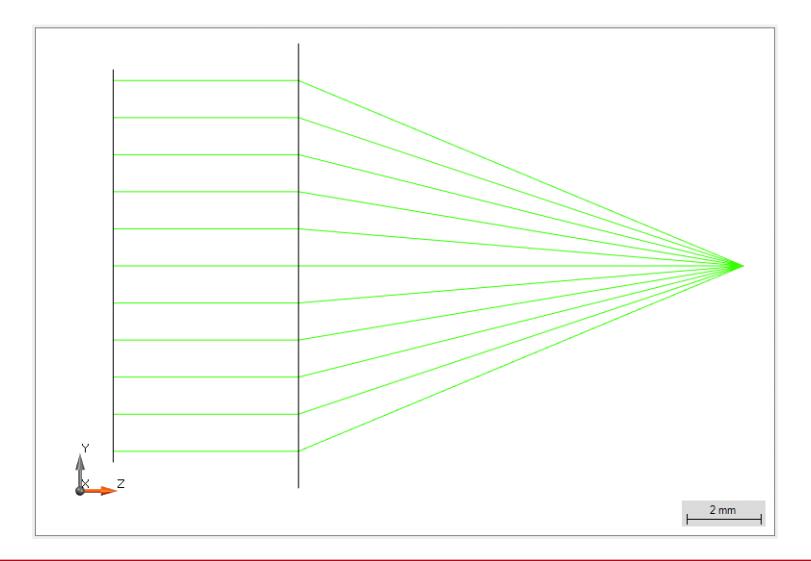


Wavefront phase after lens

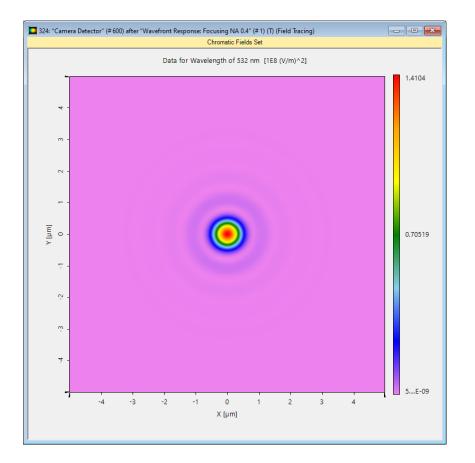


Wavefront phase error after lens

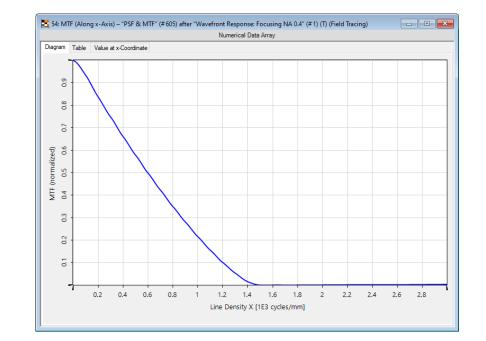
#### **Functional Design: Focusing (NA = 0.4) – Ray Tracing**



# **Functional Design: Focusing (NA = 0.4) – Field Tracing**

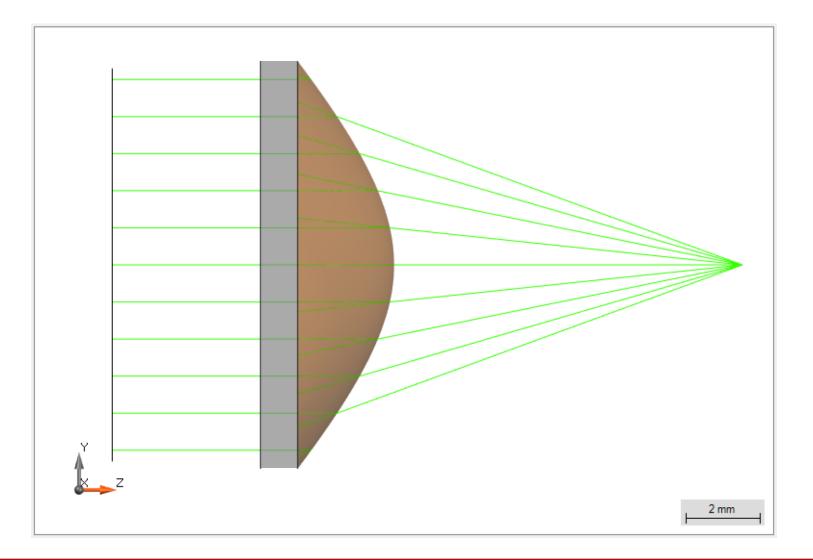


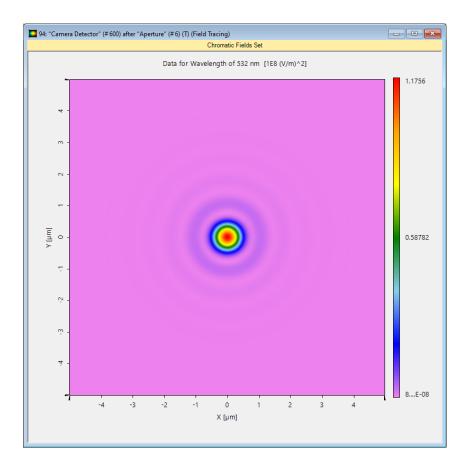
Energy Density in Focus (False Color)



MTF

#### Focusing (NA = 0.4) Lens: Ray Tracing



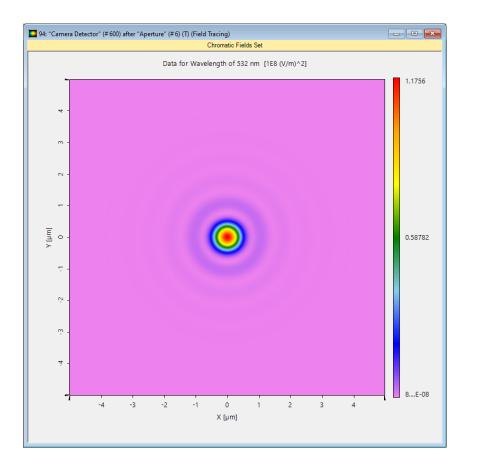


- - -2 97: MTF (Along x-Axis) - "PSF & MTF" (# 605) after "Aperture" (# 6) (T) (Field Tracing) Numerical Data Array Diagram Table Value at x-Coordinate 0.9 0.8 0.7 #1 0.6 د #0°+ 0.5 MTF (Freeform) MTF (Functional) Sub 0.4 0.3 0.2 5 0.2 0.4 0.6 0.8 1 1.2 1.4 1.6 1.8 2 2.2 2.4 2.6 2.8 Line Density X [1E3 cycles/mm]

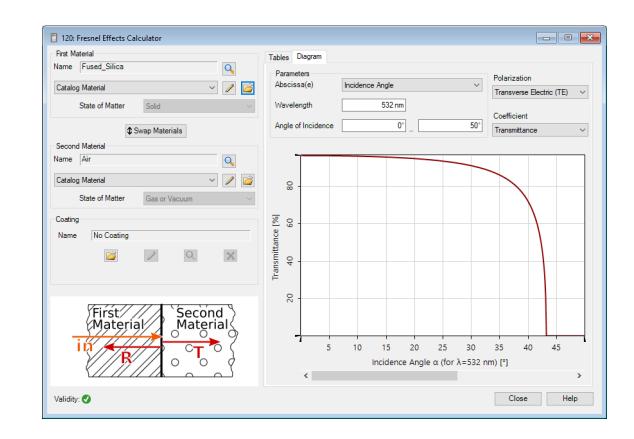
Energy Density in Focus (False Color)

MTF

Efficiency: 84.98% (efficiency after first plane: 96.5%)

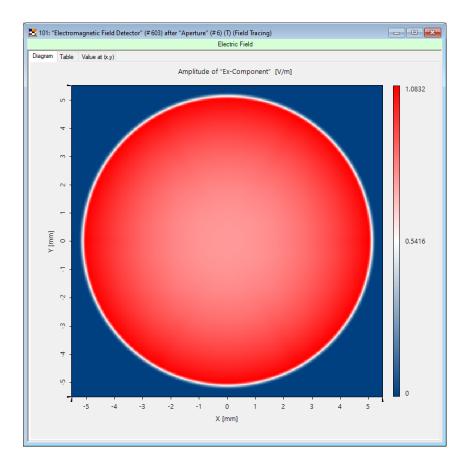


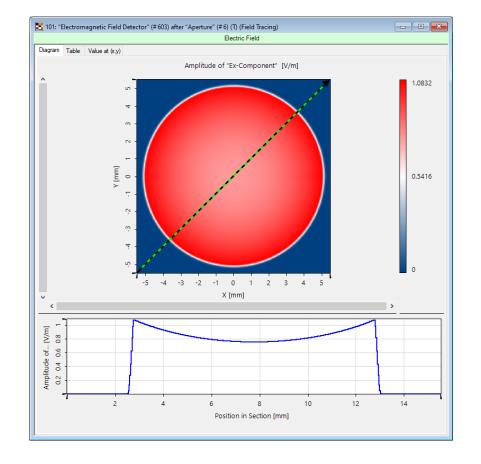
Energy Density in Focus (False Color)



#### Fresnel effect at surface

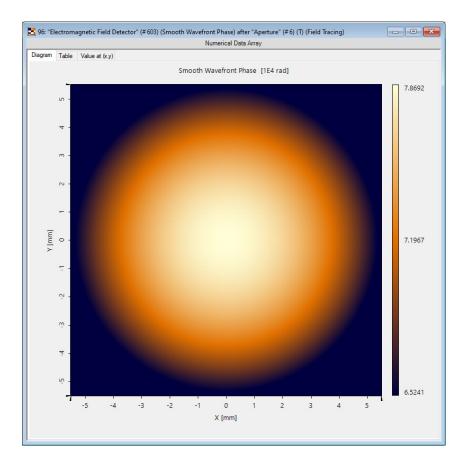
Efficiency: 84.98% (efficiency after first plane: 96.5%)



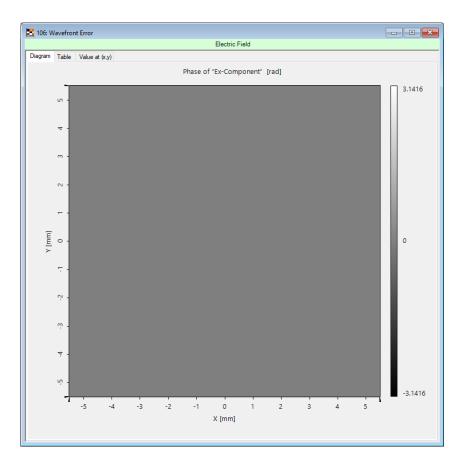


#### Amplitude after lens

Amplitude after lens

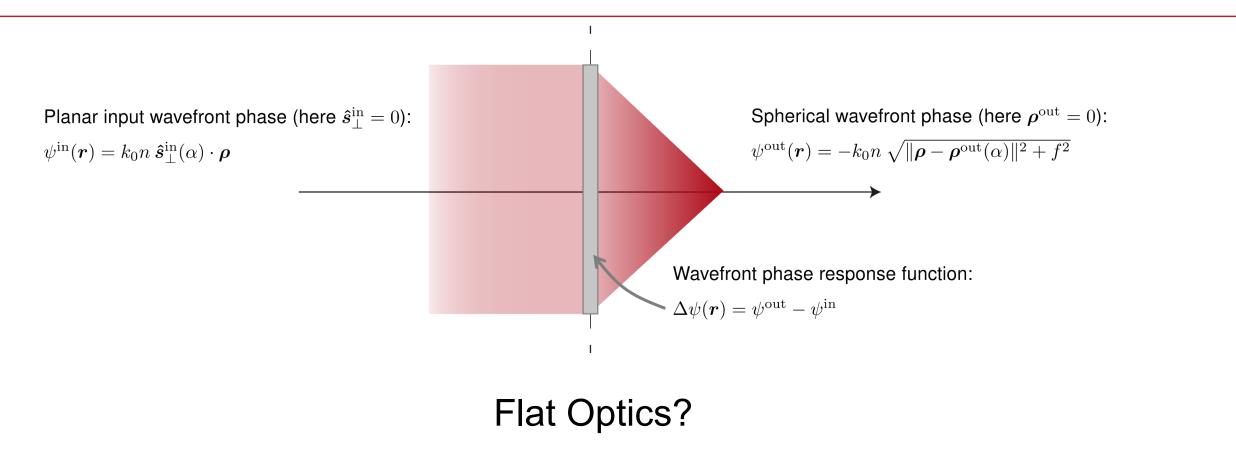


Wavefront phase after lens



#### Wavefront phase error after lens

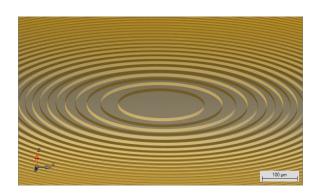
#### **Focusing Lens: Flat Optics Structural Design**



# **Structure of Webinar**

- Why physical optics in design?
- Optical design in physical optics terms
- Diffractive Optical Elements (DOE)
  - Design
  - Modeling
  - Fabrication data
- Design examples

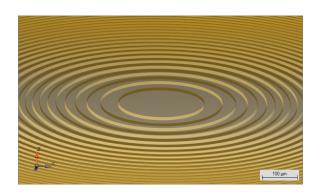




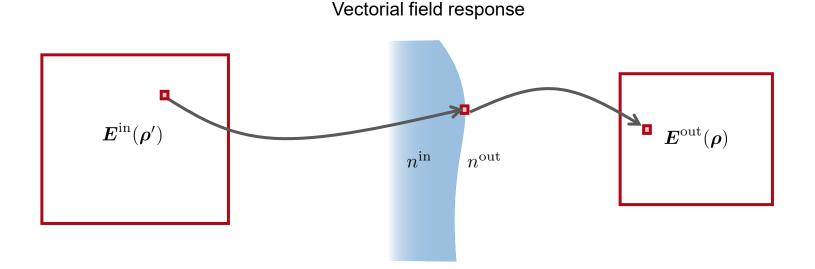
# **Structure of Webinar**

- Why physical optics in design?
- Optical design in physical optics terms
- Diffractive Optical Elements (DOE)
  - Design
  - Modeling
  - Fabrication data
- Design examples





#### **Field Response Operator: Freeform Surfaces**

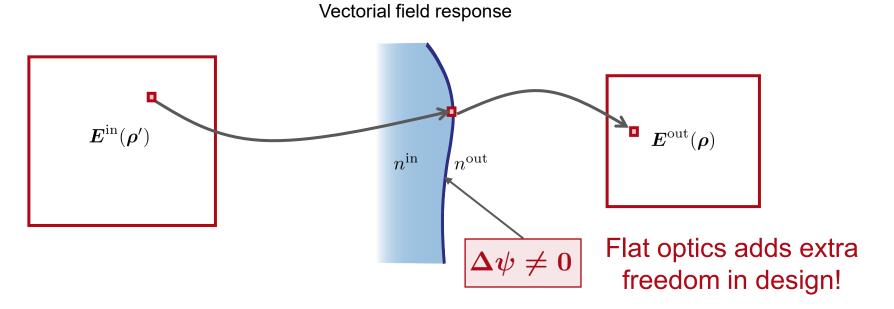


U-field response:  $\underline{\mathbf{b}}(\boldsymbol{\rho}') \boldsymbol{U}^{\mathrm{in}}(\boldsymbol{\rho}') \mapsto \boldsymbol{U}^{\mathrm{out}}(\boldsymbol{\rho})$ 

U-field response by Fresnel equations (S-matrix): TE and TM

Wavefront phase response:  $\psi^{in}(\rho') + \Delta \psi(\rho') \mapsto \psi^{out}(\rho)$ 

Wavefront response by Fresnel equations (S-matrix):  $\Delta \psi \stackrel{!}{=} 0$ 

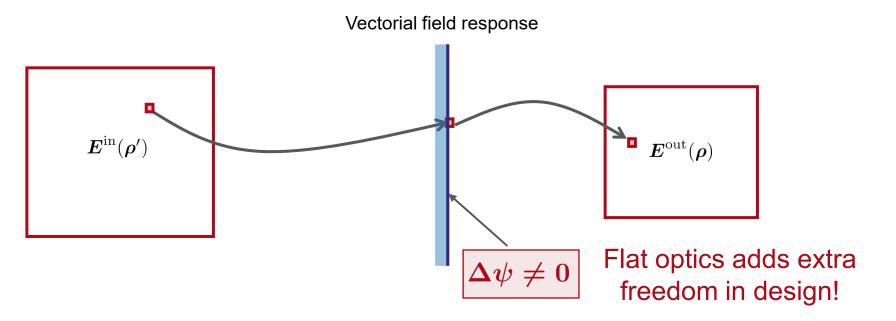


U-field response:  $\underline{\mathbf{b}}(\boldsymbol{\rho}') \boldsymbol{U}^{\mathrm{in}}(\boldsymbol{\rho}') \mapsto \boldsymbol{U}^{\mathrm{out}}(\boldsymbol{\rho})$ 

U-field response dependent on type of flat optics

Wavefront phase response:  $\psi^{in}(\rho') + \Delta \psi(\rho') \mapsto \psi^{out}(\rho)$ 

Wavefront response by different effects:  $\Delta \psi \stackrel{\cdot}{
eq} 0$ 

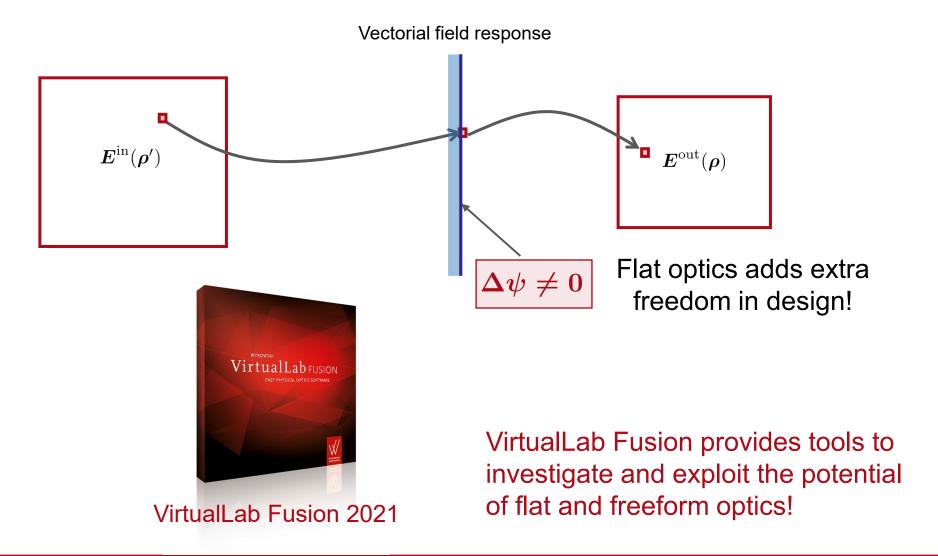


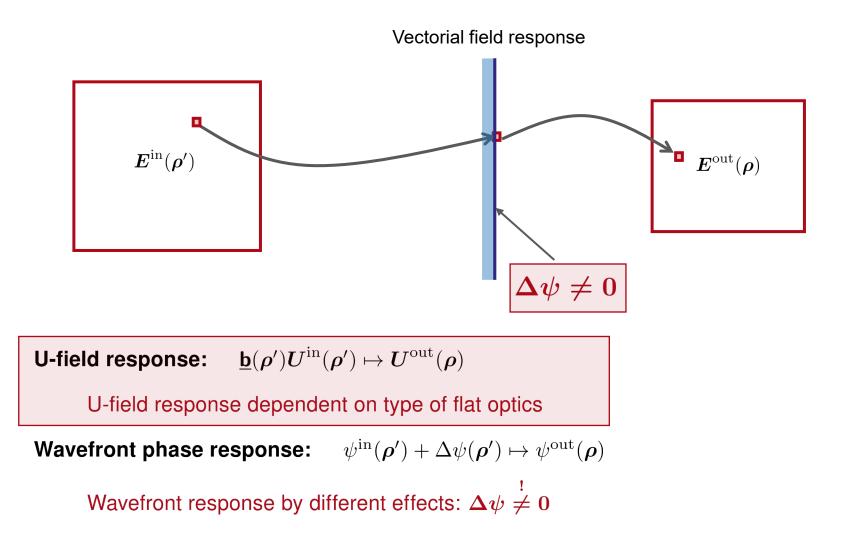
U-field response:  $\underline{\mathbf{b}}(\boldsymbol{\rho}') \boldsymbol{U}^{\mathrm{in}}(\boldsymbol{\rho}') \mapsto \boldsymbol{U}^{\mathrm{out}}(\boldsymbol{\rho})$ 

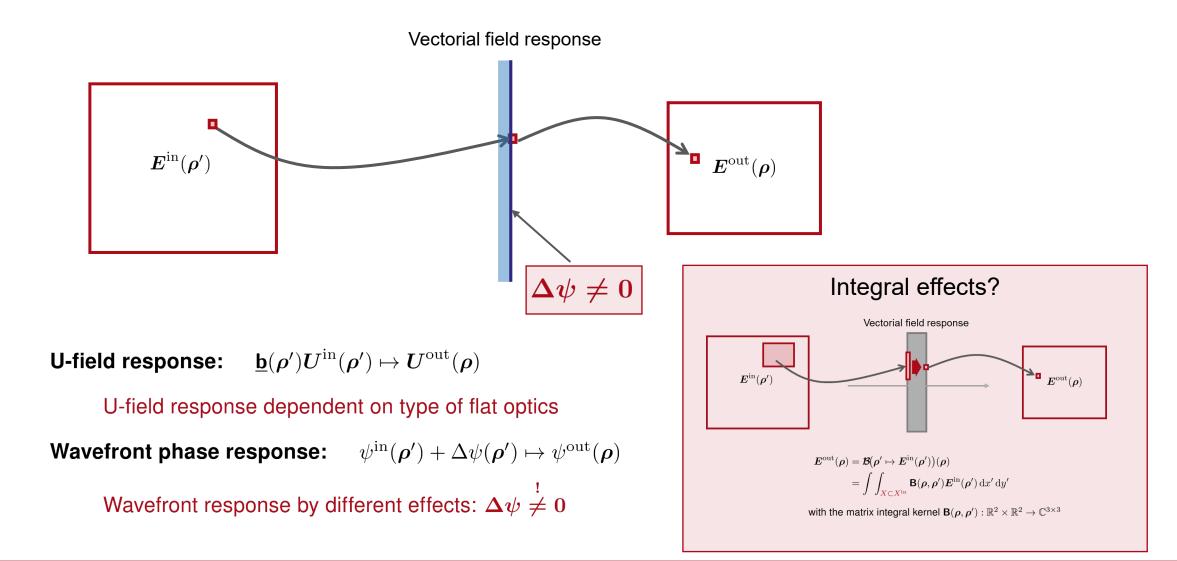
U-field response dependent on type of flat optics

Wavefront phase response:  $\psi^{in}(\rho') + \Delta \psi(\rho') \mapsto \psi^{out}(\rho)$ 

Wavefront response by different effects:  $\Delta \psi \stackrel{.}{
eq} 0$ 

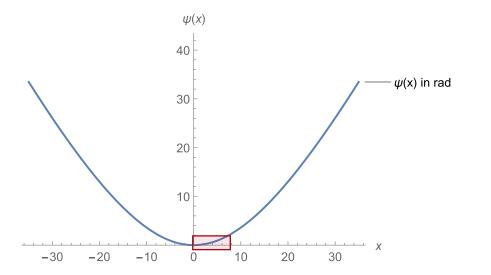




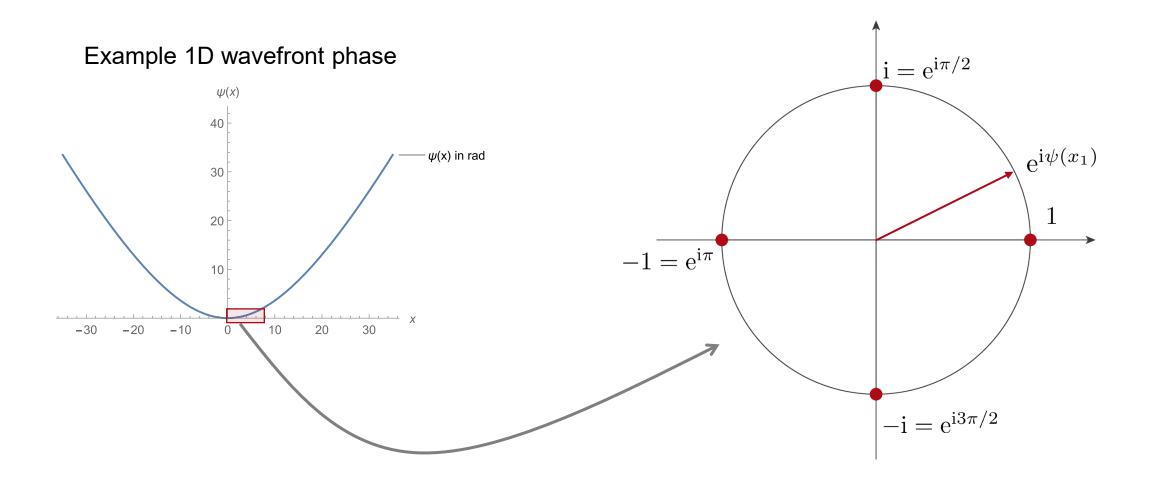


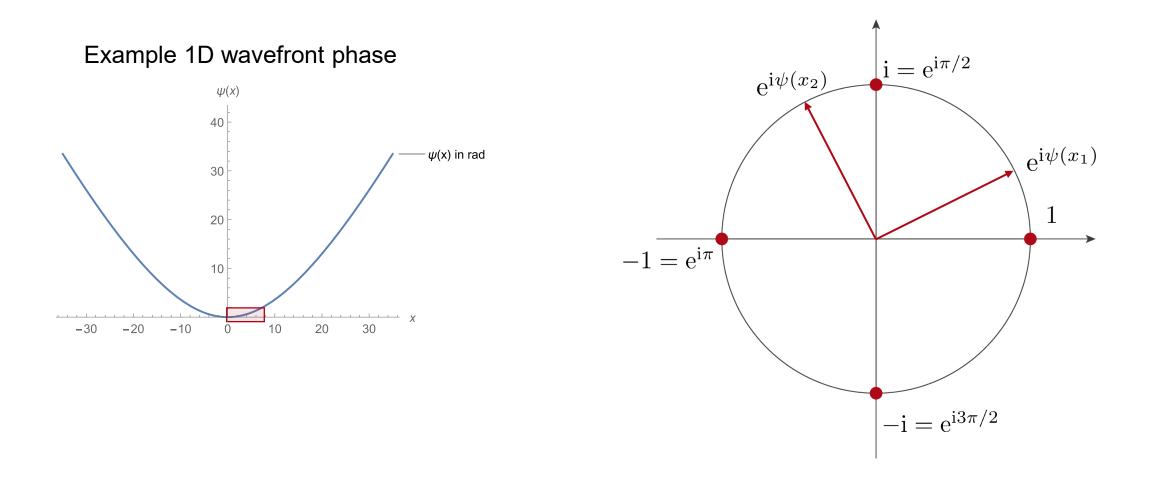
#### What Allows Flat Optics to Work?

