

Fast physical optics with VirtualLab Fusion optics software

## **Modeling and Design of Gratings, DOEs, Diffractive and Metalenses**

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# Jena, Germany



# LightTrans International



## LightTrans

- Distribution of VirtualLab Fusion, together with distributors worldwide
- Technical support, seminars, and trainings
- Engineering projects

# University of Jena



**Applied Computational Optics Group** R&D in optical modeling and design with emphasis on physical optics

# Wyrowski Photonics

**WYROWSKI PHOTONICS**

**LIGHTTRANS**