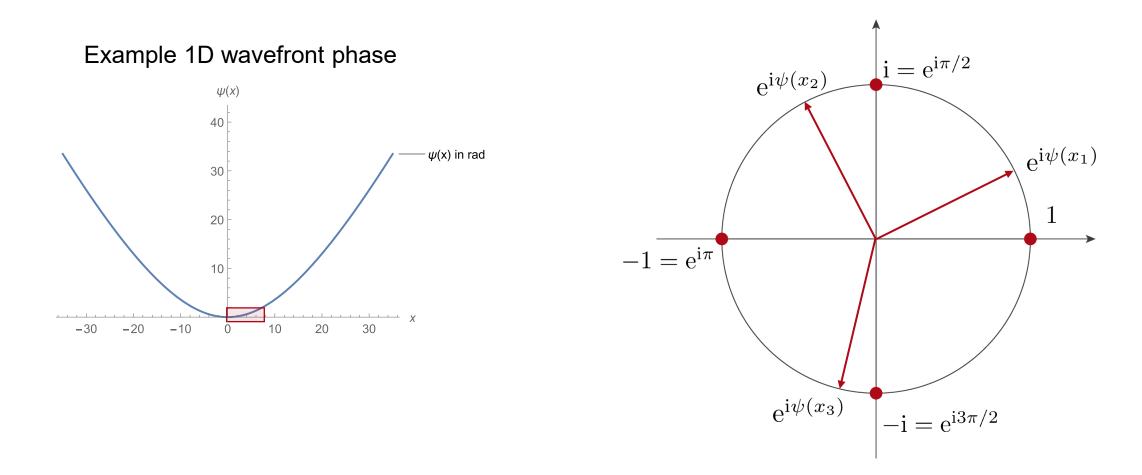
#### Example 1D wavefront phase

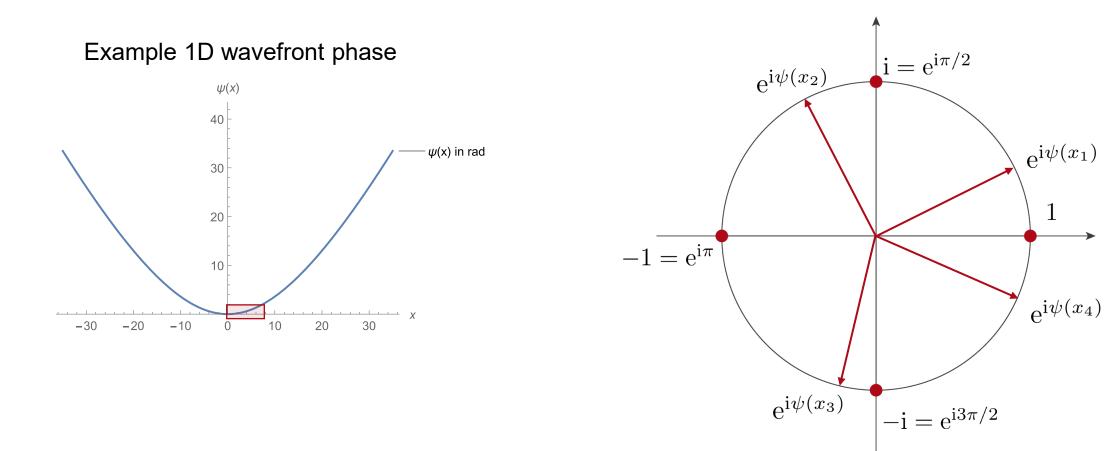


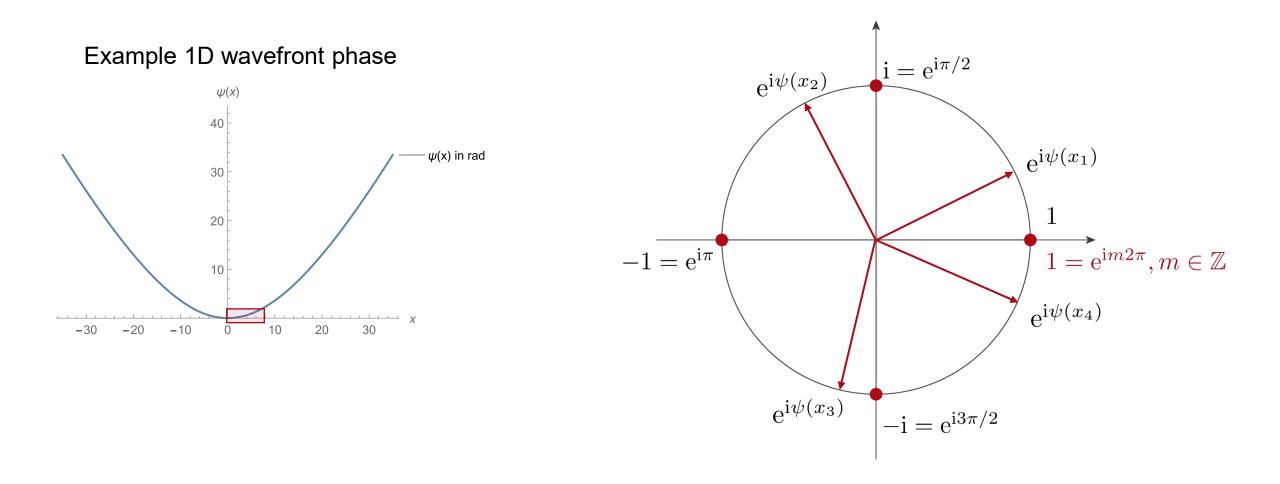
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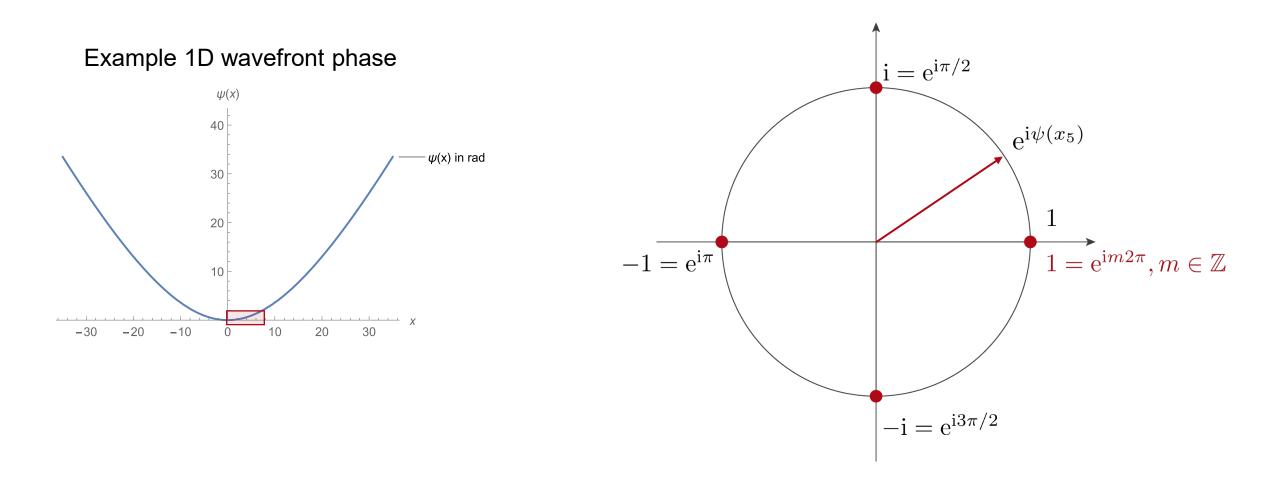










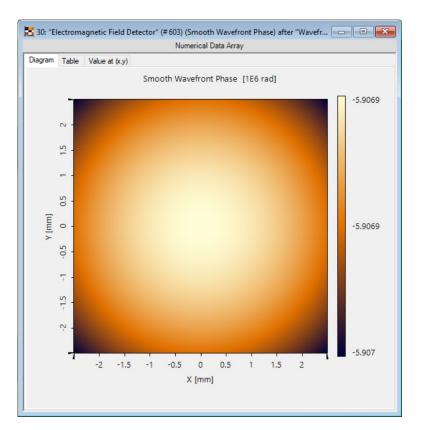


#### $\psi(x)$ $\psi(x)$ 40 40 $\psi(\mathbf{x})$ in rad 30 30 20 20 $1 = e^{i4\pi}, m = 2$ 10 $\psi(\mathbf{x})$ in rad **\_\_\_**x -20 -10 30 -30 -20 -10 10 20 30 -30 0 10 20 0

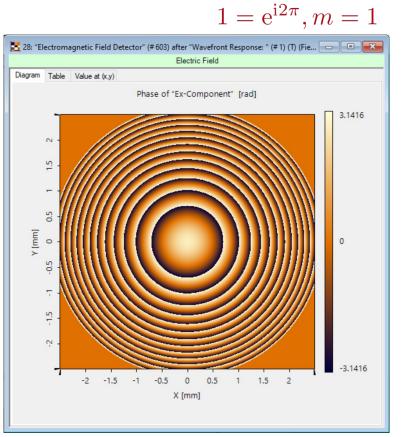
#### Example 1D wavefront phase

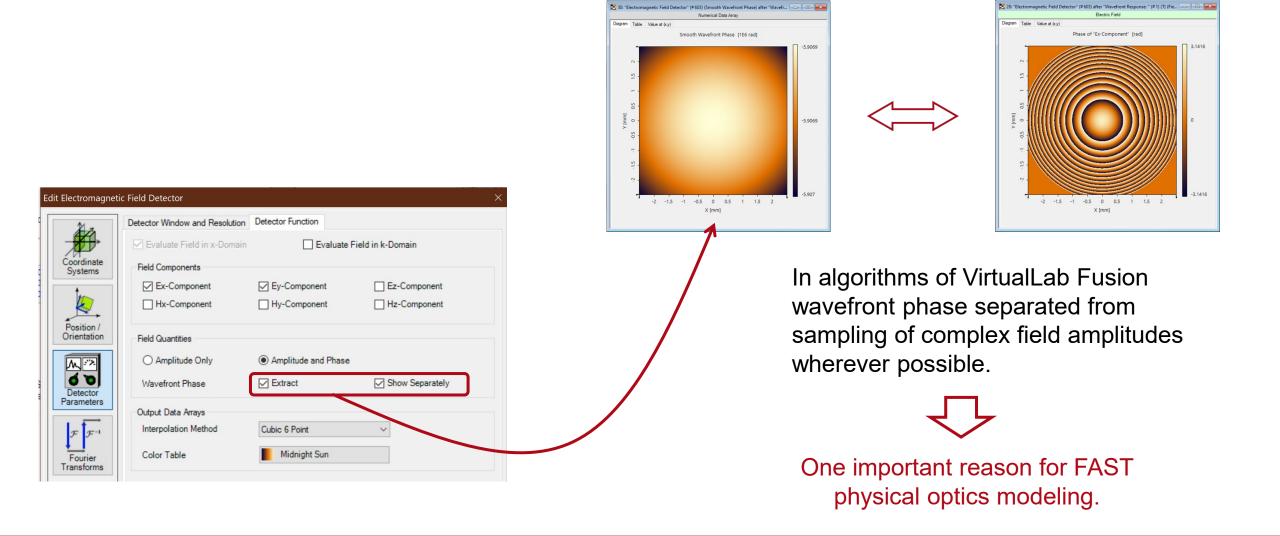
#### $\psi(x)$ $\psi(x)$ 40 40 $\psi(\mathbf{x})$ in rad 30 30 20 20 $_{10}$ 1 = e<sup>i2 $\pi$ </sup>, m = 1 10 $\psi(x)$ in rad -20 -10 30 -30 -20 -10 10 20 30 -30 0 10 20 0

#### Example 1D wavefront phase









 $1 = e^{i2\pi}, m = 1$ 

#### $\psi(x)$ $\psi(x)$ 40 40 $\psi(\mathbf{x})$ in rad 30 30 20 20 $_{10}$ 1 = e<sup>i2 $\pi$ </sup>, m = 1 10 $\psi(x)$ in rad -20 -10 30 -30 -20 -10 10 20 30 -30 0 10 20 0

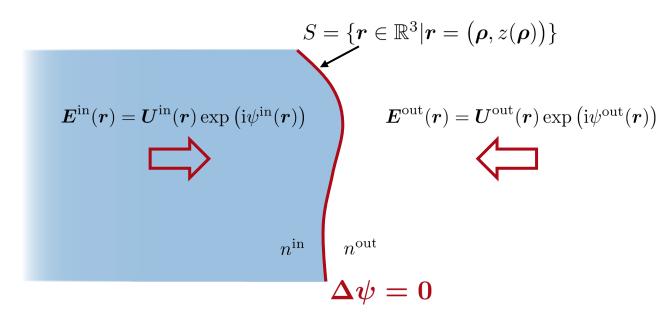
#### Example 1D wavefront phase

## **Segmented Phase Manipulation**

#### $\psi(x)$ $\psi(x)$ 40 40 $\psi(\mathbf{x})$ in rad 30 30 20 20 $1 = e^{i4\pi}, m = 2$ $-\psi(x)$ in rad ${}^{1}1 = e^{i2\pi}, m = 1$ 10 — x -40 -20 0 20 40 -20 -10 30 -30 0 10 20

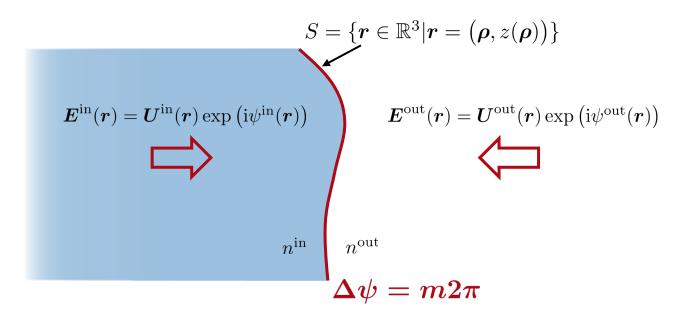
#### Example 1D wavefront phase

#### **Freeform Surface Design: Inverse Propagation**



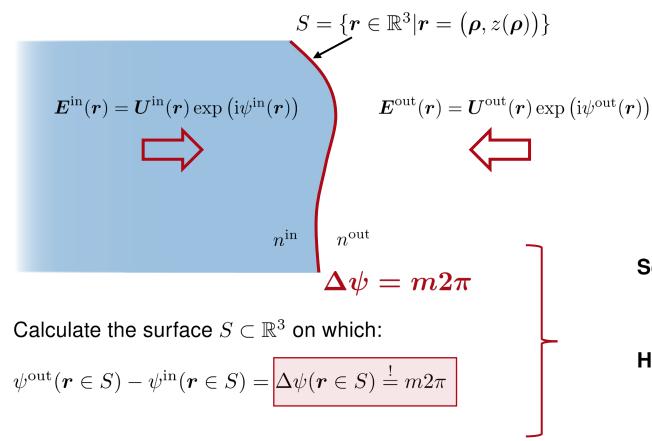
Calculate the surface  $S \subset \mathbb{R}^3$  on which:

$$\psi^{ ext{out}}(oldsymbol{r}\in S)-\psi^{ ext{in}}(oldsymbol{r}\in S)=oldsymbol{\Delta}\psi(oldsymbol{r}\in S)\stackrel{!}{=}0$$



Calculate the surface  $S \subset \mathbb{R}^3$  on which:

$$\psi^{\mathrm{out}}(\boldsymbol{r}\in S) - \psi^{\mathrm{in}}(\boldsymbol{r}\in S) = \Delta\psi(\boldsymbol{r}\in S) \stackrel{!}{=} m2\pi$$

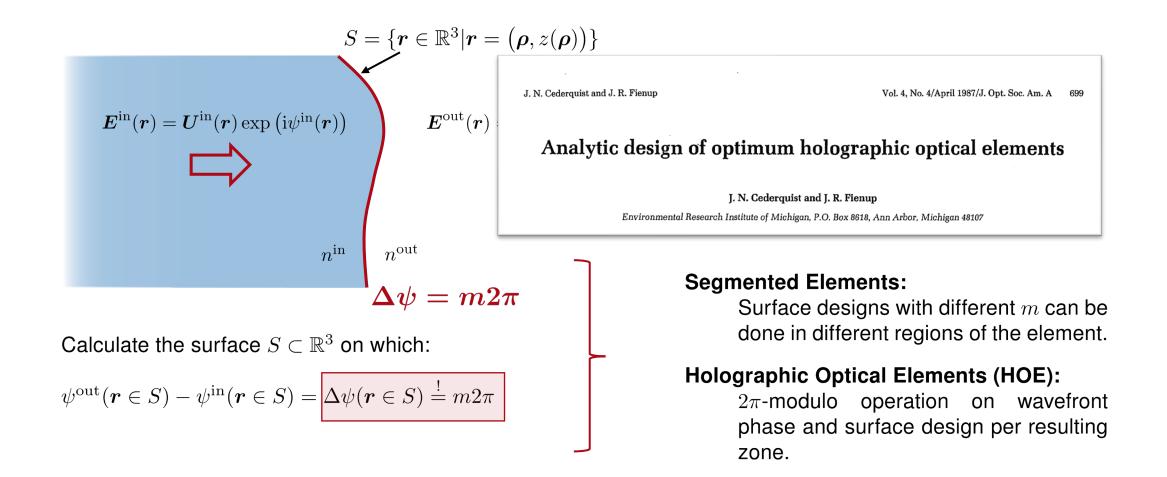


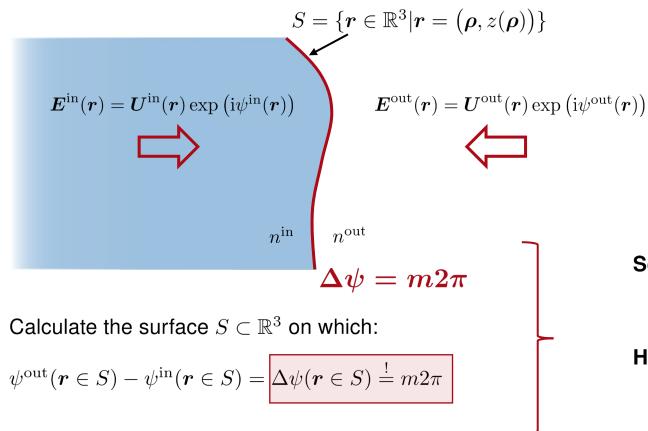
#### **Segmented Elements:**

Surface designs with different m can be done in different regions of the element.

#### Holographic Optical Elements (HOE):

 $2\pi$ -modulo operation on wavefront phase and surface design per resulting zone.







VirtualLab Fusion 2021

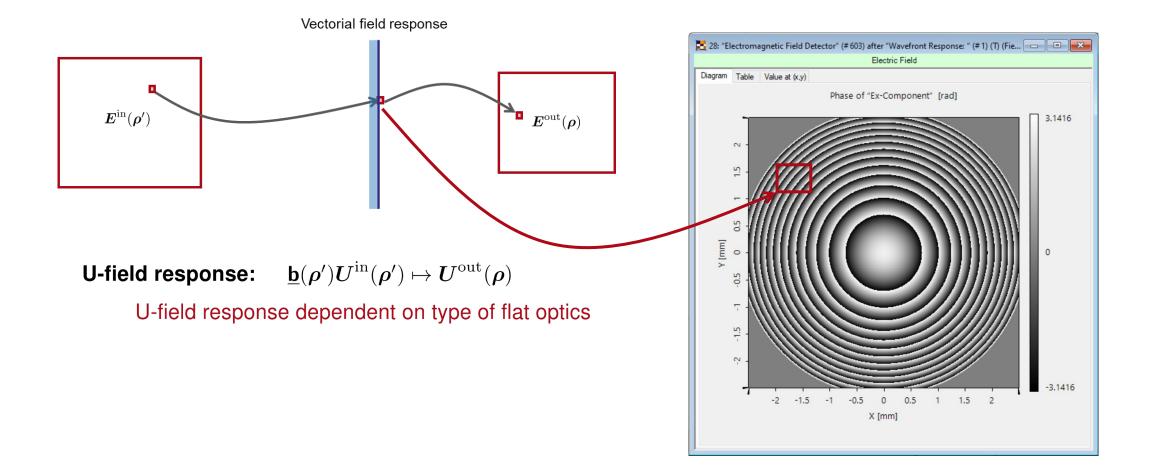
#### **Segmented Elements:**

Surface designs with different m can be done in different regions of the element.

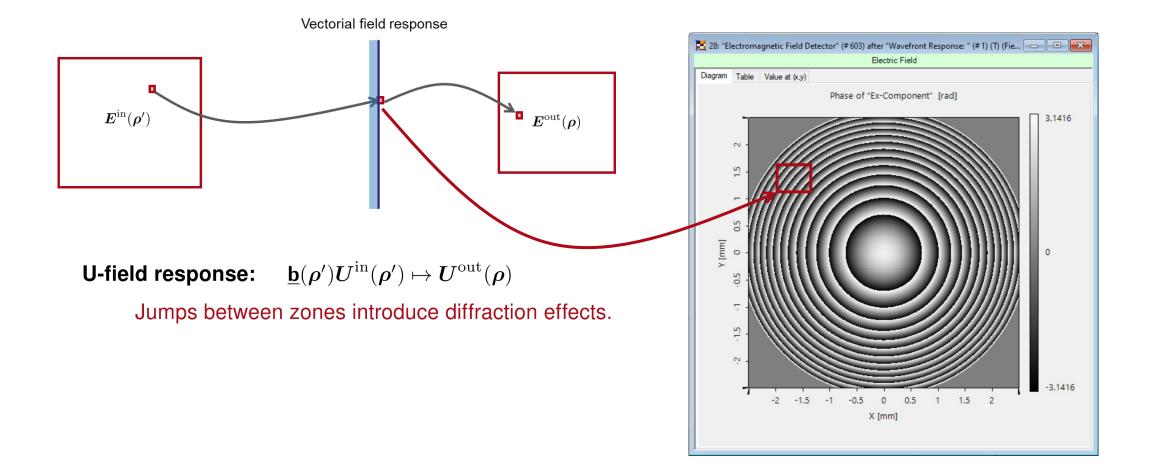
#### Holographic Optical Elements (HOE):

 $2\pi\text{-modulo}$  operation on wavefront phase and surface design per resulting zone.

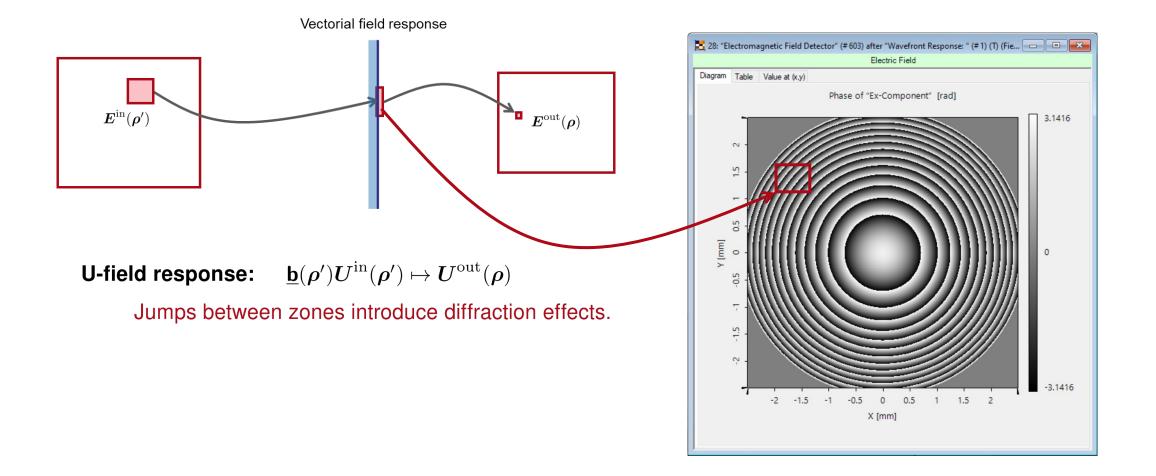
# **Field Response HOE**



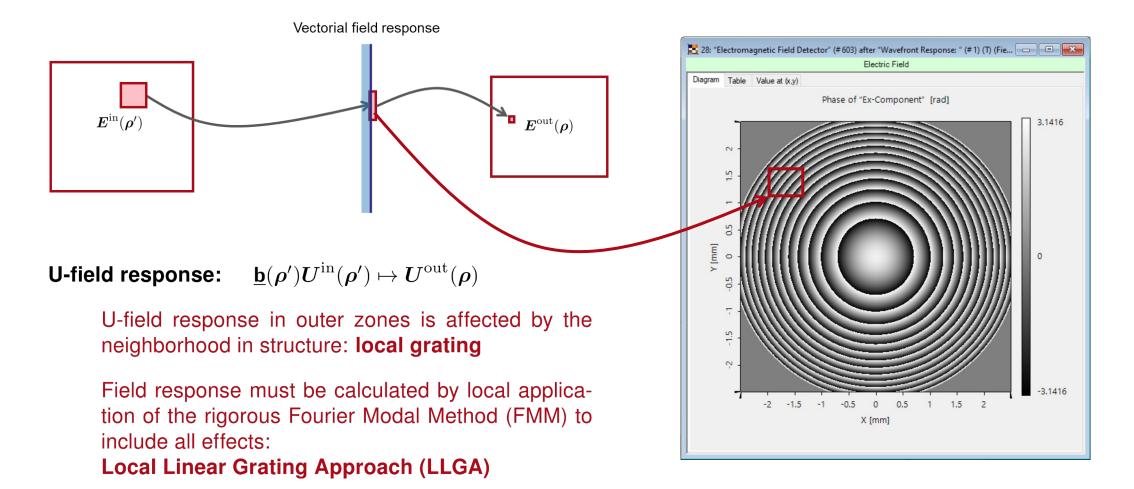
# **Field Response HOE**



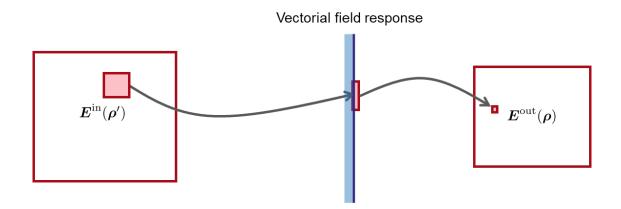
# **Field Response HOE**



## **Field Response HOE: LLGA**



# Field Response HOE: LLGA



U-field response:  $\underline{\mathbf{b}}(\boldsymbol{\rho}') U^{\mathrm{in}}(\boldsymbol{\rho}') \mapsto U^{\mathrm{out}}(\boldsymbol{\rho})$ 

U-field response in outer zones is affected by the neighborhood in structure: **local grating** 

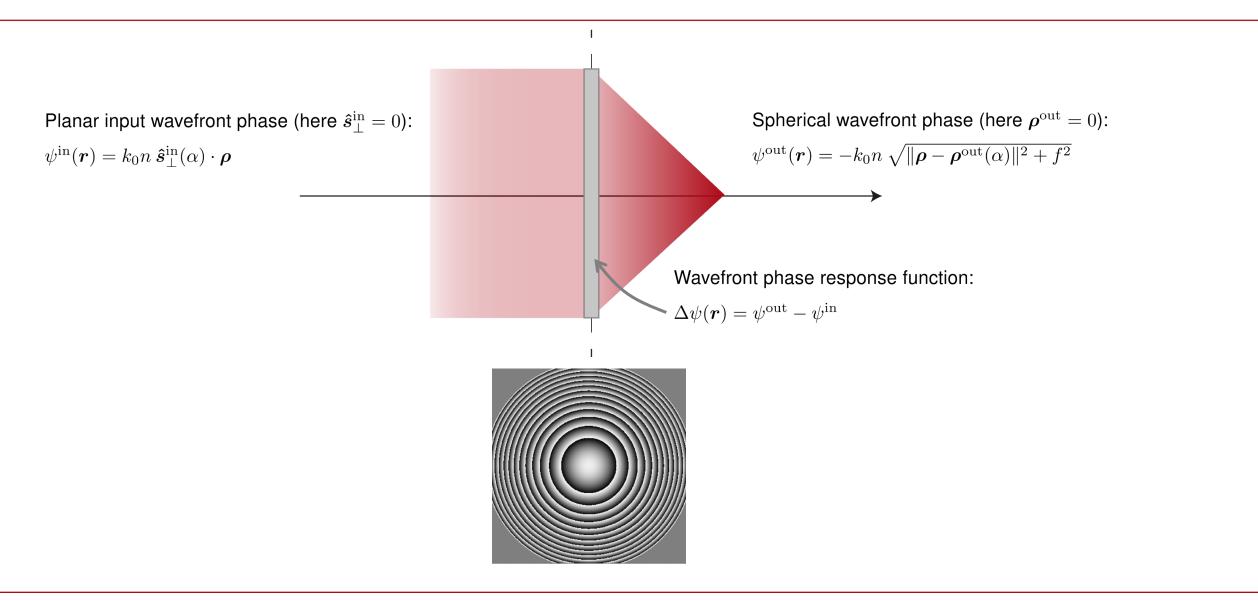
Field response must be calculated by local application of the rigorous Fourier Modal Method (FMM) to include all effects:

Local Linear Grating Approach (LLGA)

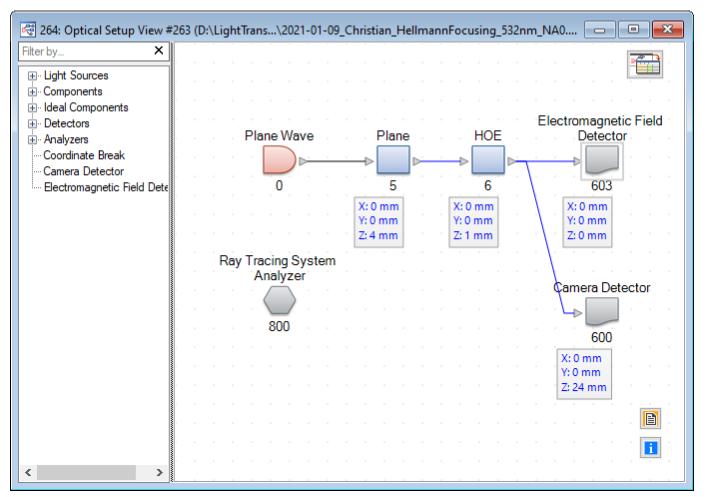


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### **Diffractive Focusing Lens: Structural Design**

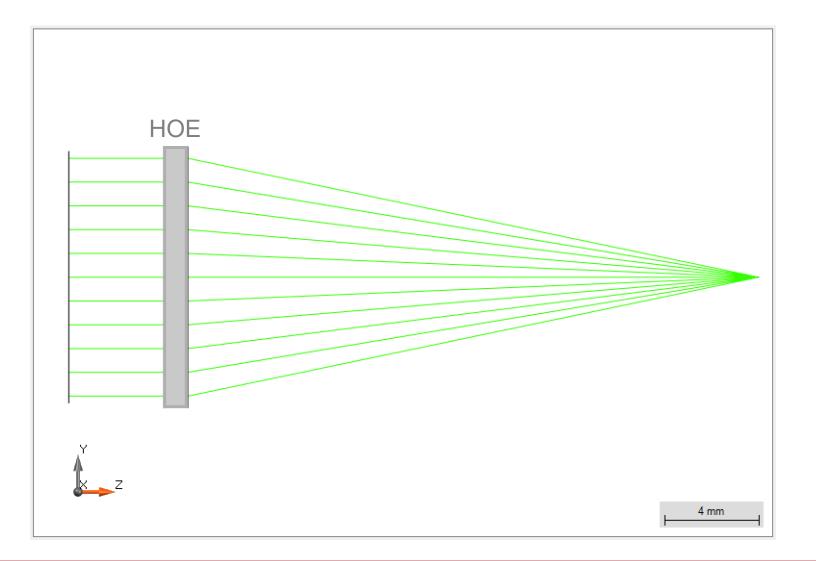


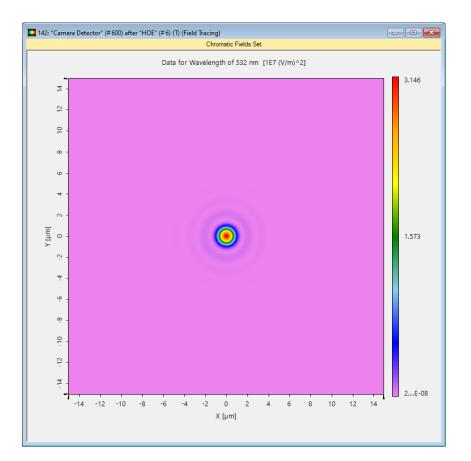
### **Structural Design Focusing (NA = 0.2): HOE**

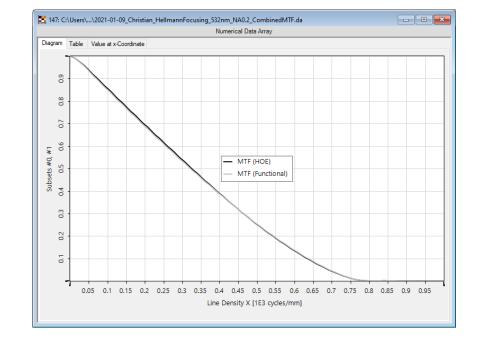


#### HOE surface: 8 Levels

### Focusing (NA = 0.2) HOE: Ray Tracing



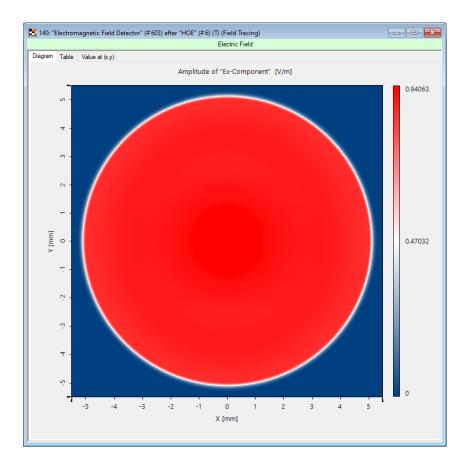


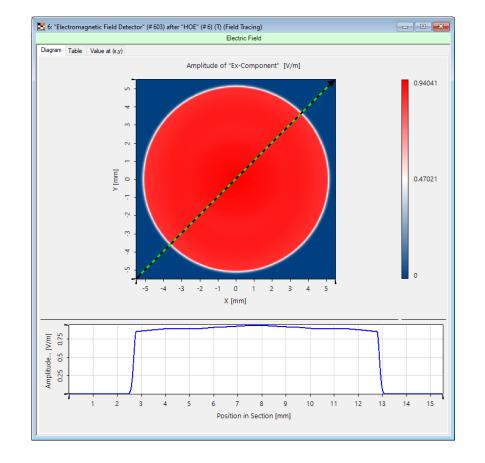


Field in Focus (False Color)

#### MTF

Efficiency: 78.99% (Efficiency after First Plane: 96.5%)

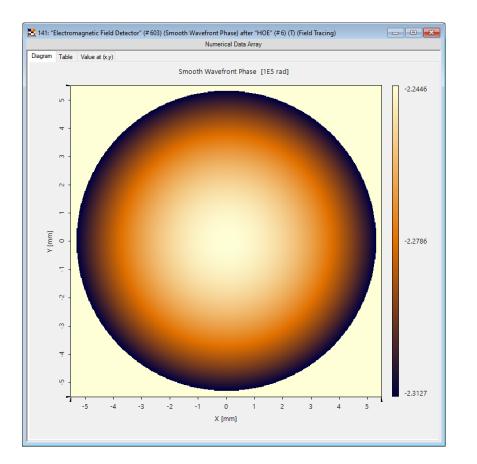




#### Amplitude after HOE

Amplitude after HOE

# Focusing (NA = 0.2) HOE: Ray Tracing

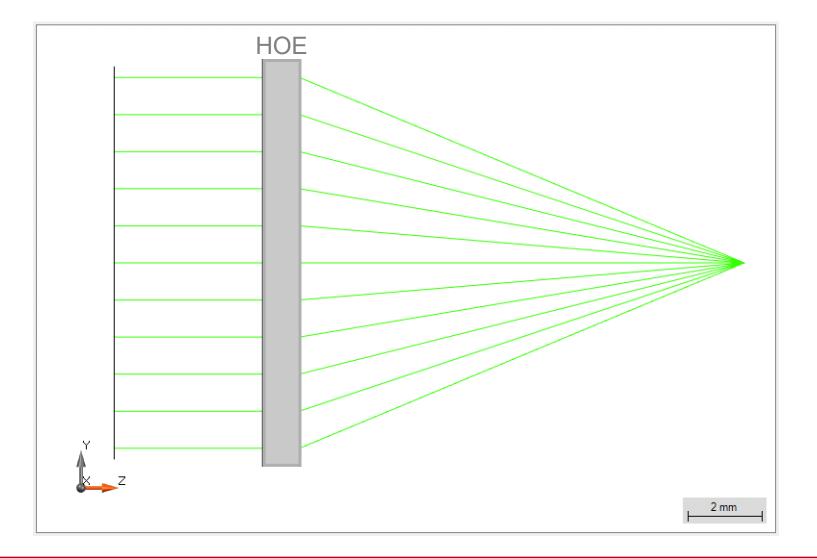


🔀 6: "Electromagnetic Field Detector" (# 603) after "HOE" (# 6) (T) (Field Tracing) Electric Field Diagram Table Value at (x.y) '15Phase of "Ex-Component" [rad] 4 ŝ 2 0 [m -0.20481  $\geq$ 2 ņ 4 -0.40962 7 -5 -4 -3 -2 -1 0 1 2 3 4 5 X [mm]

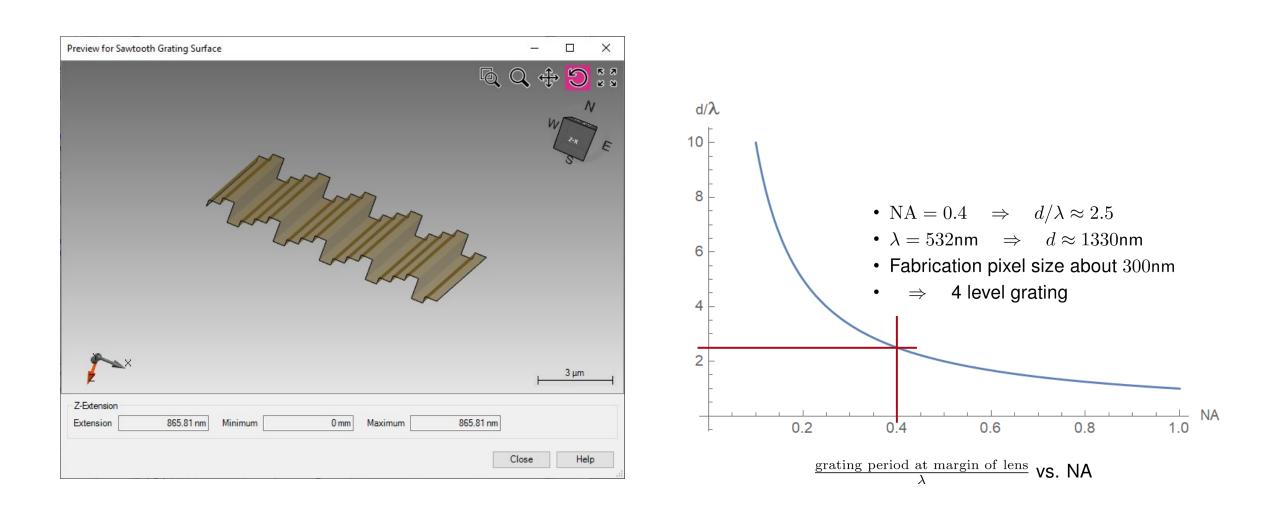
#### Wavefront Error after HOE

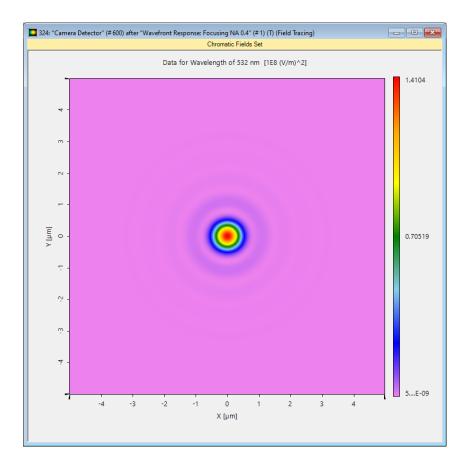
Wavefront after HOE

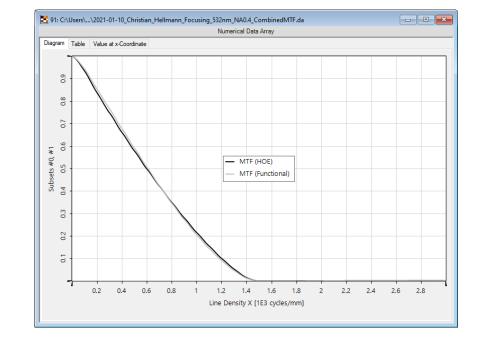
## Focusing (NA = 0.4) HOE: Ray Tracing



## **Grating Profile for HOE: Four Level**



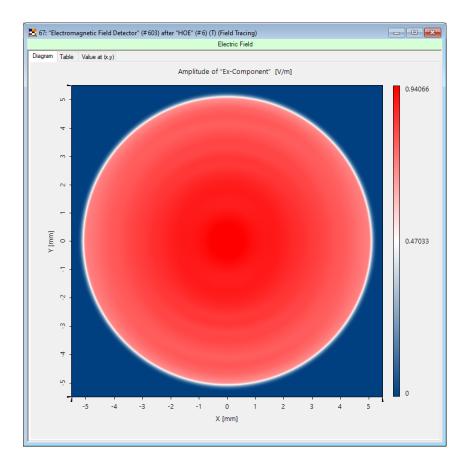


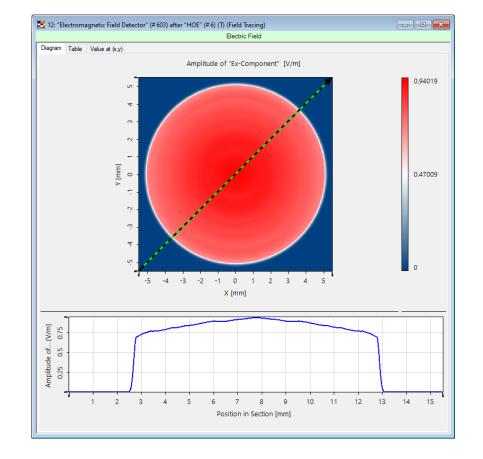


Energy Density in Focus (False Color)

MTF

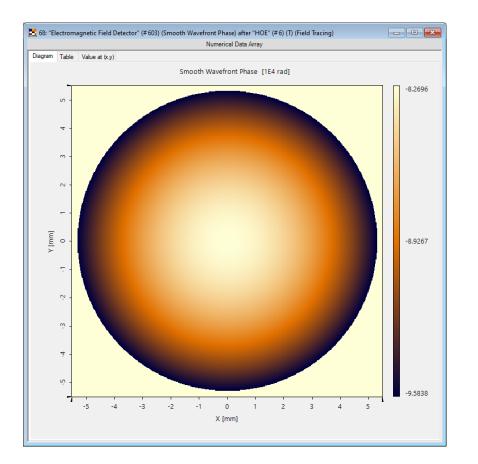
Efficiency: 65.17% (efficiency after first plane: 96.5%)





#### Amplitude after HOE

#### Amplitude after HOE

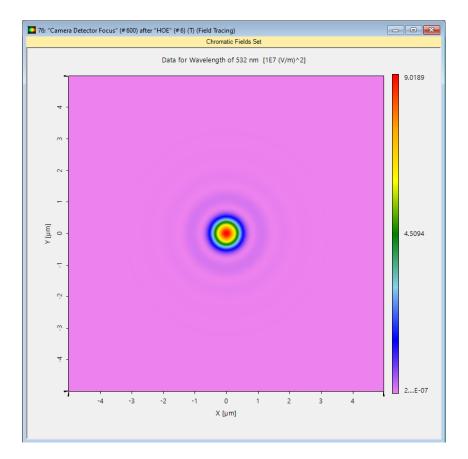


12: "Electromagnetic Field Detector" (# 603) after "HOE" (# 6) (T) (Field Tracing) Electric Field Diagram Table Value at (x.y) '13Phase of "Ex-Component" [rad] 0.06702 4 0 0 [mm] > 2 ņ 4 . Ю -0.40458 -5 -4 -3 -2 -1 0 2 3 4 5 X [mm]

#### Wavefront Error after HOE

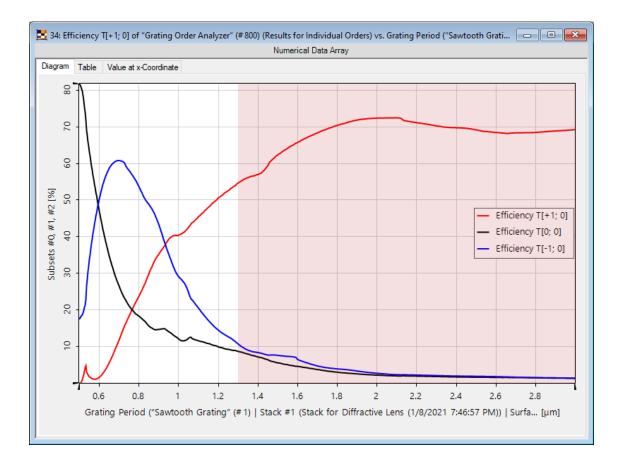
#### Wavefront after HOE

# Focusing (NA = 0.4) HOE: Field Tracing $\rightarrow$ -1<sup>st</sup>, 0<sup>th</sup>, +1<sup>st</sup>

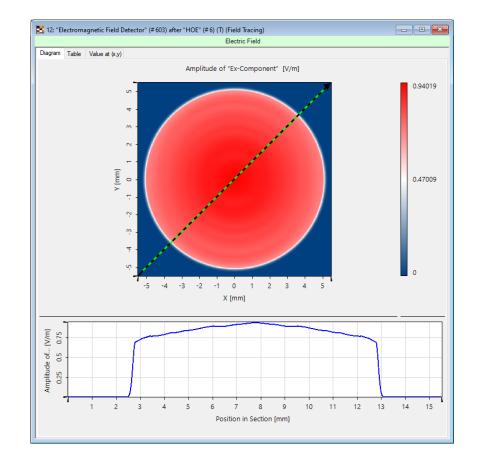


Order HOE	Efficiency after HOE
-3	0.98%
-2	3.51%
-1	5.31%
0	3.46%
1	65.17%
2	6.17%
3	0.31%

Energy Density in Focus (False Color)

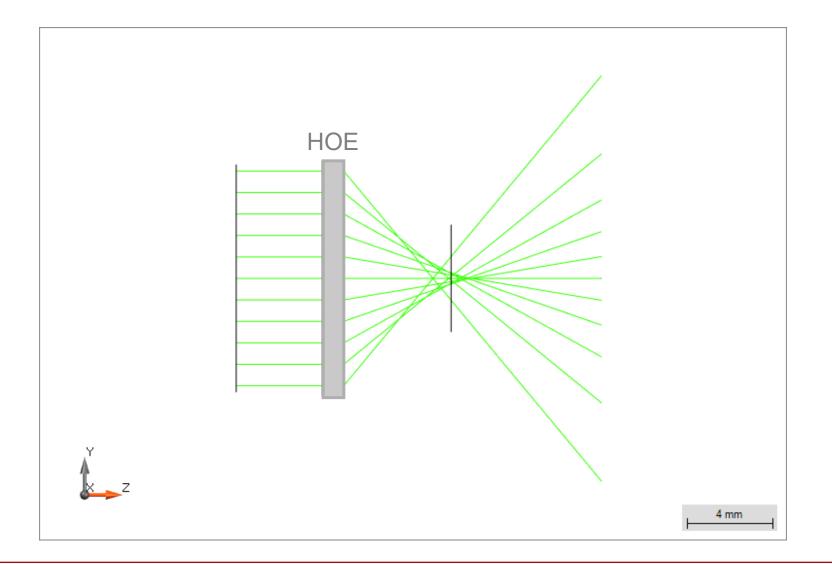


#### Efficiencies vs. Period

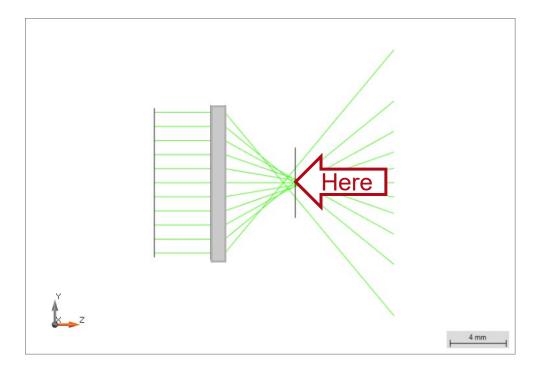


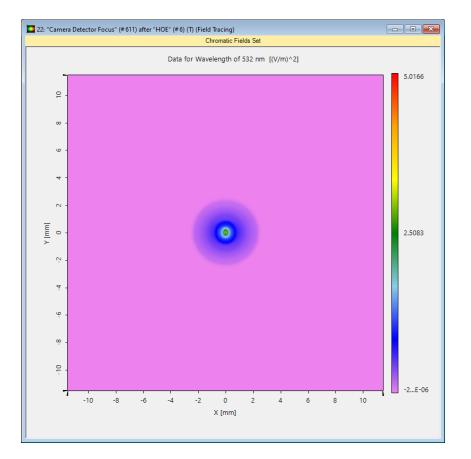
#### Amplitude after HOE

# Focusing (NA = 0.4) HOE: Ray Tracing $\rightarrow$ 2<sup>nd</sup> Order



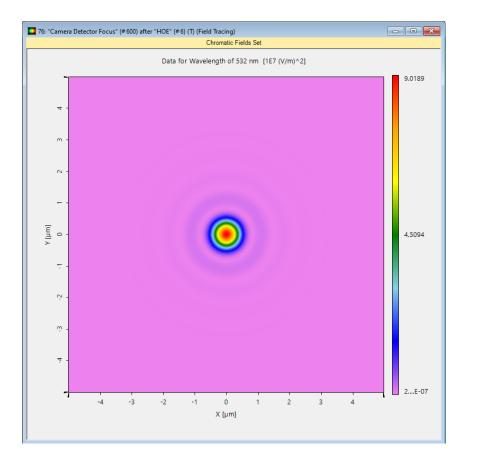
# Focusing (NA = 0.4) HOE: Field Tracing $\rightarrow$ 2<sup>nd</sup> Order





Intermediate focus after 5mm

### Focusing (NA = 0.4) HOE: Field Tracing $\rightarrow$ -1<sup>st</sup>, 0<sup>th</sup>, +1<sup>st</sup>



279: D:\OneDrive\...\2021-01-10\_Christian\_Hellmann\_Focusing\_532nm\_NA0.4\_CombinedMTF\_wHigherOrders.da Numerical Data Array Diagram Table Value at x-Coordinate 0.9 0.8 0.7 ŧ 0.6 #2, MTF (HOE with Higher Orders) Ô, 0.5 MTF (Functional) Subsets — MTF (HOE) 0.4 0.3 0.2 0.1 0.2 0.4 0.6 0.8 1 1.2 1.4 1.6 1.8 2 2.2 2.4 2.6 2.8 Line Density X [1E3 cycles/mm]

Energy Density in Focus (False Color)

MTF

### **Design Workflow in VirtualLab Fusion**

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

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#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

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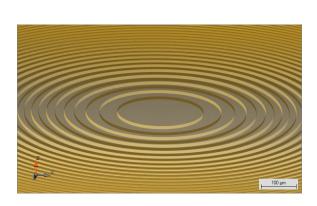
Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

### **Structure of Webinar**

- Why physical optics?
- Optical design in physical optics terms
- Diffractive Optical Elements (DOE)
  - Design
  - Modeling
  - Fabrication data
- Design examples

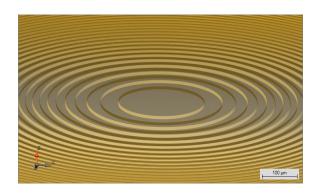




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- Design examples





### **HOE Fabrication Data Export**

Edit Holographic Optical Element Component	×
Solid Channel Operator Diffractive Structure Model   O Idealized Grating Structure <ul> <li>Real Structure</li> <li>Design Wavelength</li> <li>Height Scaling Factor</li> <li>Image: Structure</li> <li>Use Profile Quantization</li> <li>Number of Height Levels</li> <li>Use Profile Quantization</li> <li>Orders for Simulation</li> <li>Orders for Simulation</li> <li>Order</li> <li>Add Order</li> <li>Remove Order</li> </ul>	Structure export for quantized height structures can be performed by clicking on the corresponding button in the edit dialog
Channel Configuration	of the HOE.

### **HOE Fabrication Data Export**

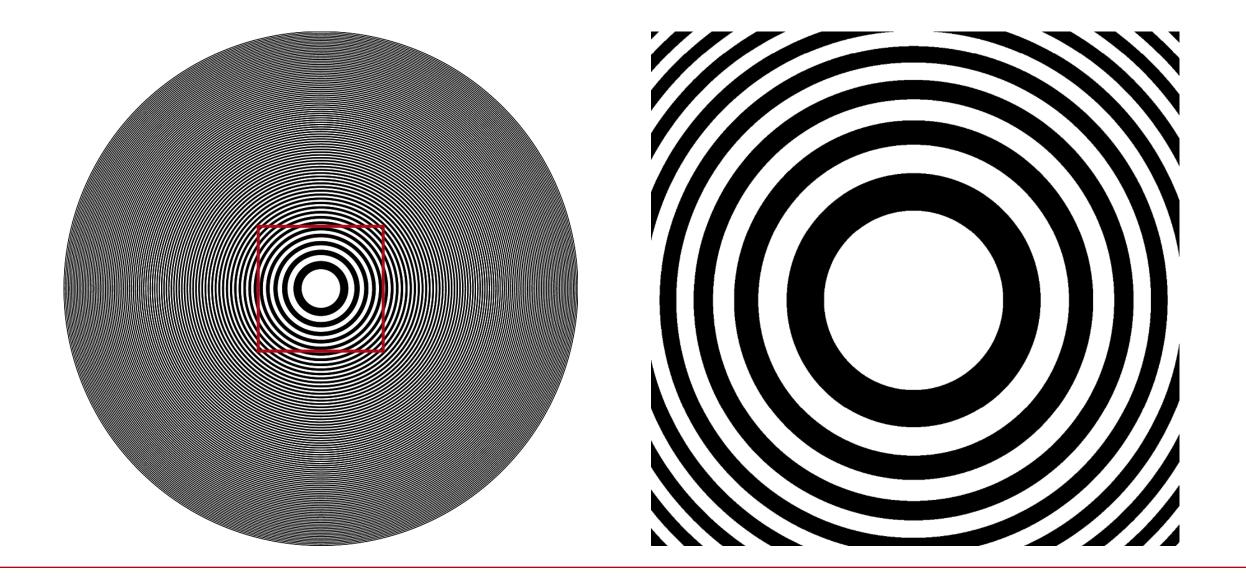
Configure Fabrication Export X
Output File(s)       D:\FabricationData\       Select         Path       D:\FabricationData\       Select         File Names (Without Extension)       Export_Data .*
Mask Decomposition Settings Invert File Name Convention Ascending ~ 1
Export Settings Export Type
Sampling Distance 20 µm x 20 µm
Export as
Bitmap (*.bmp) ASCII (*.txt) Plain Text (*.ptf)
CIF (*.cif) GDSII (*.gds)
Summary Files
ASCII file (*.txt) XML file (*.xml)
HTML file (*.html)
▶ Go!
Dereview Close

- Fabrication export supports specification of
  - Target directory
  - Parameters for mask decomposition
  - Pixelated or polygon data export (+ export accuracy parameters)
  - File format (supported formats: bitmap, text files, GDISII or CIF)

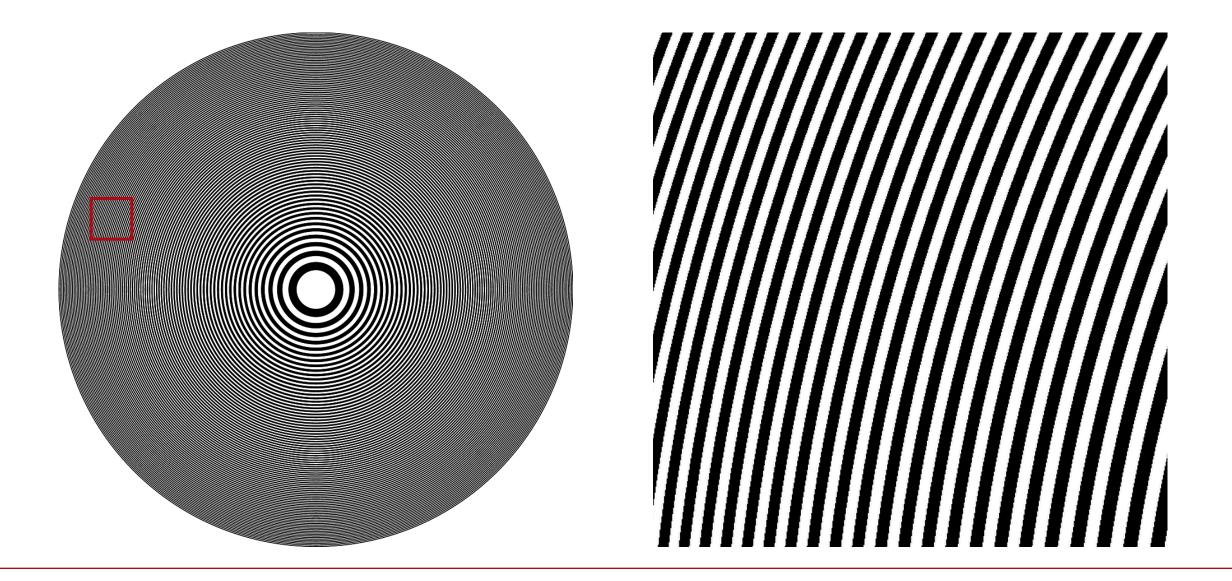
### **HOE Fabrication Data Export – Sample Data Pixelated Bitmap**

Configure Fabrication Export X	
Output File(s)       D:\FabricationData\       Select         Path       D:\FabricationData\       Select         File Names (Without Extension)       Export_Data       .*	
Mask Decomposition Settings         Invert       File Name Convention         Ascending       ✓	
Export Settings Export Type Pixelated Data Export O Polygon Data Export Sampling Distance 500 nm x 500 nm	
Export as  Export as  ASCII (*.txt)  Plain Text (*.ptf)  CIF (*.cif)  GDSII (*.gds)	
Summary Files ASCII file (*.txt) XML file (*.xml)	
HTML file (*.html) Rich Text Format (*.rtf)	
Deview Close	

### **HOE Fabrication Data Export – Sample Data Pixelated Bitmap**

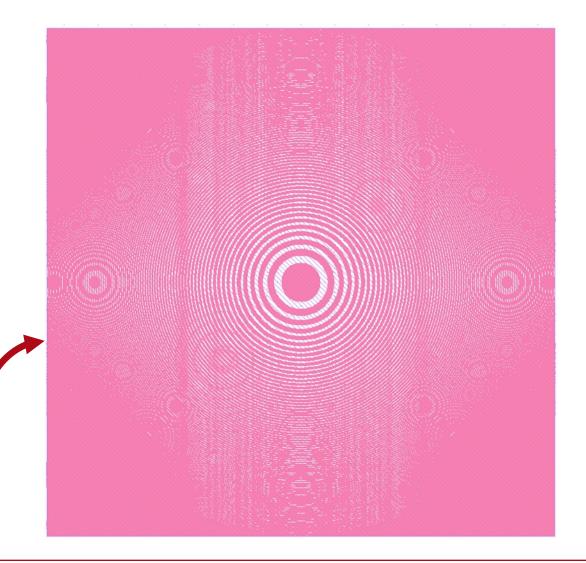


### **HOE Fabrication Data Export – Sample Data Pixelated Bitmap**

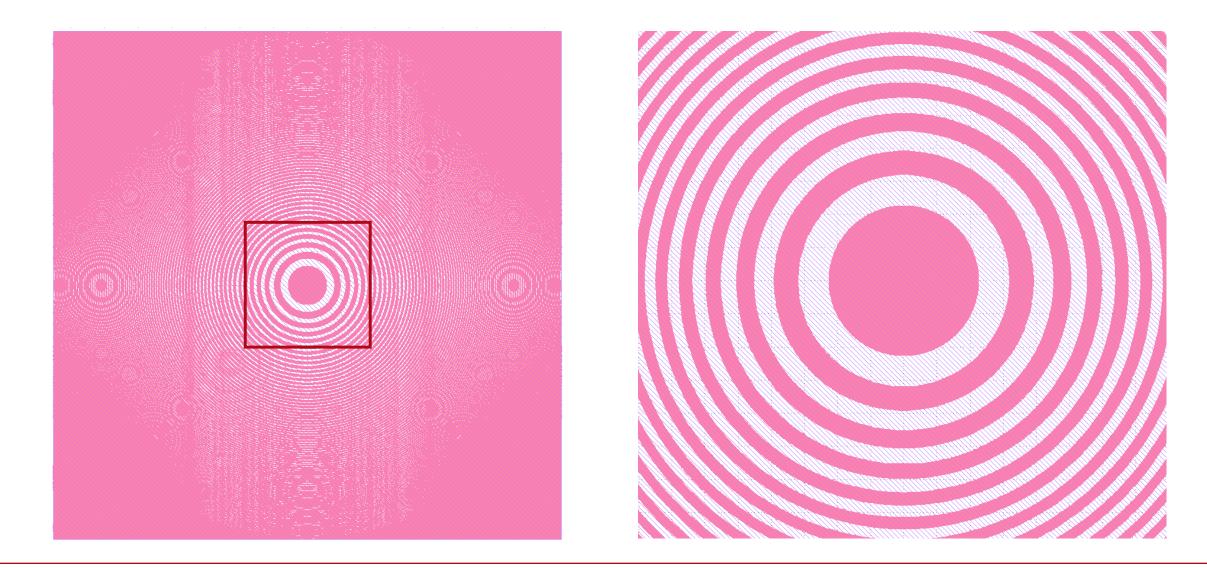


### **HOE Fabrication Data Export – Sample Data Pixelated GDSII**

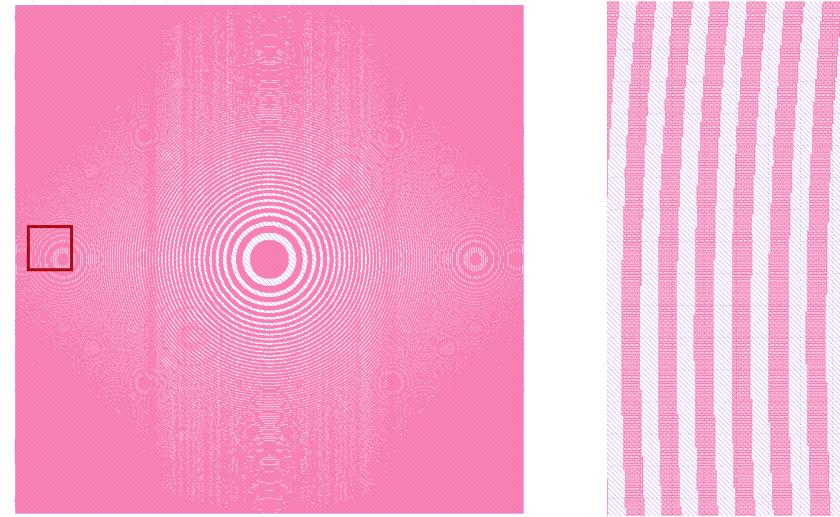
onfigure Fabrication Export	×
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HTML file (*.html)	Rich Text Format (*.rtf)
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D Preview	Close

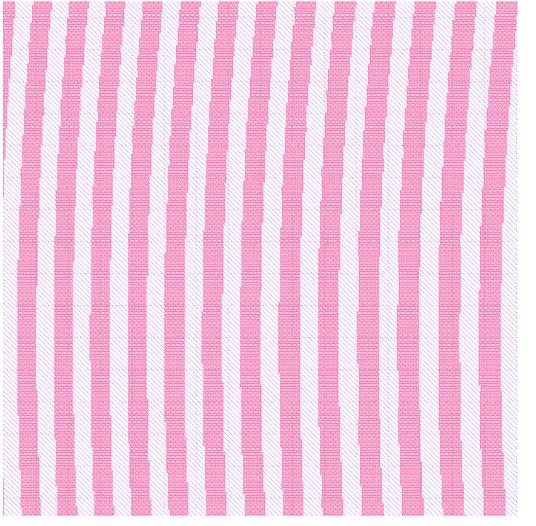


### **HOE Fabrication Data Export – Sample Data Pixelated GDSII**



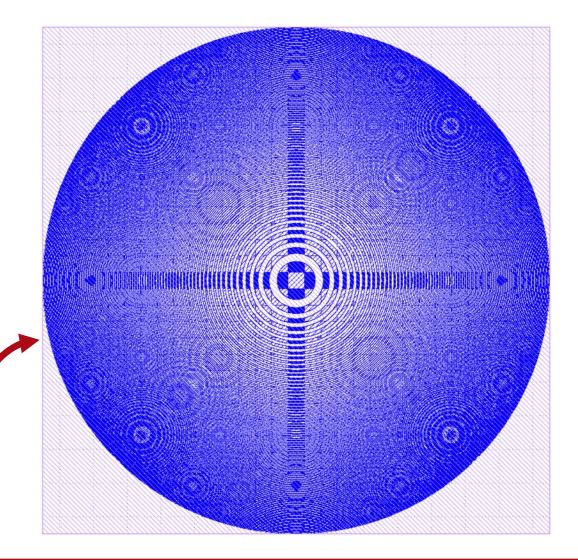
### **HOE Fabrication Data Export – Sample Data Pixelated GDSII**



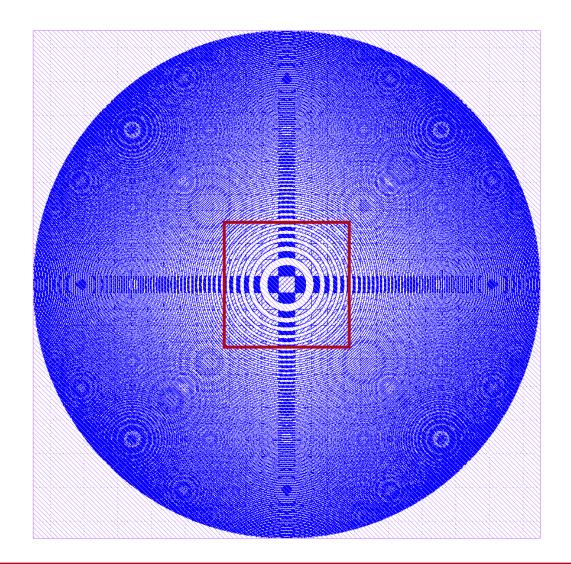


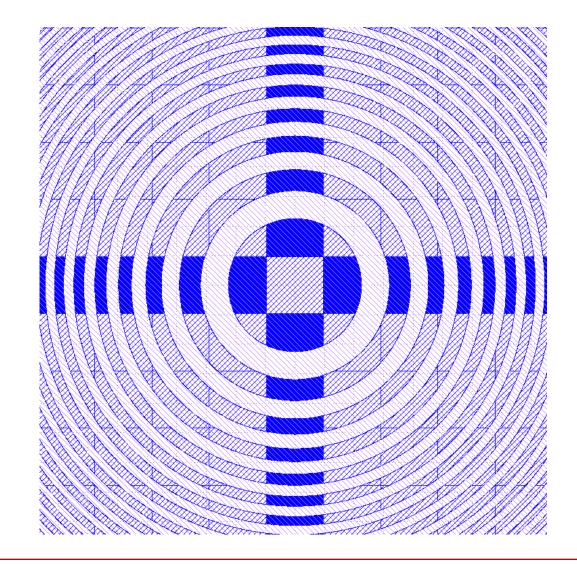
### **HOE Fabrication Data Export – Sample Data Polygon CIF**

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File Names (Without Extension)	Export_Data .*
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Export Settings	
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Polygon Detection Accuracy (i)	500 - Accuracy (λ/i) = 1.064 nm
Maximum Number of Points per	Polygon 8000 ਦ
Export as	
CIF (*.cif)	GDSII (*.gds)
Summary Files	
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HTML file (*.html)	Rich Text Format (*.rtf)
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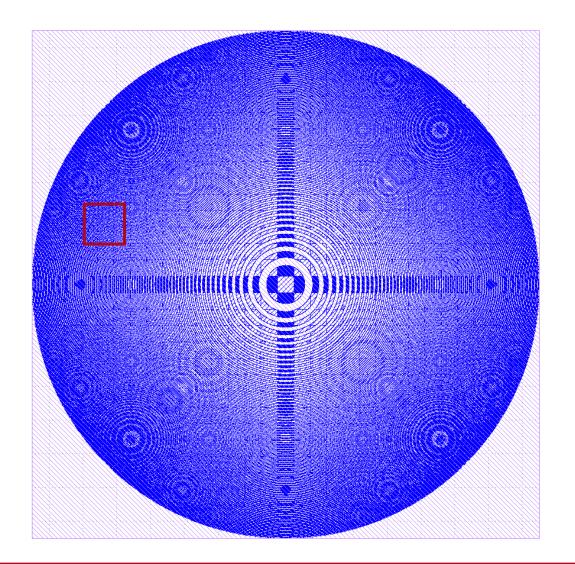


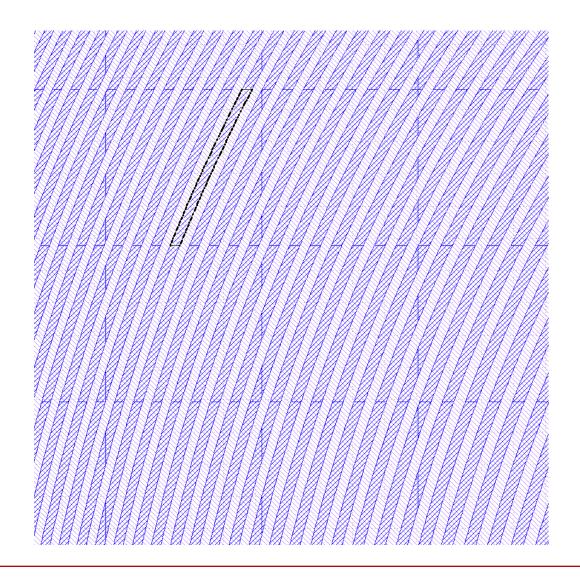
### HOE Fabrication Data Export – Sample Data Polygon CIF





### HOE Fabrication Data Export – Sample Data Polygon CIF

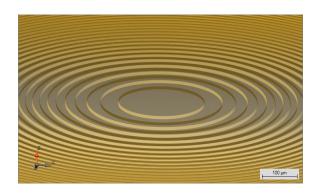




### **Structure of Webinar**

- Why physical optics?
- Optical design in physical optics terms
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- Design examples



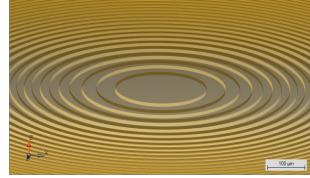


### **Structure of Webinar**

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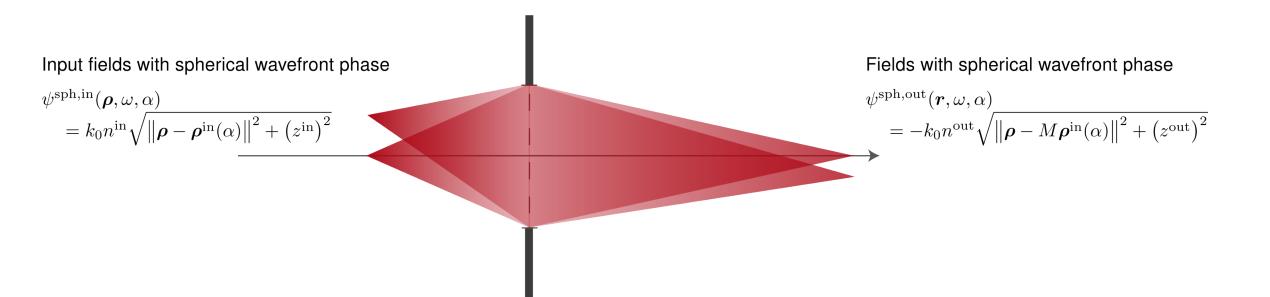






### Imaging with one component

### **Imaging with One Component: Scenario**



Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

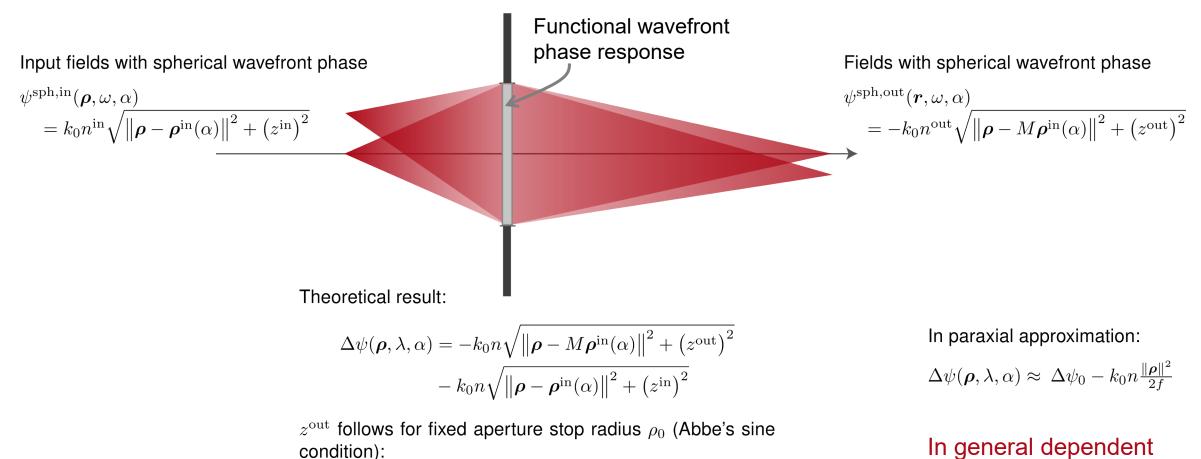
Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

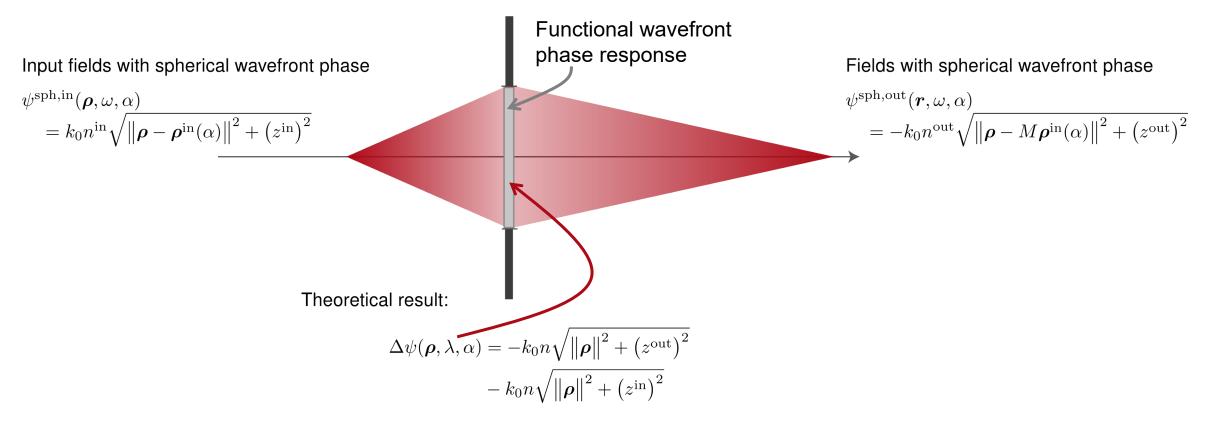
### **Imaging with One Component: Functional Design**



of input field

$$z^{\text{out}} = \sqrt{(z^{\text{in}}M)^2 + \rho_0^2 (M^2 - 1)}$$

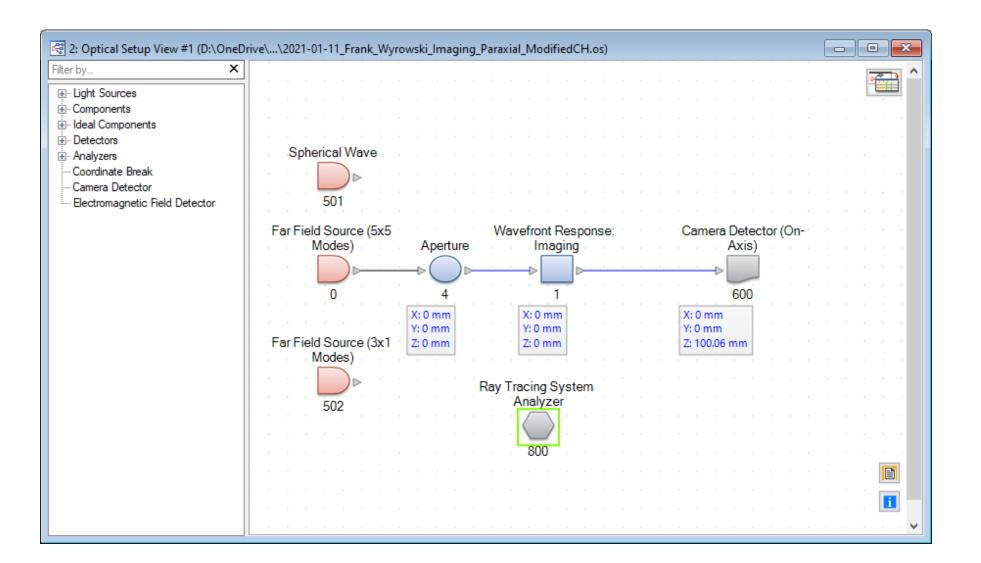
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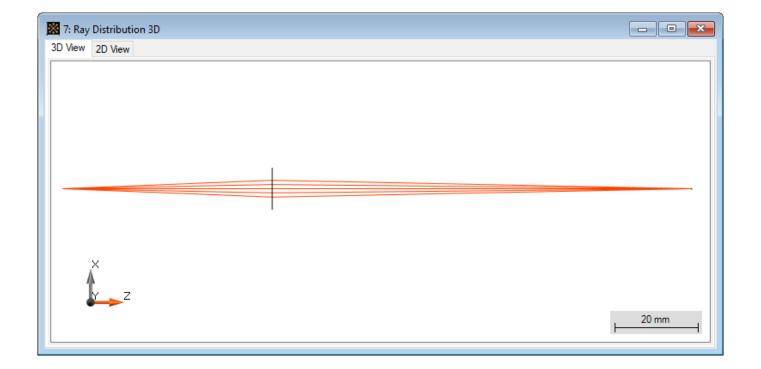
 $z^{\text{out}}$  follows for fixed aperture stop radius  $\rho_0$  (Abbe's sine condition):

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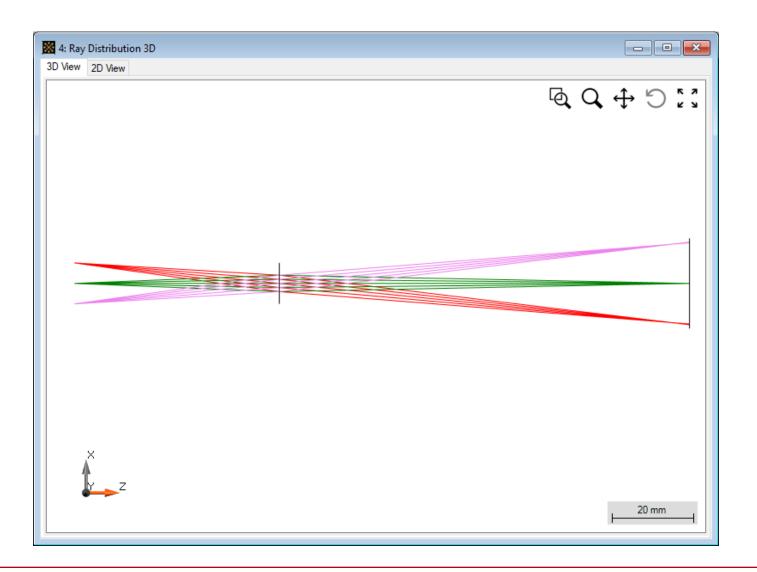
### **Functional Design for Imaging: NA 0.02**



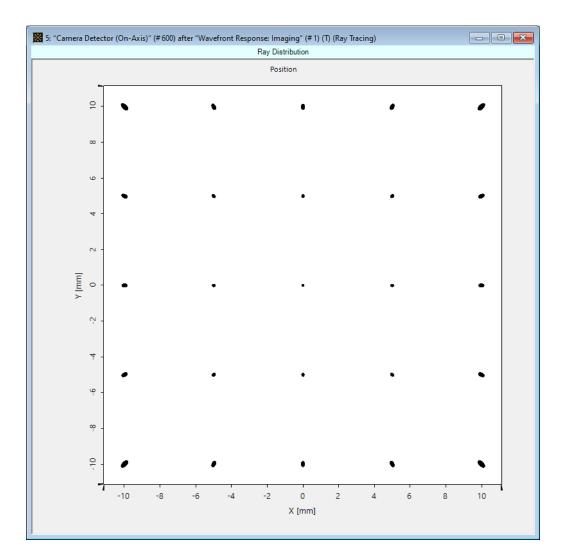
### **Functional Design for Imaging (NA 0.02): Ray Tracing**



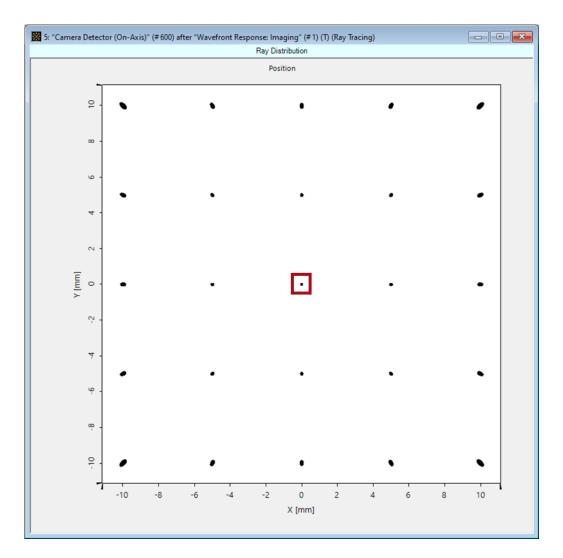
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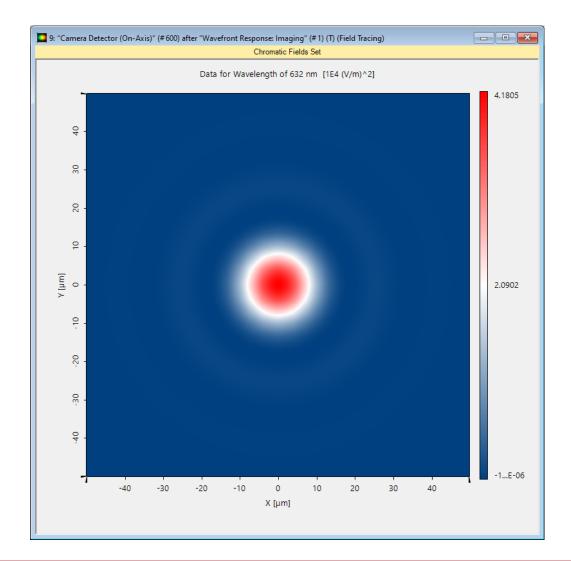


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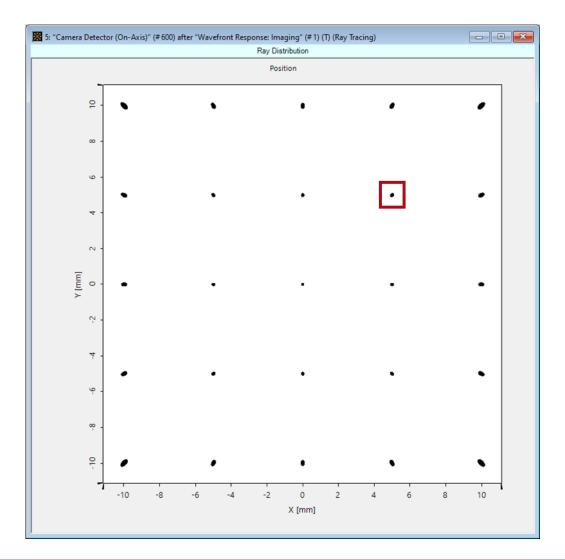


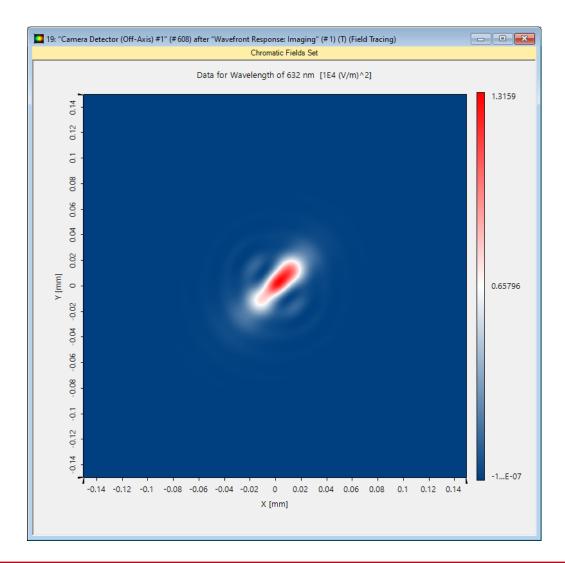
### **Functional Design for Imaging (NA 0.02): Field Tracing**



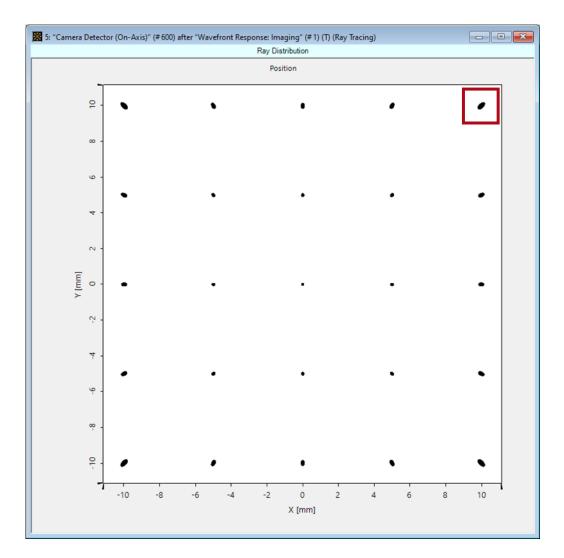


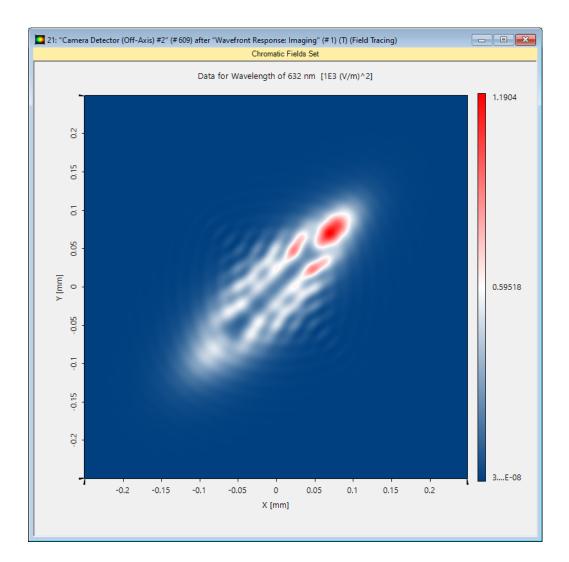
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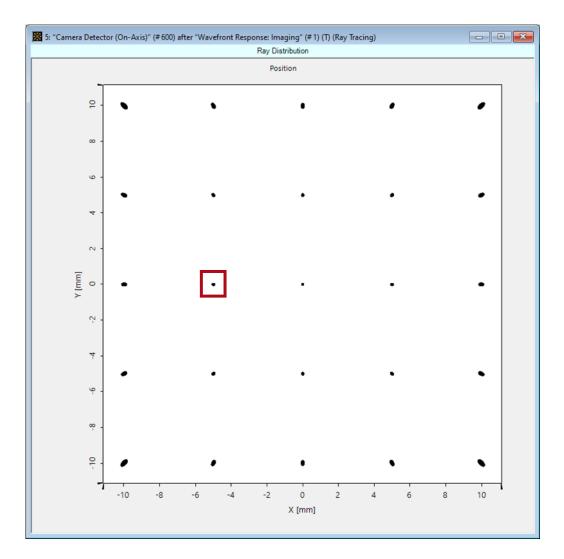


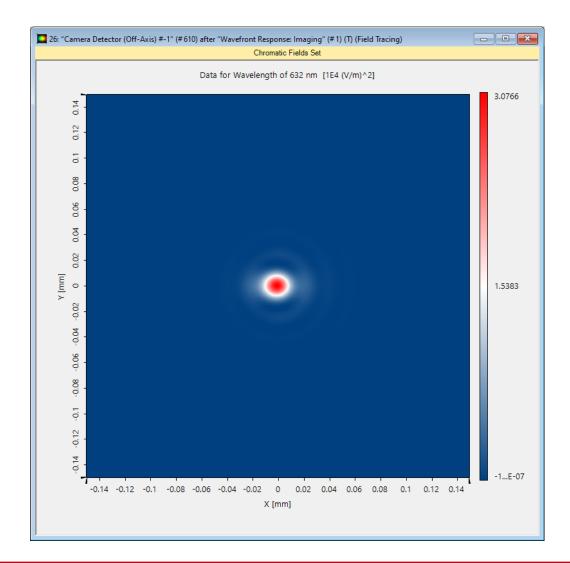


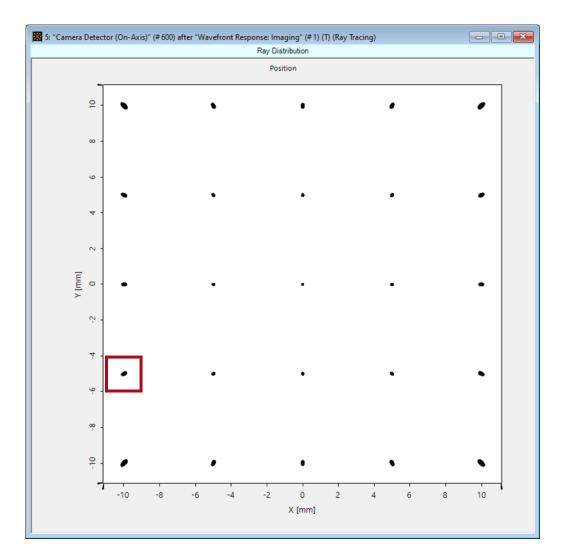
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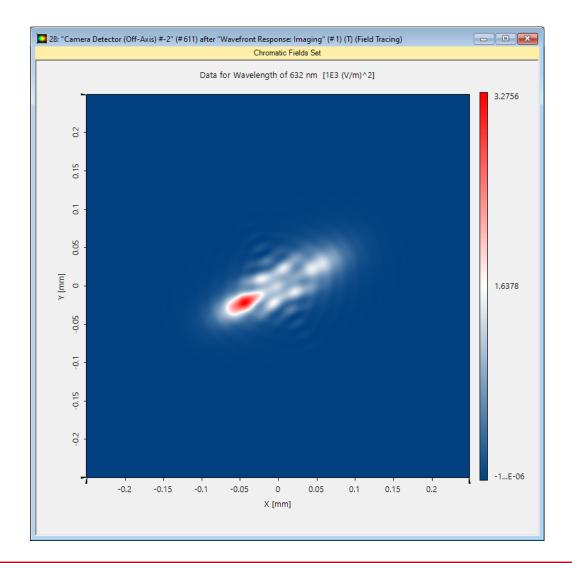


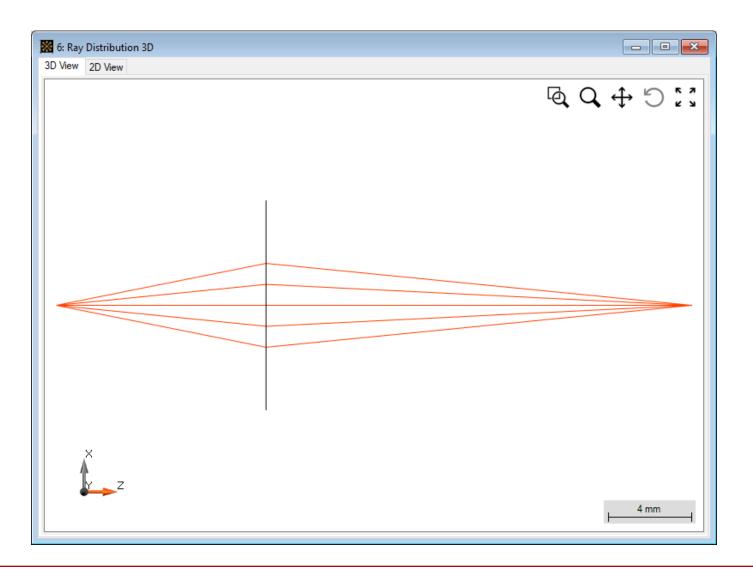


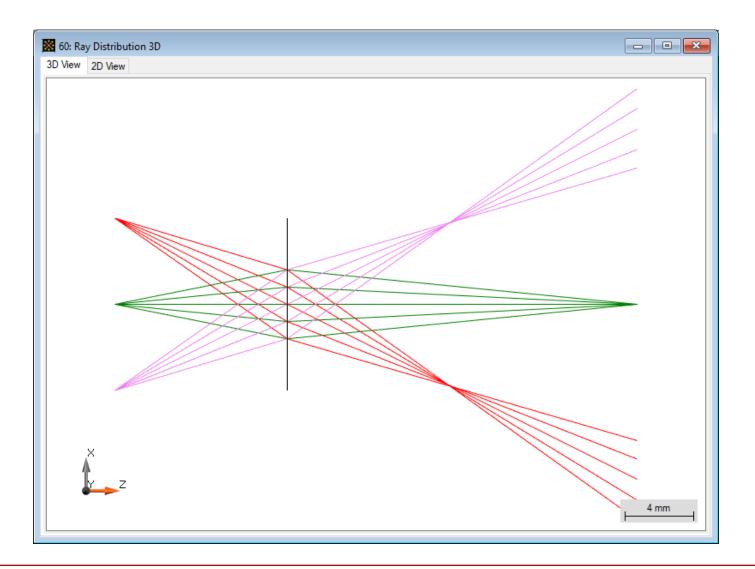


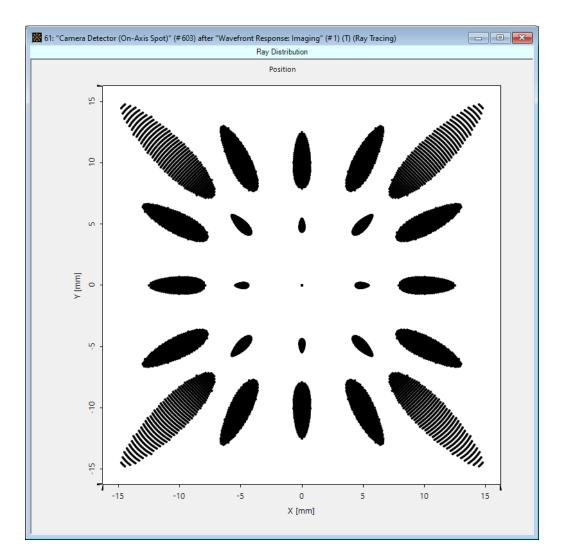


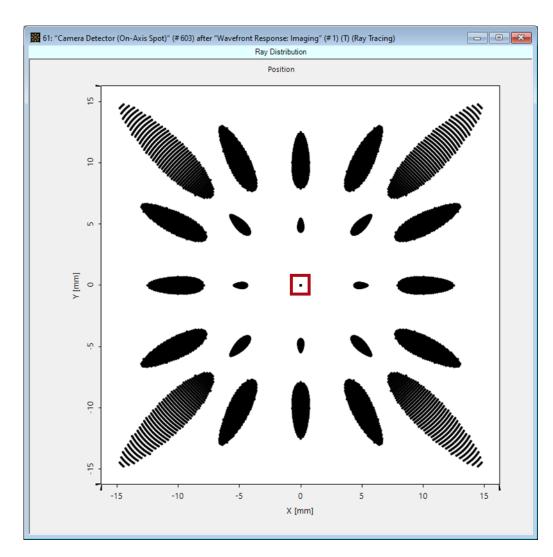


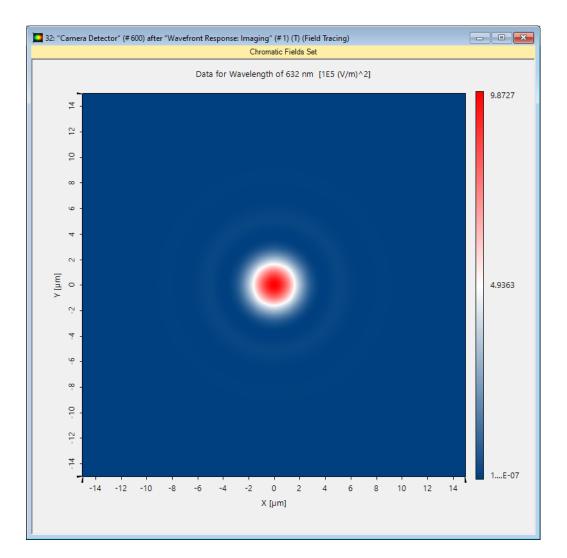


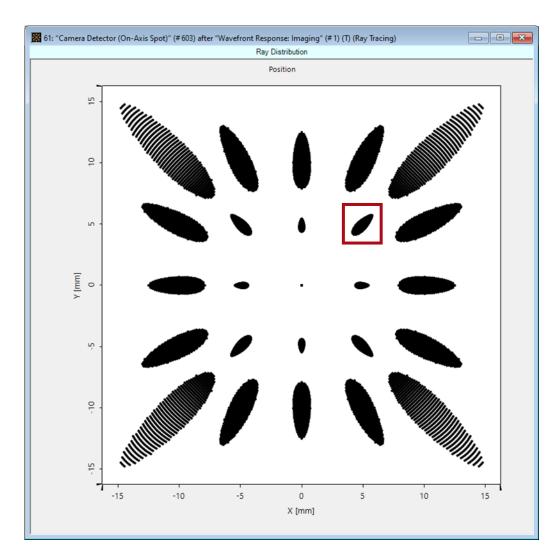


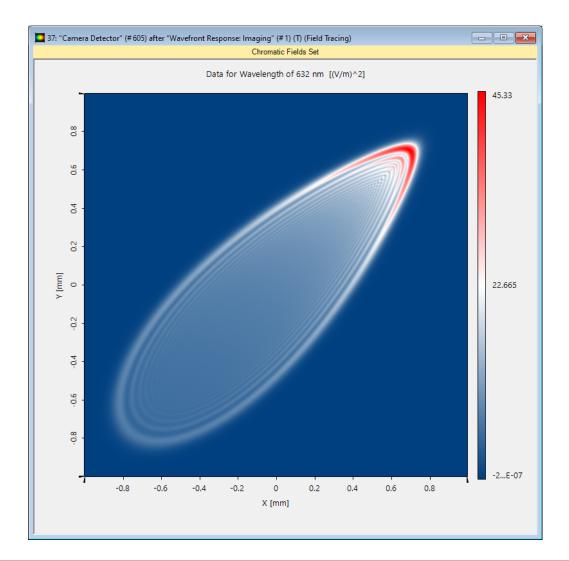


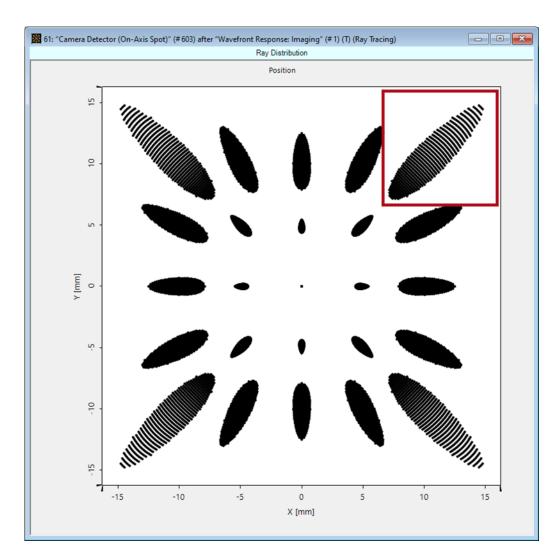


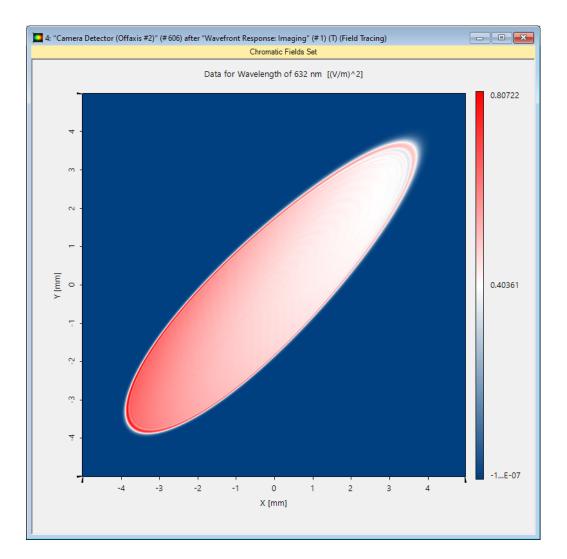


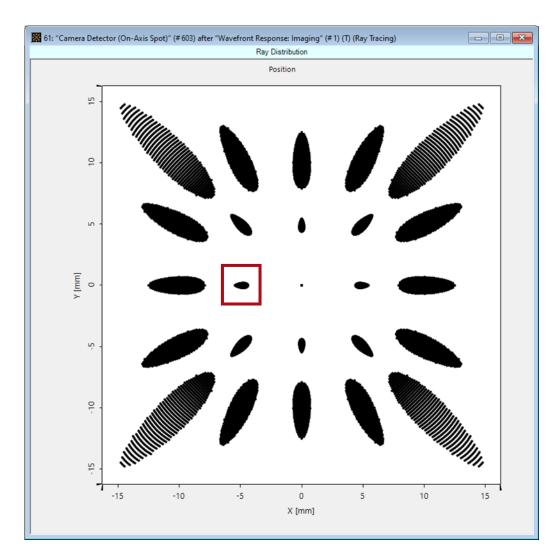


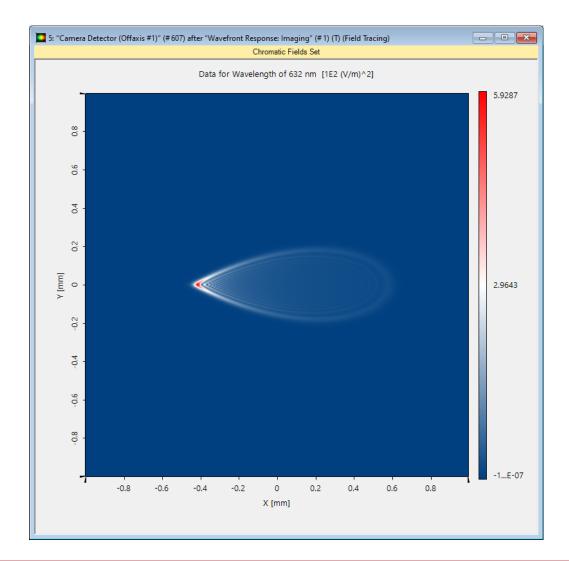


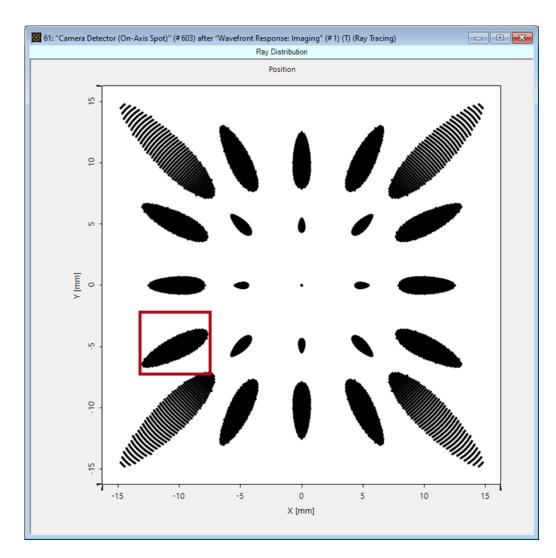


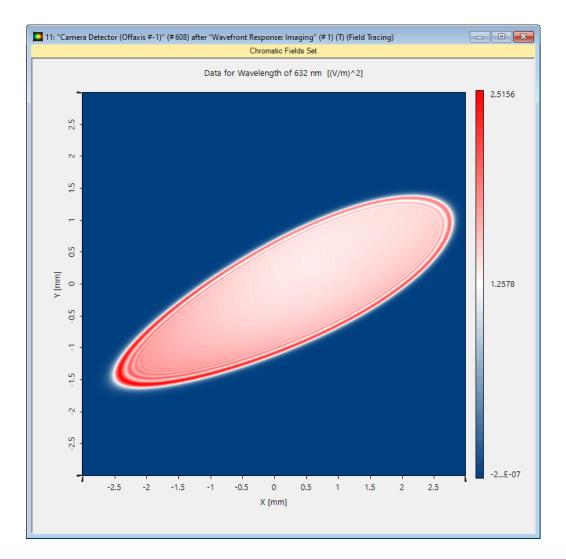




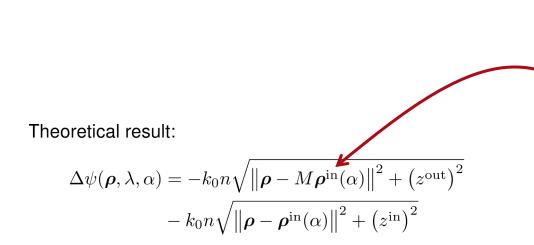






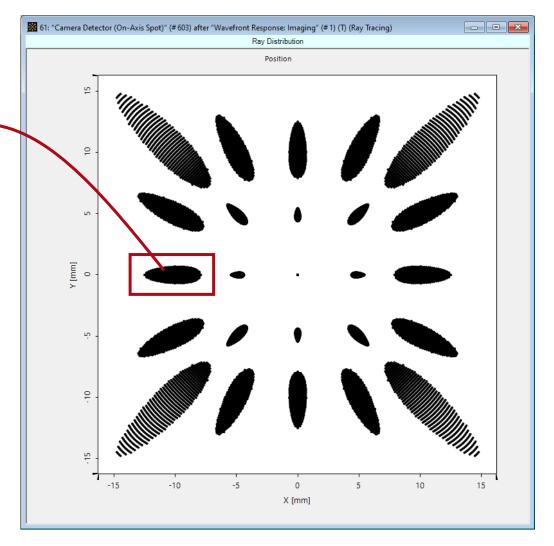


## **Functional Design for Imaging (NA 0.1): Off-Axis Mode**

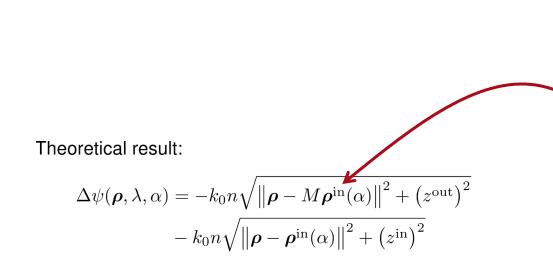


 $z^{\rm out}$  follows for fixed aperture stop radius  $\rho_0$  (Abbe's sine condition):

$$z^{\text{out}} = \sqrt{(z^{\text{in}}M)^2 + \rho_0^2 (M^2 - 1)}$$

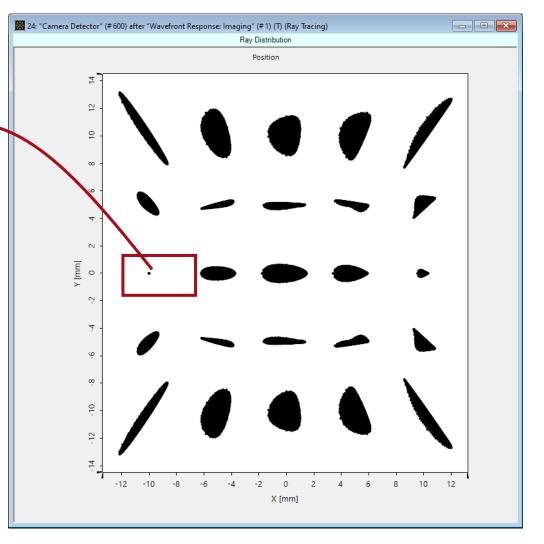


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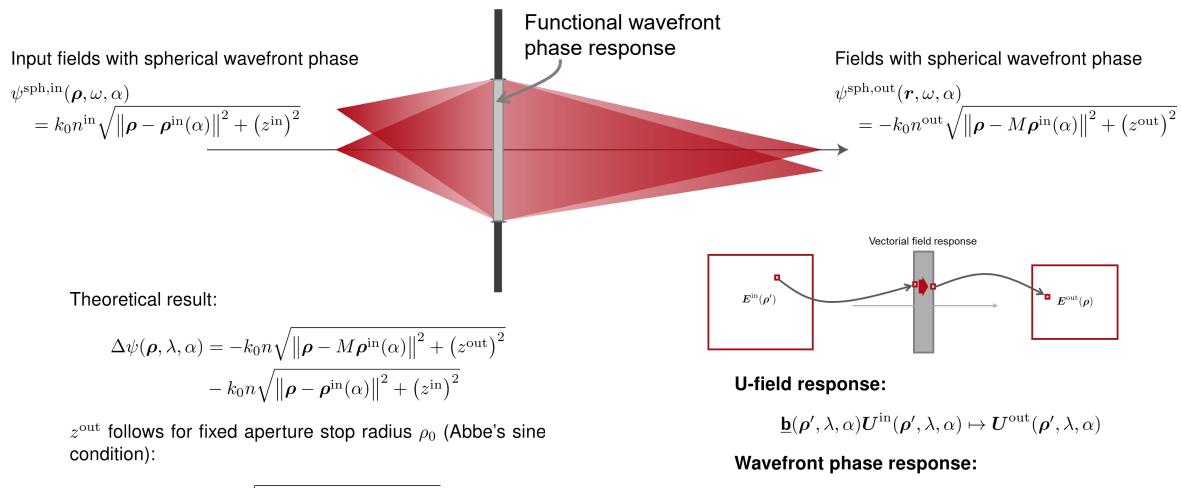


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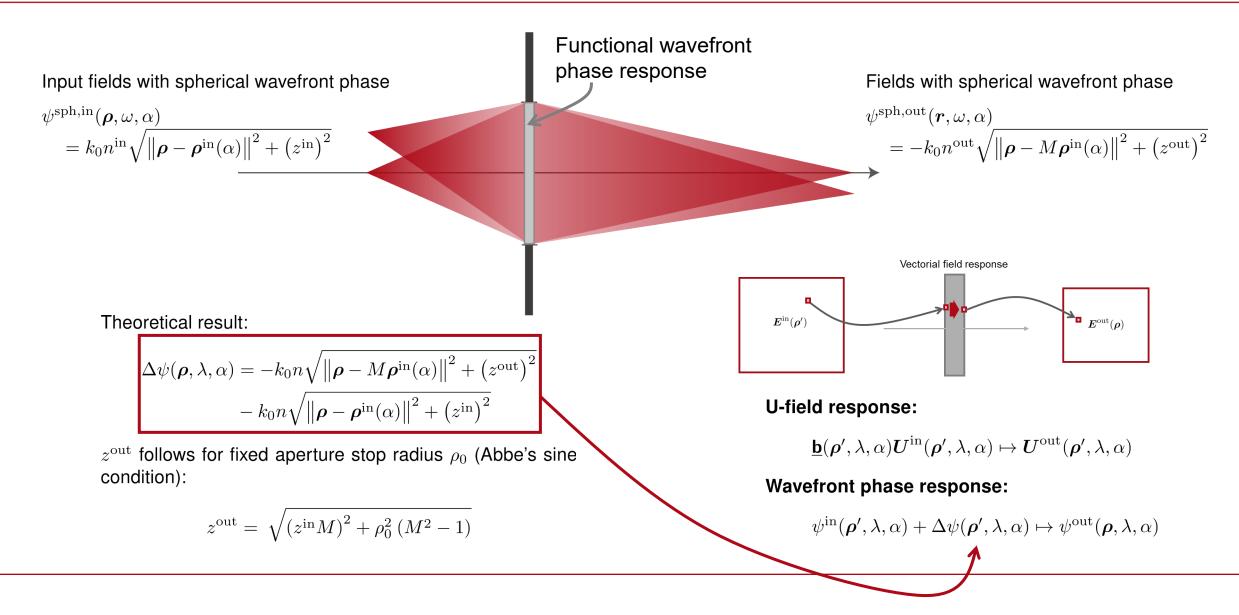
## **Imaging with One Component: Structural Design**



 $\psi^{\text{in}}(\rho',\lambda,\alpha) + \Delta \psi(\rho',\lambda,\alpha) \mapsto \psi^{\text{out}}(\rho,\lambda,\alpha)$ 

$$z^{\text{out}} = \sqrt{(z^{\text{in}}M)^2 + \rho_0^2 (M^2 - 1)}$$

## **Imaging with One Component: Structural Design**



# FUNCTIONAL DESIGN

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#### STRUCTURAL DESIGN

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# MODELING & EVALUATION

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#### FURTHER OPTIMIZATION

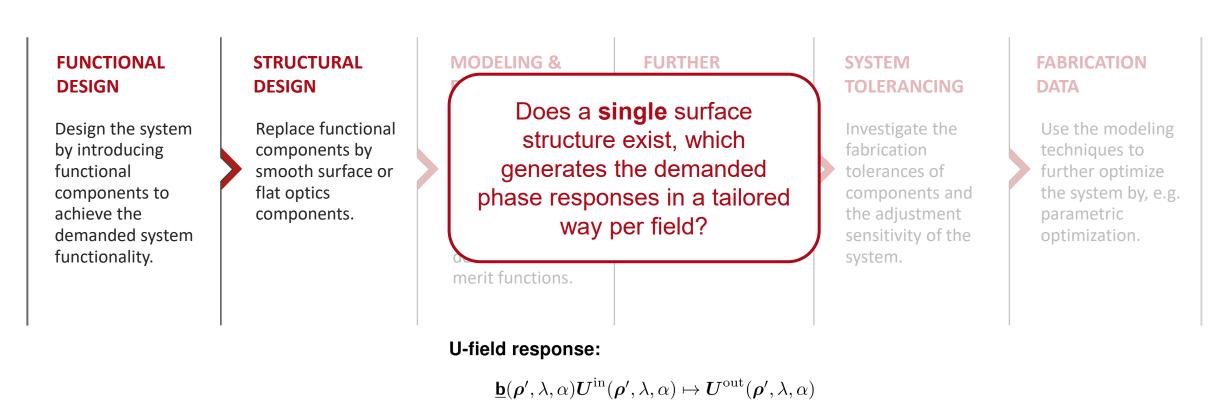
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#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.



Wavefront phase response:

 $\psi^{\mathrm{in}}(\boldsymbol{\rho}',\lambda,\alpha) + \Delta\psi(\boldsymbol{\rho}',\lambda,\alpha) \mapsto \psi^{\mathrm{out}}(\boldsymbol{\rho},\lambda,\alpha)$ 

FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

#### **MODELING &**

FURTHER

Meta surfaces may offer a chance for a tailored wavefront phase response to some extent. But still ongoing R&D and final answer not available.

merit functions.

#### U-field response:

 $\underline{\mathbf{b}}(\boldsymbol{\rho}',\boldsymbol{\lambda},\alpha)\boldsymbol{U}^{\mathrm{in}}(\boldsymbol{\rho}',\boldsymbol{\lambda},\alpha)\mapsto\boldsymbol{U}^{\mathrm{out}}(\boldsymbol{\rho}',\boldsymbol{\lambda},\alpha)$ 

Wavefront phase response:

 $\psi^{\rm in}(\boldsymbol{\rho}',\boldsymbol{\lambda},\boldsymbol{\alpha}) + \Delta\psi(\boldsymbol{\rho}',\boldsymbol{\lambda},\boldsymbol{\alpha}) \mapsto \psi^{\rm out}(\boldsymbol{\rho},\boldsymbol{\lambda},\boldsymbol{\alpha})$ 

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Design the system by introducing functional components to achieve the demanded system functionality. STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

#### **MODELING &**

FURTHER

However, we know for sure: A combination of surfaces can solve the problem well. Flat optics adds extra flexibility and options to further improve such solutions!

merit functions.

#### **U-field response:**

 $\underline{\mathbf{b}}(\boldsymbol{\rho}',\boldsymbol{\lambda},\alpha)\boldsymbol{U}^{\mathrm{in}}(\boldsymbol{\rho}',\boldsymbol{\lambda},\alpha)\mapsto\boldsymbol{U}^{\mathrm{out}}(\boldsymbol{\rho}',\boldsymbol{\lambda},\alpha)$ 

Wavefront phase response:

 $\psi^{\rm in}(\boldsymbol{\rho}',\lambda,\alpha) + \Delta\psi(\boldsymbol{\rho}',\lambda,\alpha) \mapsto \psi^{\rm out}(\boldsymbol{\rho},\lambda,\alpha)$ 

#### SYSTEM TOLERANCING

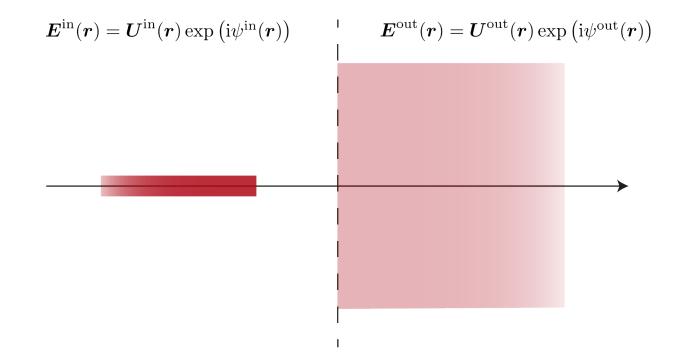
Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

# **Beam Expander**

### **Beam Expander: Scenario**



# FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

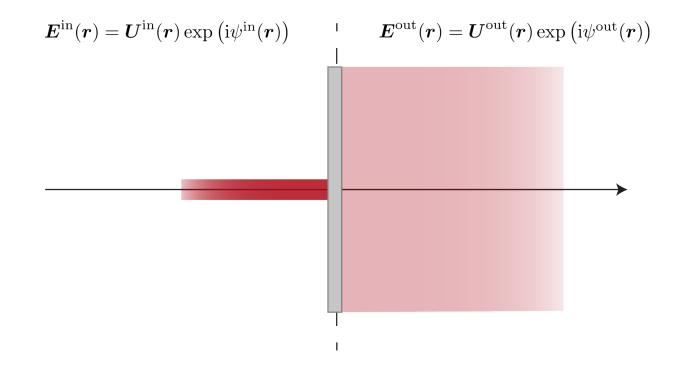
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Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

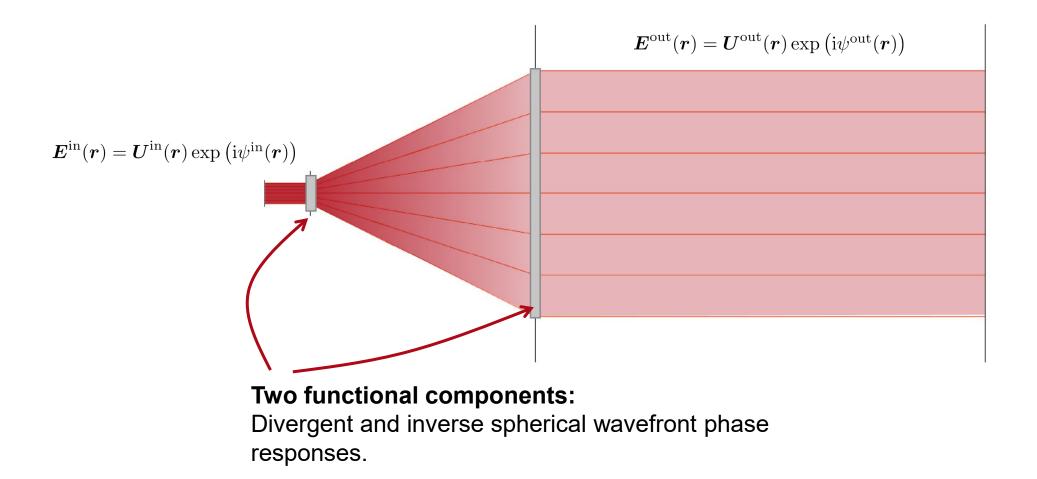
#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

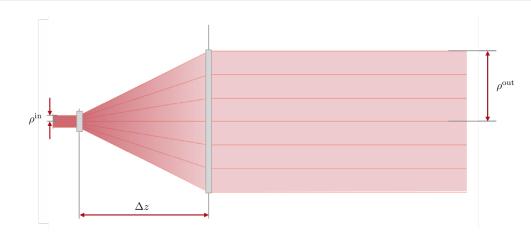
### **Beam Expander: Functional Design**



### **Beam Expander: Functional Design**



### **Beam Expander: Functional Design**



- Let assume the given parameters are the expander ratio  $\zeta = \rho^{\text{out}}/\rho^{\text{in}}$  and the distance  $\Delta z$ .
- A straightforward evaluation leads to the equations

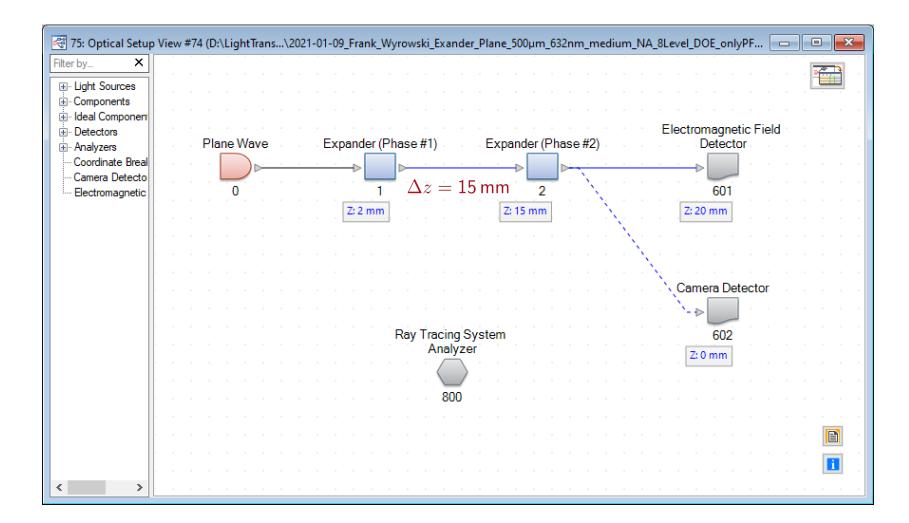
$$R_{1} = \frac{\Delta z}{(\zeta - 1)}$$
$$R_{2} = -(\Delta z + R_{1})$$
$$NA = \frac{n}{\sqrt{1 + (\Delta z / \rho^{\text{out}})^{2}}}$$

for radii of the first and second spherical wavefront phase response and the related NA .

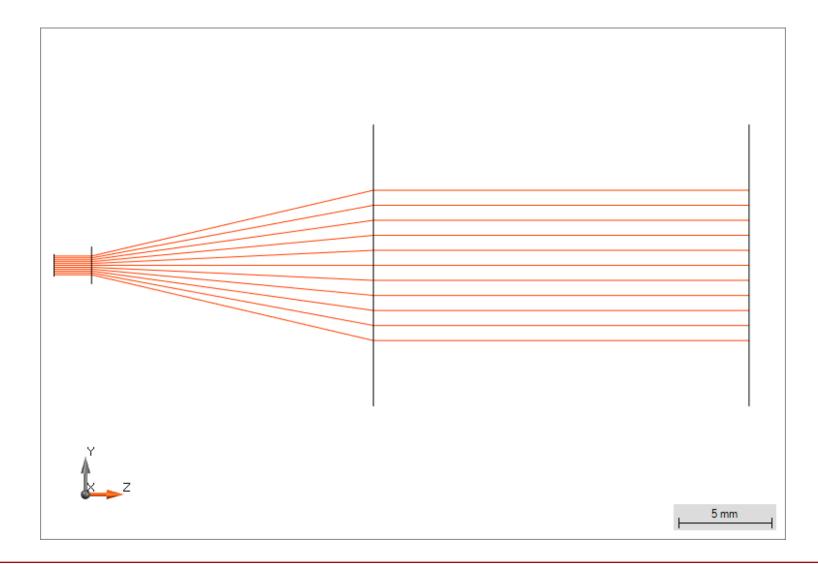
• Thus, the functional design results by analytical considerations to the wavefront phases:

$$\Delta \psi_1(\boldsymbol{\rho}, k_0) = k_0 n \sqrt{\|\boldsymbol{\rho}\|^2 + R_1^2}$$
$$\Delta \psi_2(\boldsymbol{\rho}, k_0) = -k_0 n \sqrt{\|\boldsymbol{\rho}\|^2 + R_2^2}$$

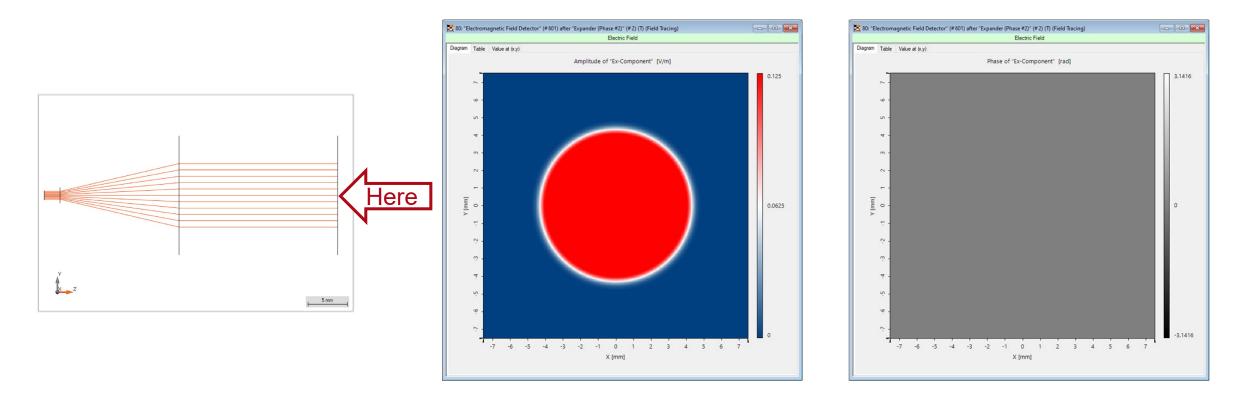
# **Beam Expander (1:5) – Functional Design**



### **Beam Expander (1:5) – Functional Design: Ray Tracing**



## **Beam Expander (1:5) – Functional Design: Output Beam**



Amplitude after Beam Expander

Phase after Beam Expander

# FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

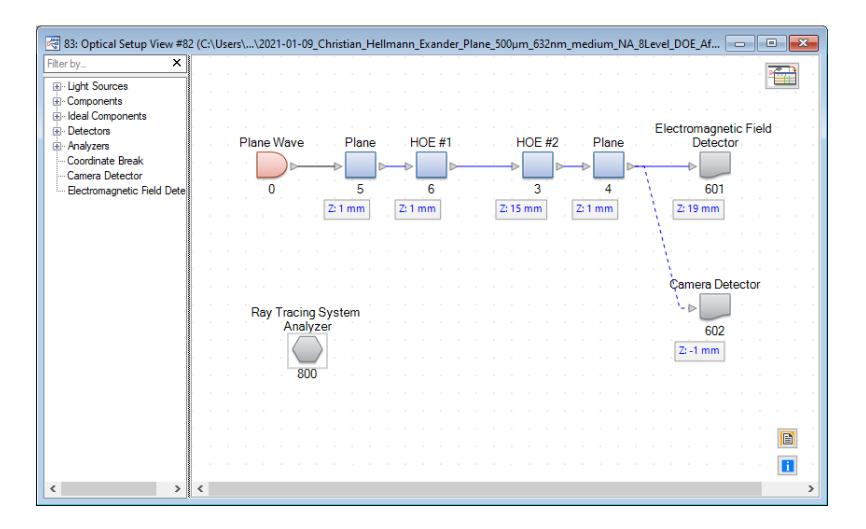
#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

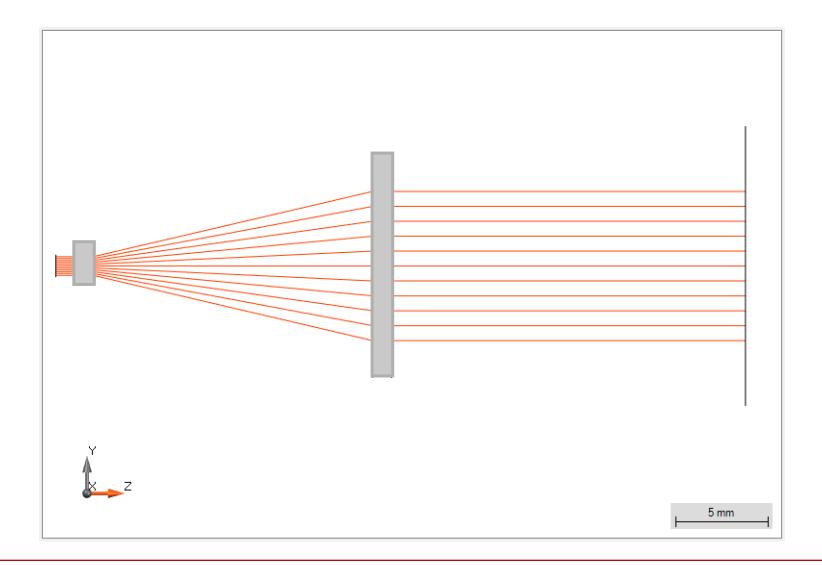
#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

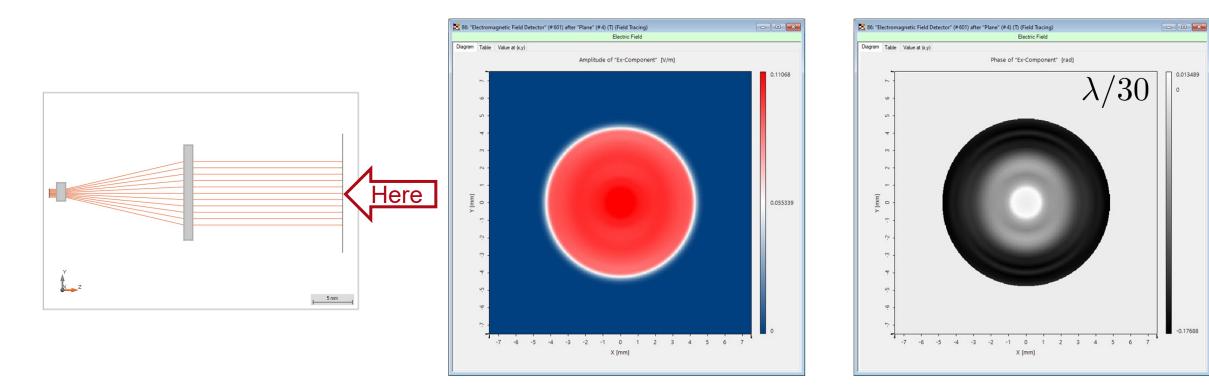
### **Beam Expander (1:5) – Structural Design: HOEs**



### **Beam Expander (1:5) – Structural Design: HOEs**



## **Beam Expander (1:5): Output Beam for HOEs**

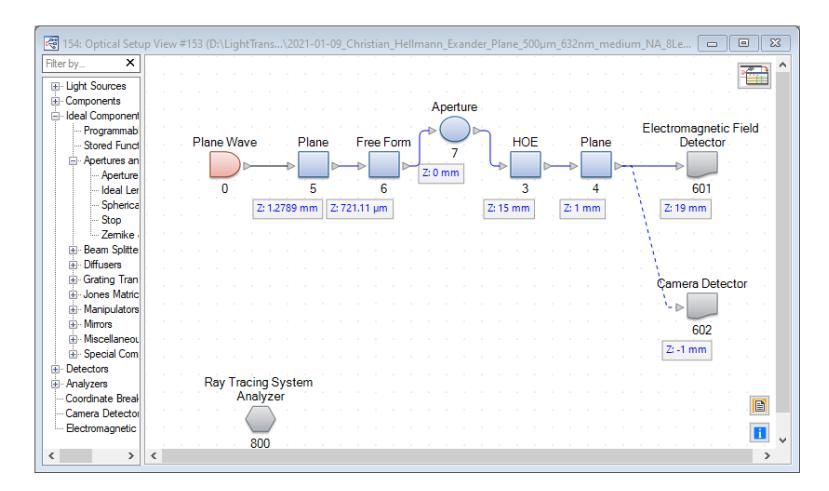


Amplitude after Beam Expander

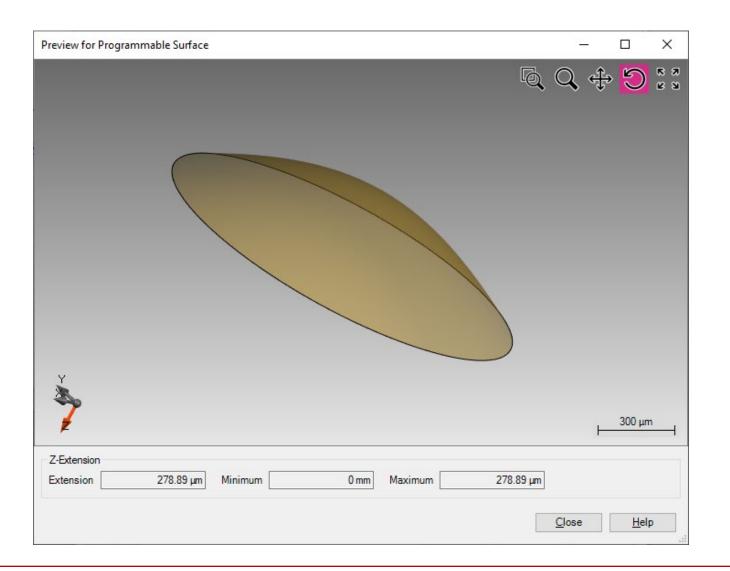
Phase after Beam Expander

Efficiency of HOE #1: 76.82% Efficiency of HOE #2: 77.15% System Efficiency: 59.27%

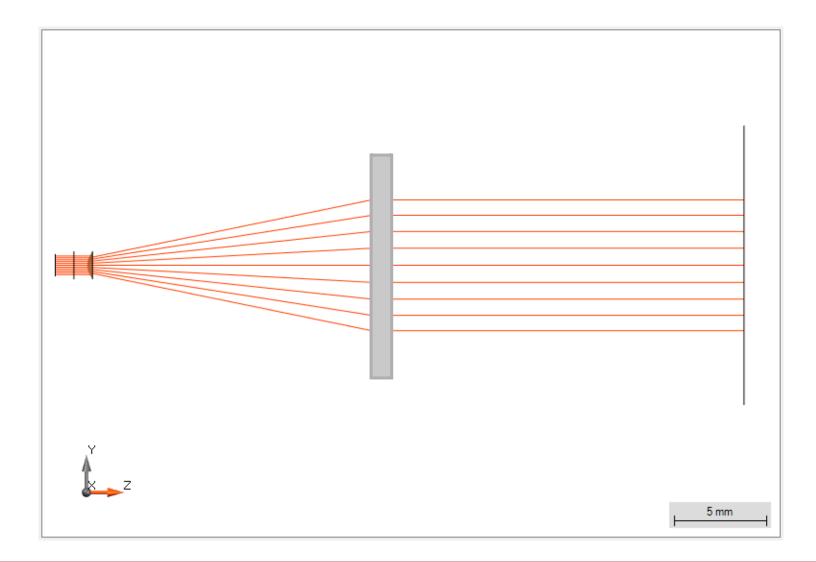
### Beam Expander (1:5) – Structural Design: Lens + HOE



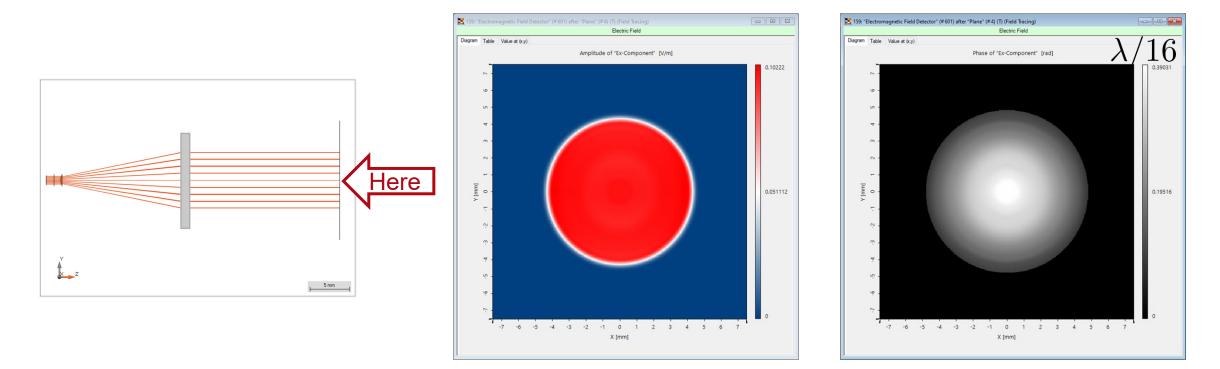
## **Beam Expander (1:5) – Structural Design: Lens**



### Beam Expander (1:5) – Structural Design: Lens + HOE



## Beam Expander (1:5): Output Beam for Lens + HOE



Amplitude after Beam Expander

Phase after Beam Expander

Efficiency of Freeform: 93.09% Efficiency of HOE: 77.15% System Efficiency: 71.82%

# FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

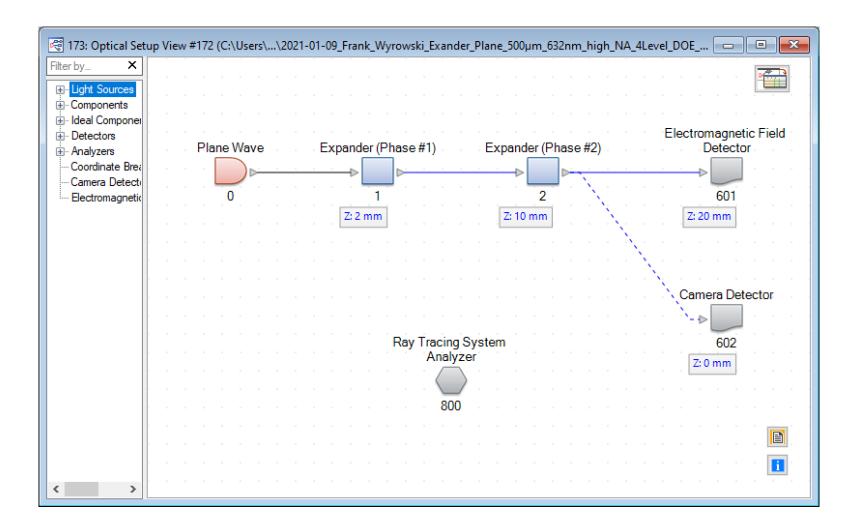
#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

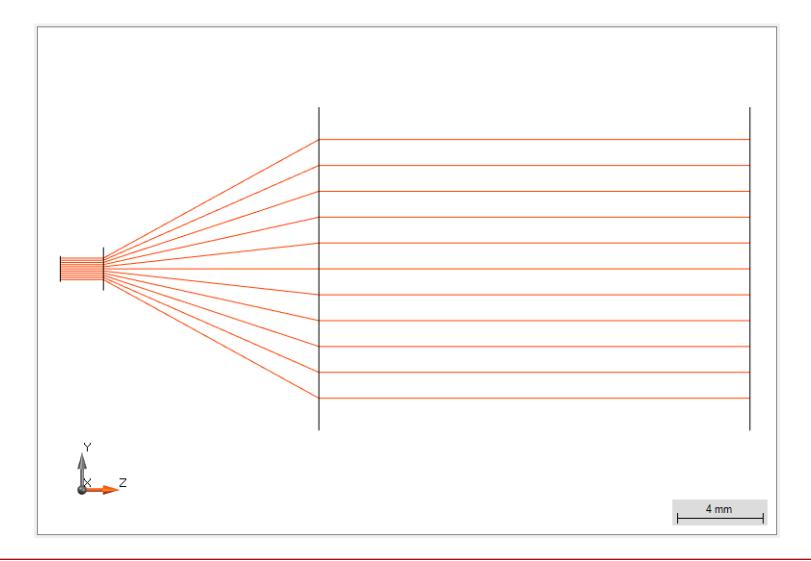
#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

### **Beam Expander (1:10) – Functional Design**



### **Beam Expander (1:10) – Functional Design: Ray Tracing**



## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

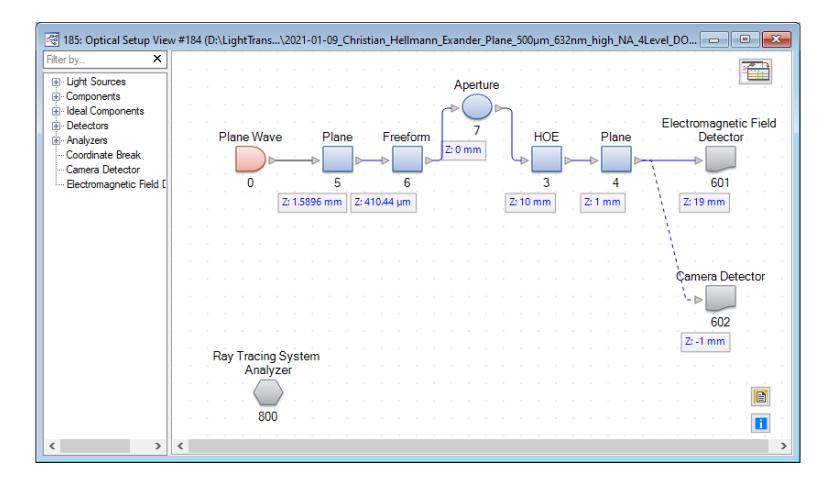
#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

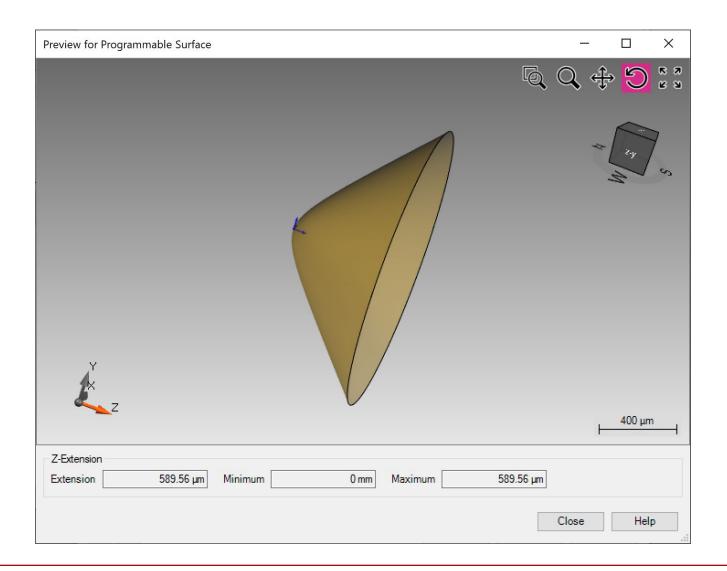
#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

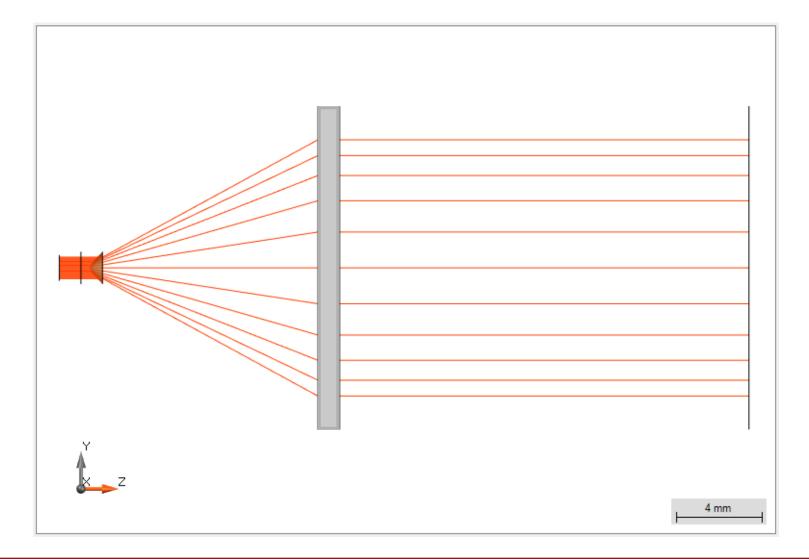
### Beam Expander (1:10) – Structural Design: Lens + HOE



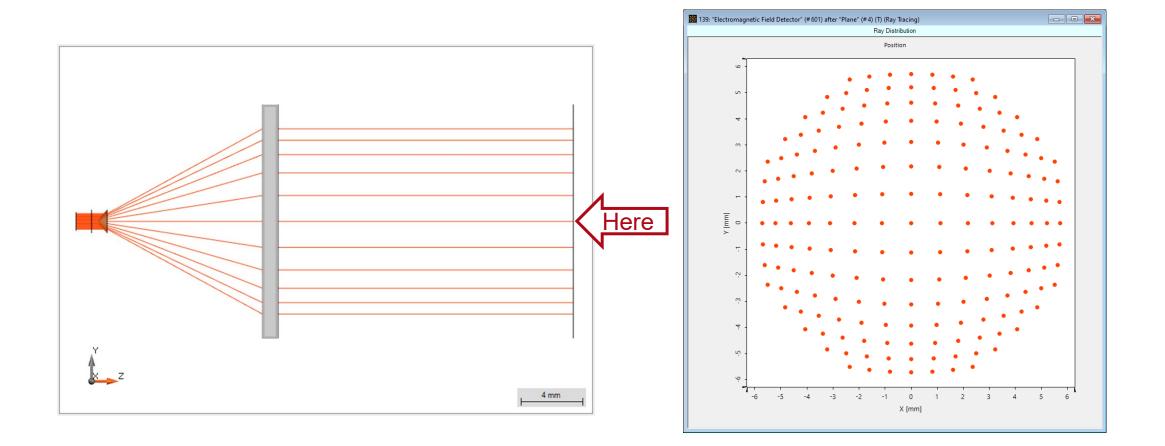
### Beam Expander (1:10) – Structural Design: Lens



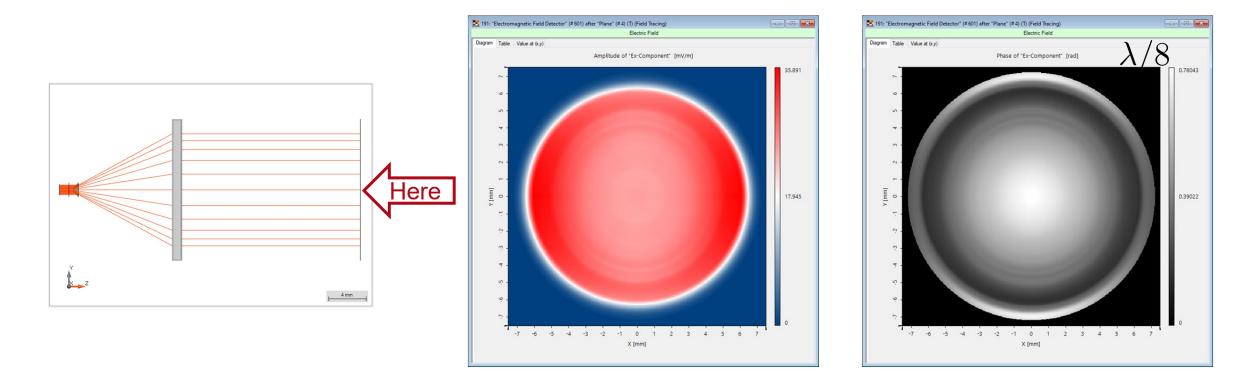
### Beam Expander (1:10) – Structural Design: Lens + HOE



### Beam Expander (1:10) – Structural Design: Lens + HOE



### Beam Expander (1:10): Lens + HOE Output Beam

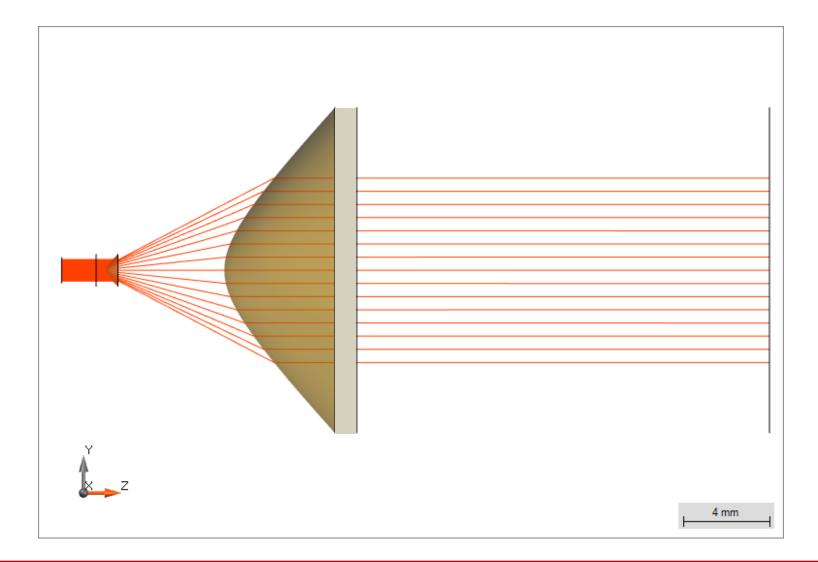


Amplitude after Beam Expander

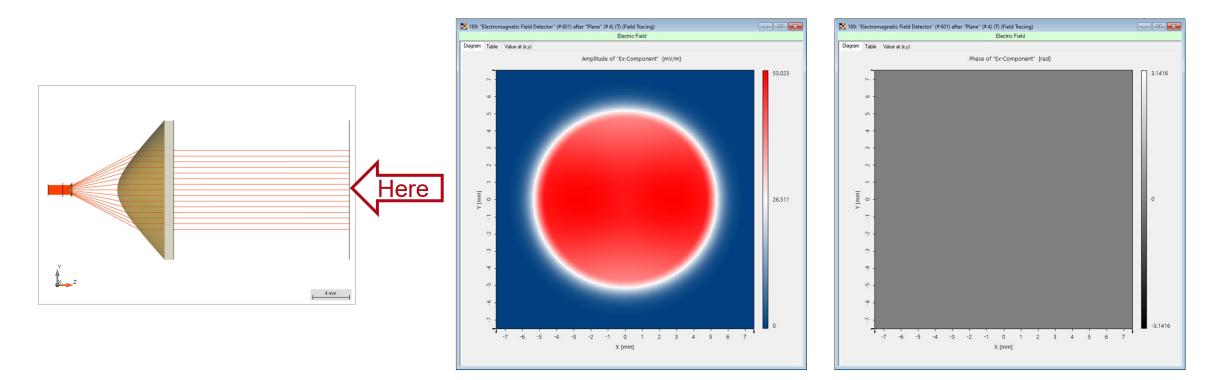
Phase after Beam Expander

Efficiency of Freeform: 89.53% Efficiency of HOE: 53,39% System Efficiency: 47.8%

### Beam Expander (1:10) – Structural Design: Lens + Lens



### Beam Expander (1:10) : Lens + Lens Output Beam



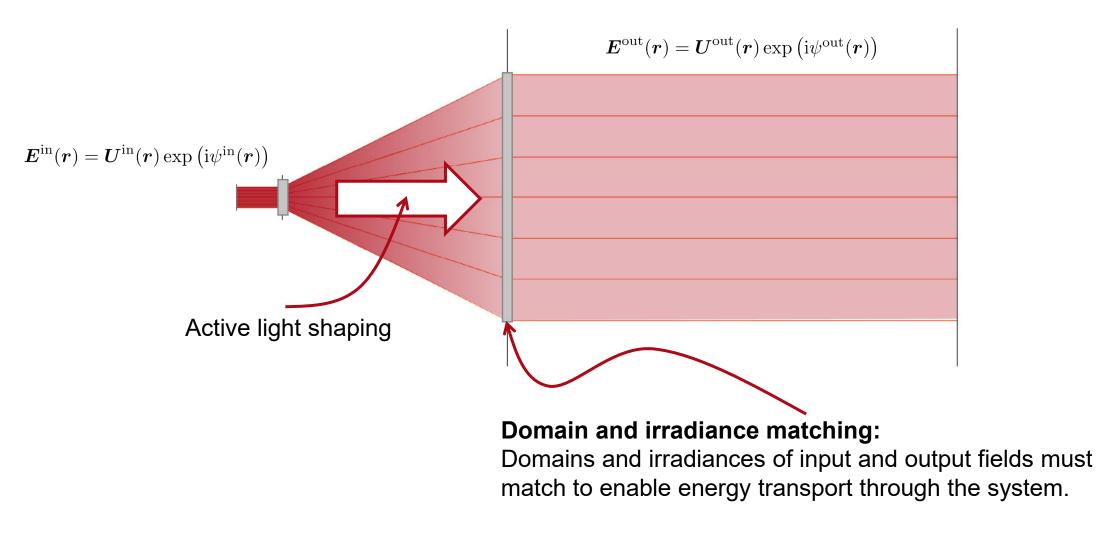
Amplitude after Beam Expander

Phase after Beam Expander

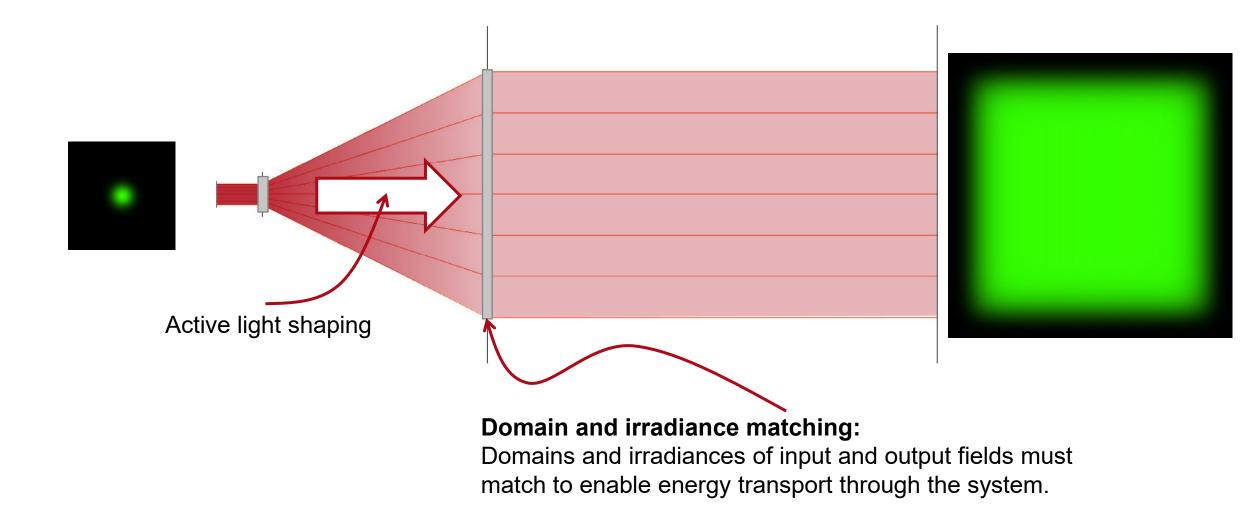
Efficiency of Freeform #1: 89.53% Efficiency of Freeform #2: 89.53% System Efficiency: 80.16%

### **Beam expander with light shaping**

### **Shaping Beam Expander: Scenario**



### **Shaping Beam Expander: Scenario**



## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

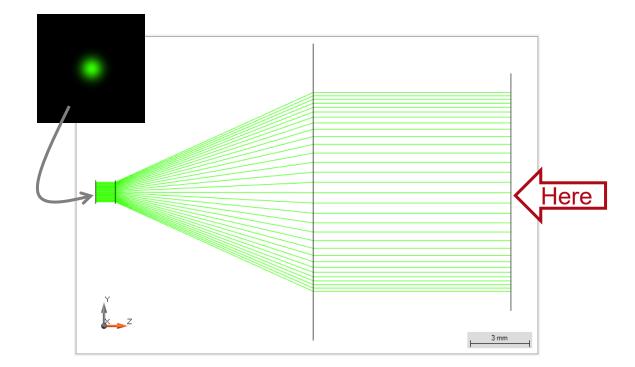
#### SYSTEM TOLERANCING

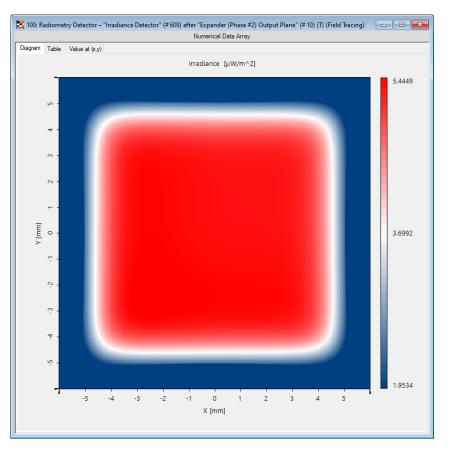
Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

### **Shaping Beam Expander: Functional Design**





Irradiance (by field tracing)

## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

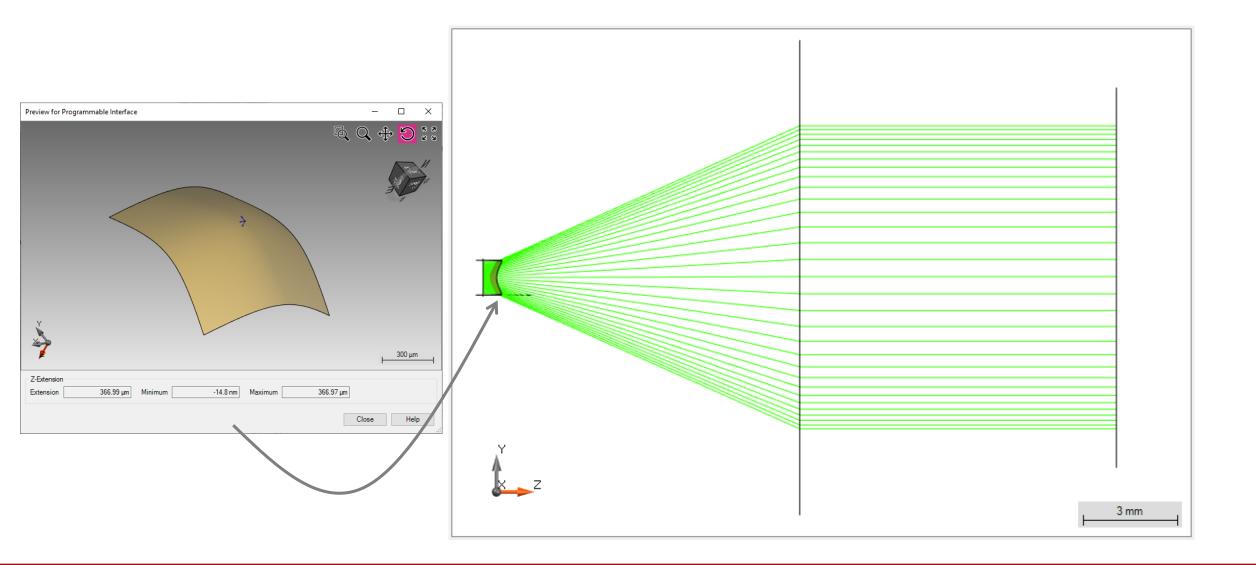
#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

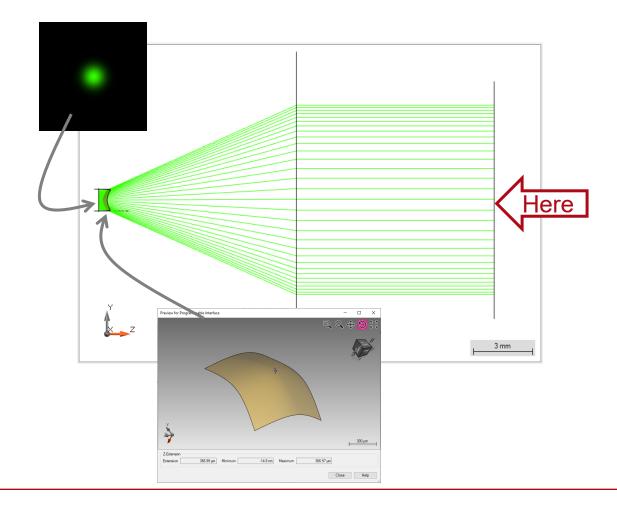
#### FABRICATION DATA

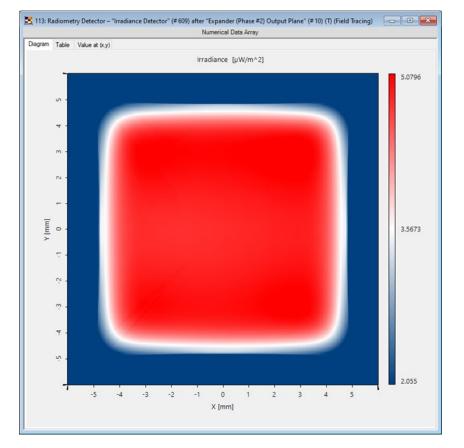
Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

### **Shaping Beam Expander: Freeform + Functional**



### **Shaping Beam Expander: Freeform + Functional**





Irradiance (by field tracing)

### Design and Analysis of a Hybrid Eyepiece for Correction of Chromatic Aberration

Functional design in Zemax® OpticStudio®

## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

Zemax® enables functional design of a wavefront phase response (binary surfaces) by parametric optimization

### **Design Workflow in VirtualLab Fusion**

FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

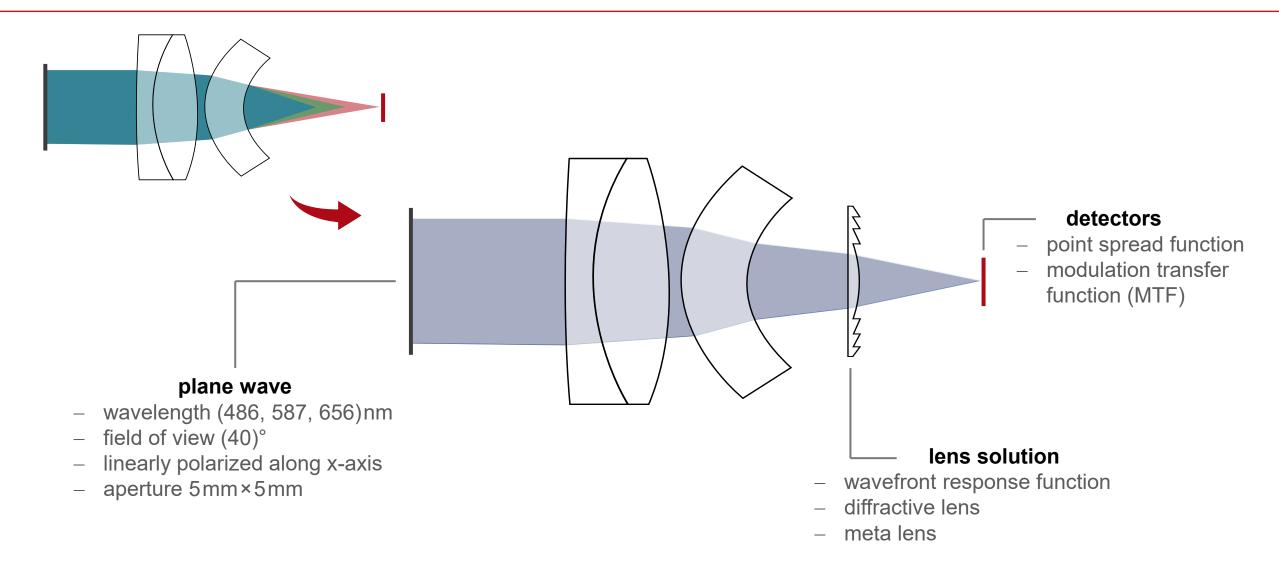
#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

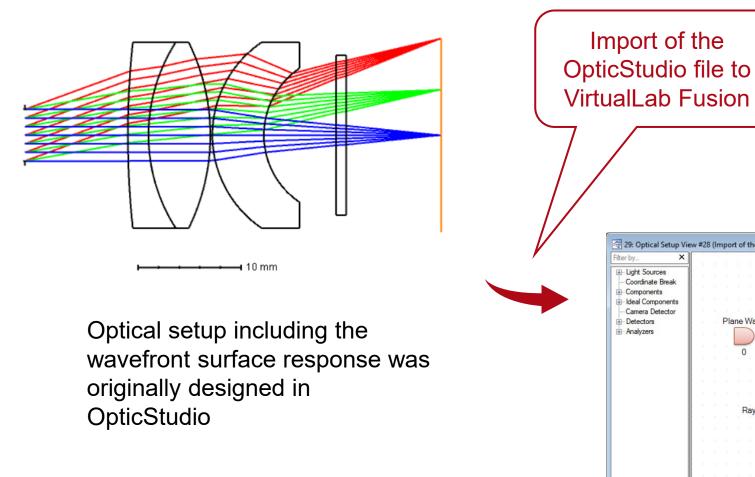
Import of Zemax file into VirtualLab Fusion and further processing of workflow.

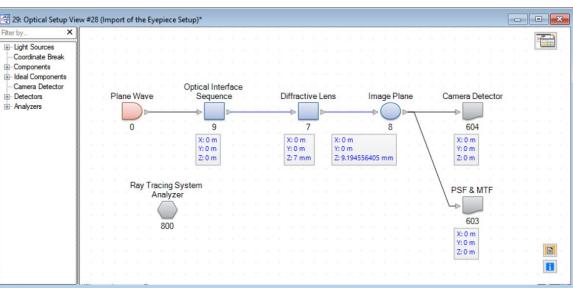


### **Modeling and Design Scenario**



### **Design of Wavefront Surface Response in OpticStudio**





## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

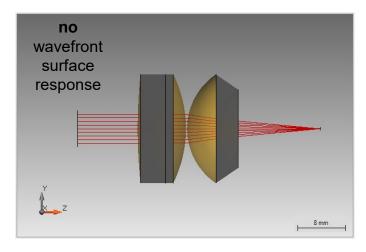
#### FABRICATION DATA

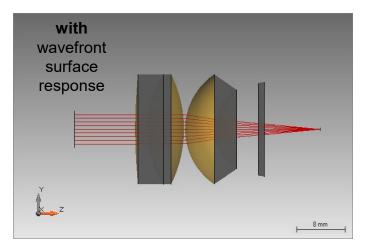
Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

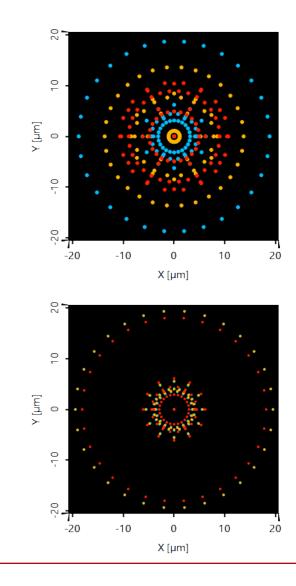
Import of Zemax file into VirtualLab Fusion and further processing of workflow.



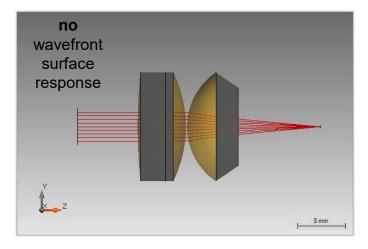
### **On-Axis Analysis: Comparison of Spot Diagram**

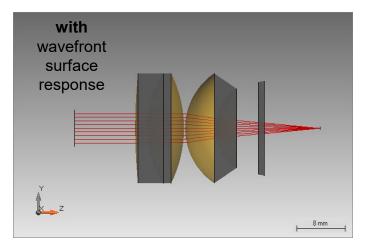


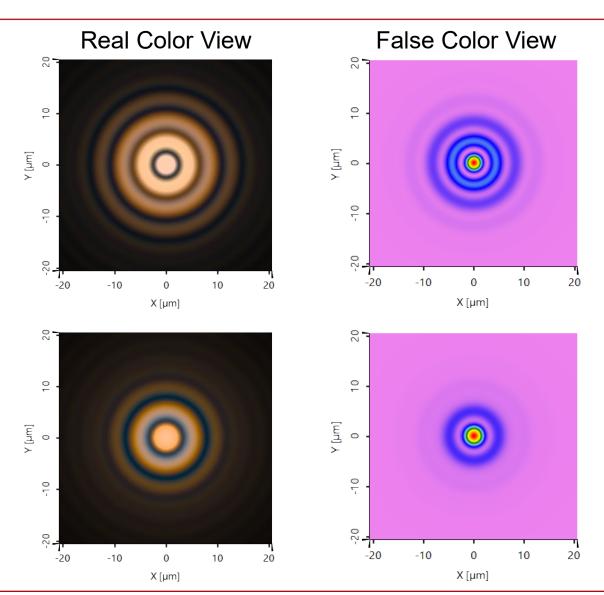




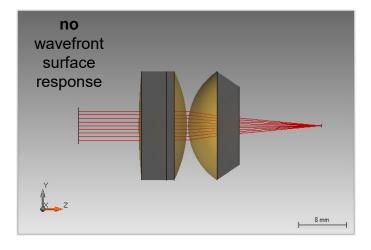
### **On-Axis Analysis: Comparison of PSF**

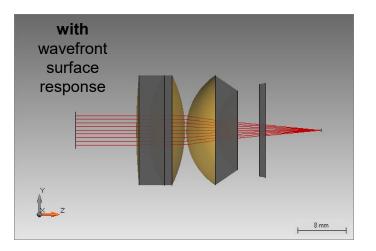


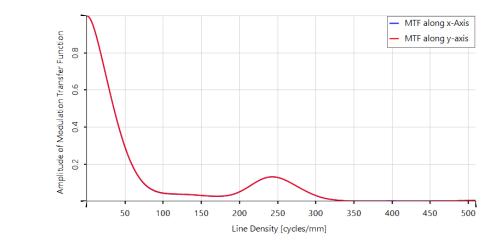


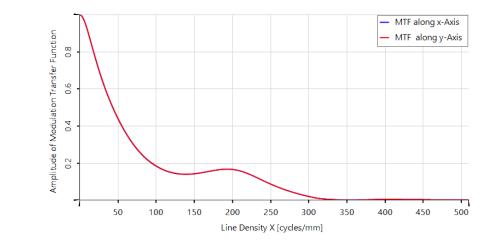


### **On-Axis Analysis: Comparison of MTF**

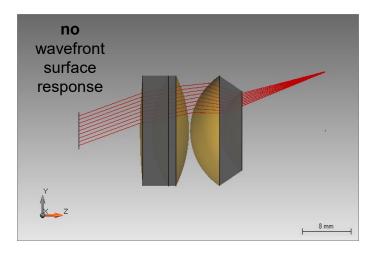


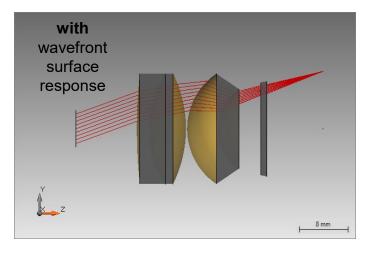


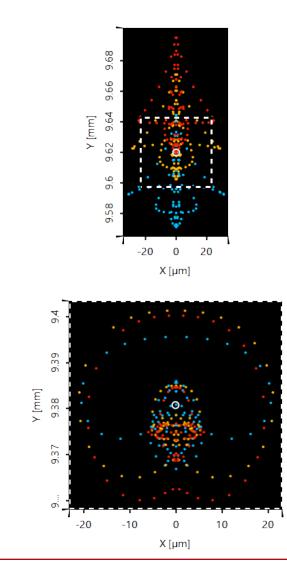




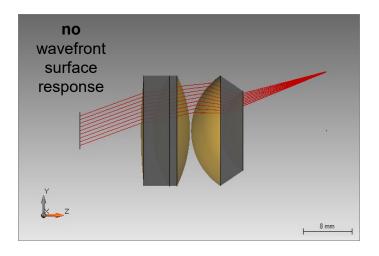
### **Off-Axis Analysis: Comparison of Spot Diagram**

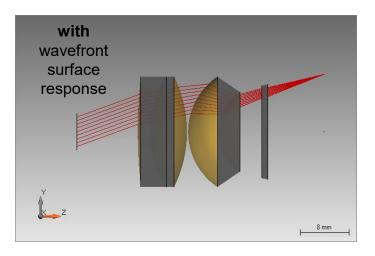


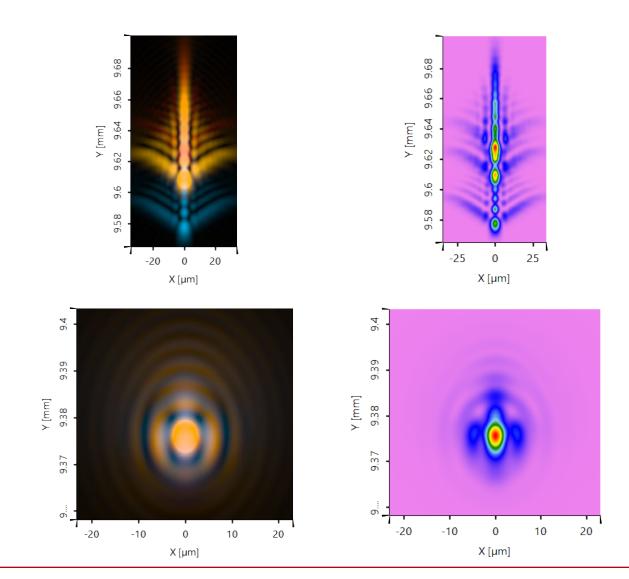




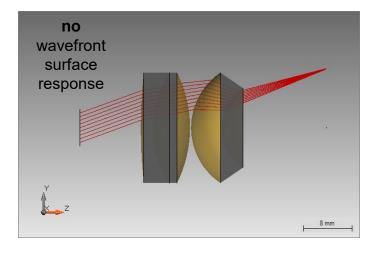
### **Off-Axis Analysis: Comparison of PSF**

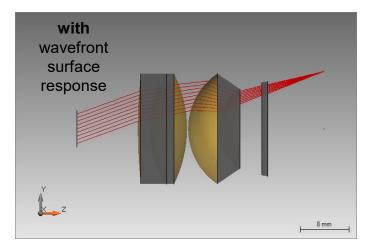


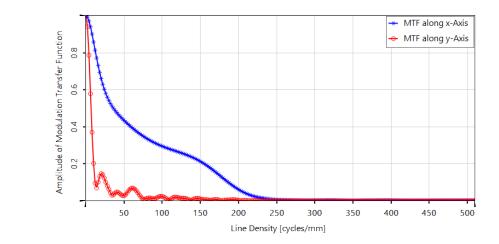


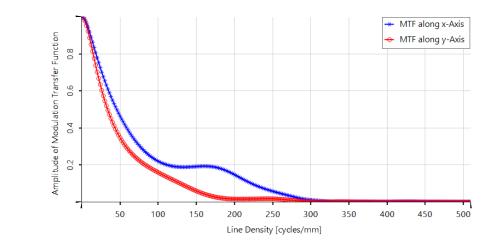


### **Off-Axis Analysis: Comparison of MTF**









## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

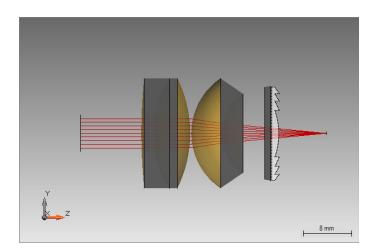
#### FABRICATION DATA

Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

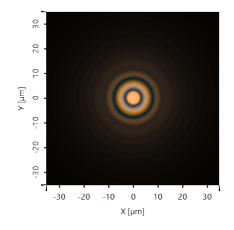
Import of Zemax file into VirtualLab Fusion and further processing of workflow.



### **On-Axis Analysis: Inclusion of Higher Orders**



 $\propto \text{Electric Energy Density}_{[1E6 (V/m)^2]}$ 



0

10

-20

30

-30 -20 -10 0 10

X [µm]

0<sup>th</sup> diffraction order

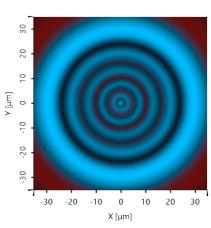
20 30

[mr] >

3.96

∝ Electric Energy Density

 $[1E3 (V/m)^2]$ 



0

X [µm]

20

-20

∝ Electric Energy Density

 $[(V/m)^2]$ 

64.8

33.1

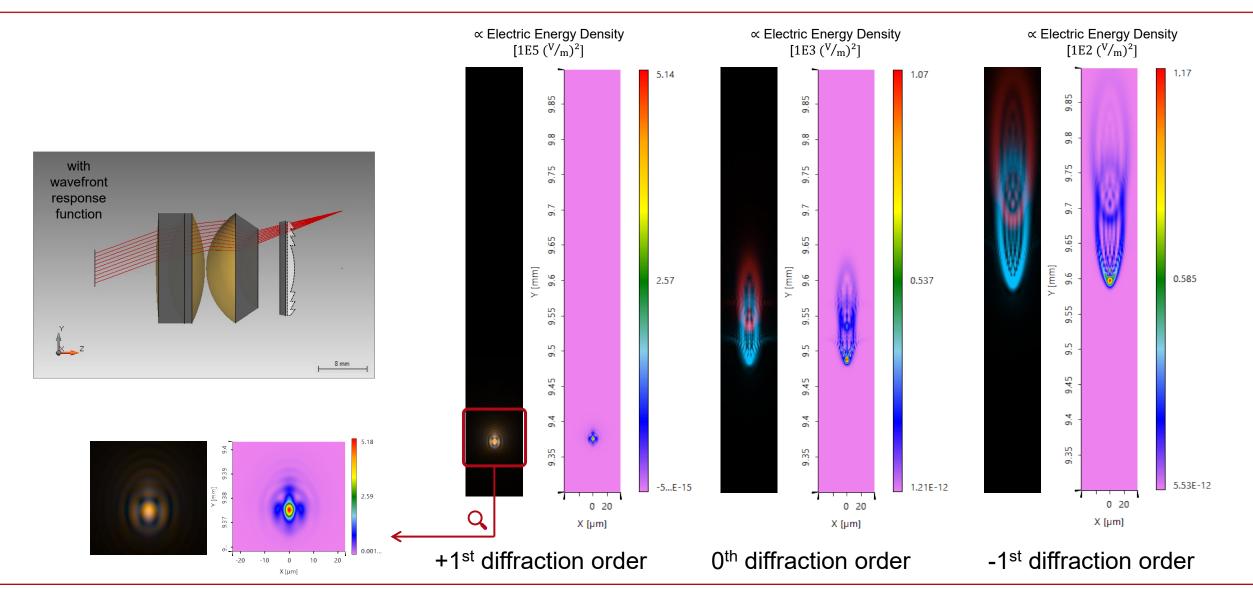
1.51

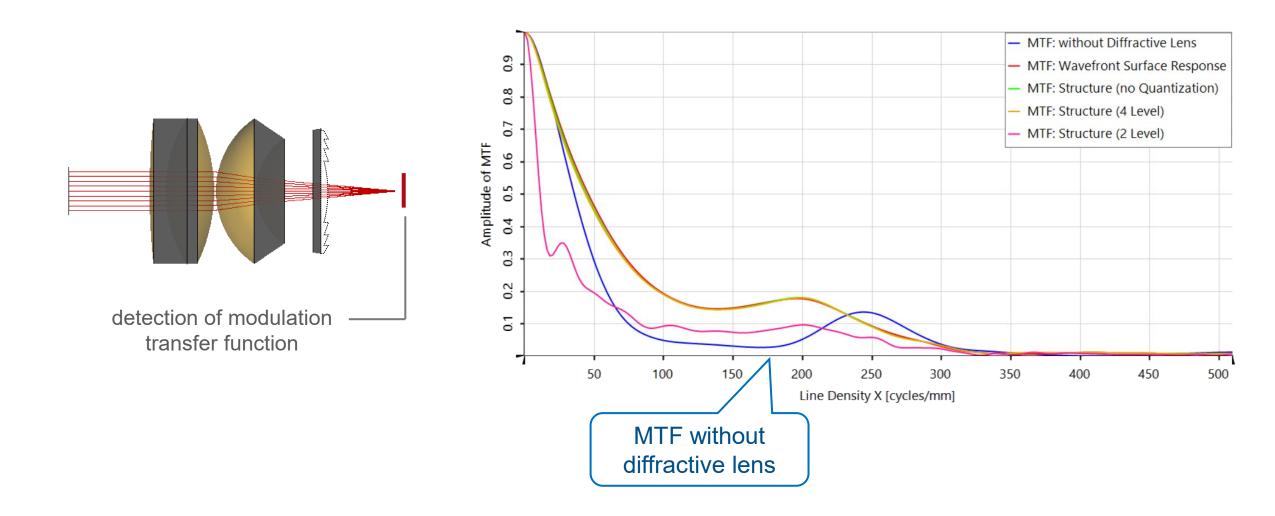
-1<sup>st</sup> diffraction order

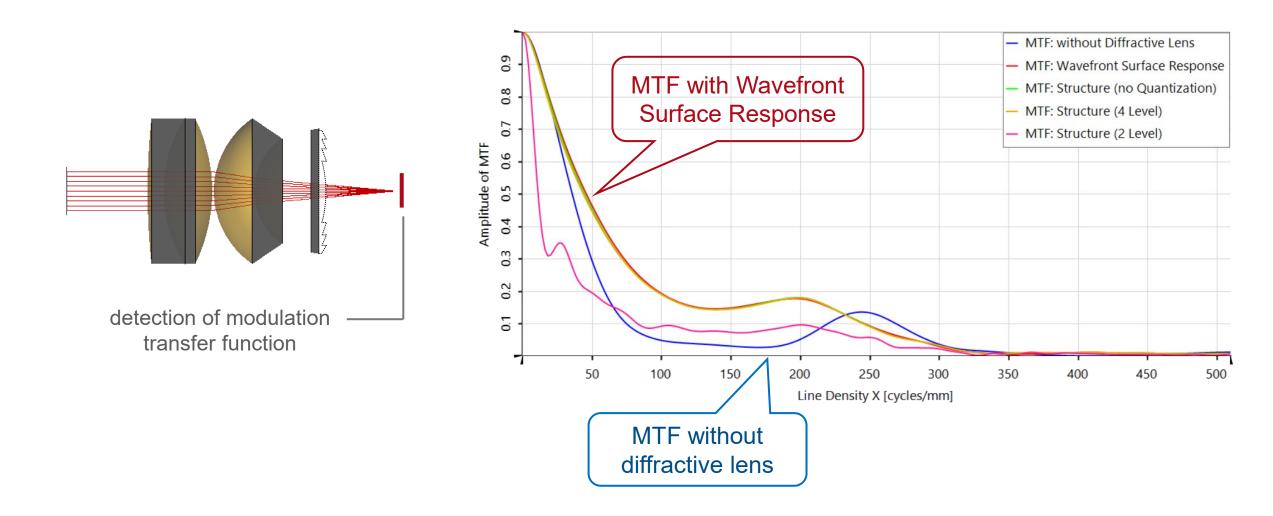
+1<sup>st</sup> diffraction order

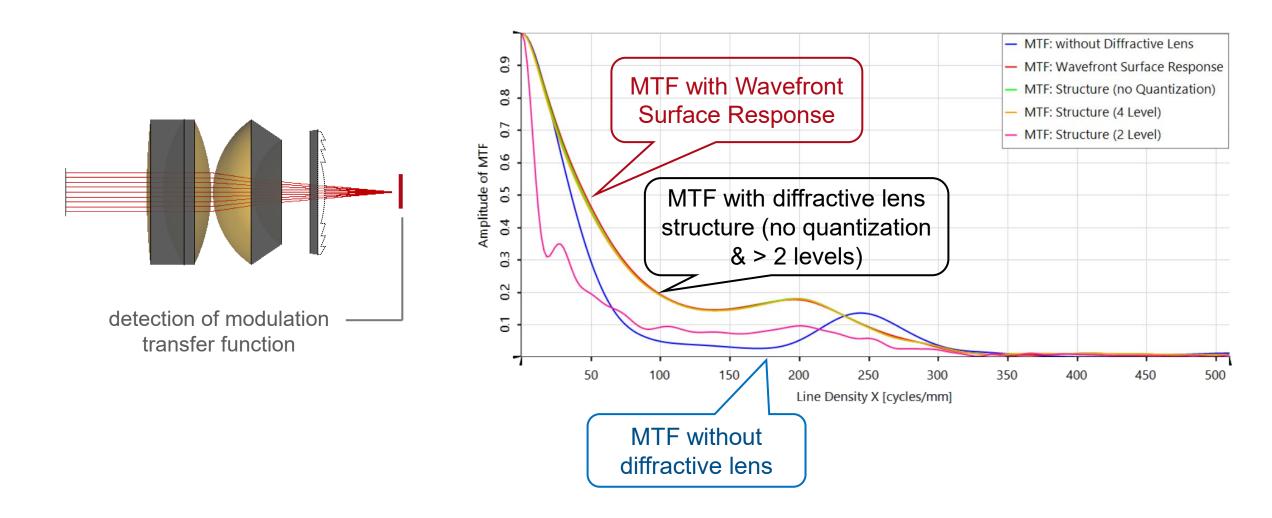
simulation time per order ~seconds

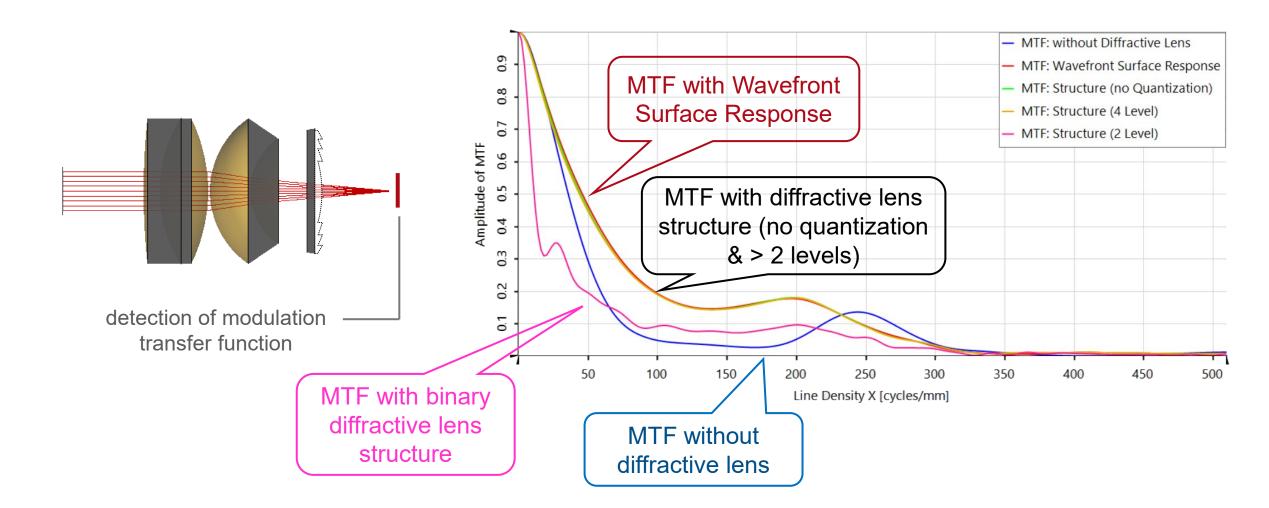
### **Off-Axis Analysis: Inclusion of Higher Orders**











## FUNCTIONAL DESIGN

Design the system by introducing functional components to achieve the demanded system functionality.

#### STRUCTURAL DESIGN

Replace functional components by smooth surface or flat optics components.

# MODELING & EVALUATION

Model the system with ray tracing and physical optics. Evaluate the performance by suitable detectors and merit functions.

#### FURTHER OPTIMIZATION

Use the modeling techniques to further optimize the system by, e.g., parametric optimization.

#### SYSTEM TOLERANCING

Investigate the fabrication tolerances of components and the adjustment sensitivity of the system.

#### FABRICATION DATA

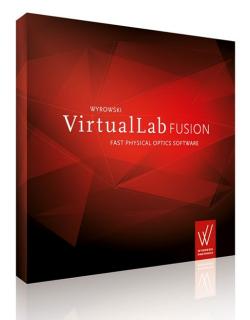
Use the modeling techniques to further optimize the system by, e.g. parametric optimization.

Import of Zemax file into VirtualLab Fusion and further processing of workflow.



### Conclusion

- VirtualLab Fusion provides a steadily growing number of tools for flat and freeform optics.
- Functional design concepts essential in workflow.
- New surface design techniques avoid parametric optimization.
- VirtualLab Fusion modeling and design tools allow the investigation of pros and cons of flat and freeform optics.
- Techniques demonstrated in this webinar are:
  - All available in-house for modeling and design services
  - Partly included in current version of VirtualLab Fusion
  - All will be released in 2021



VirtualLab Fusion 2021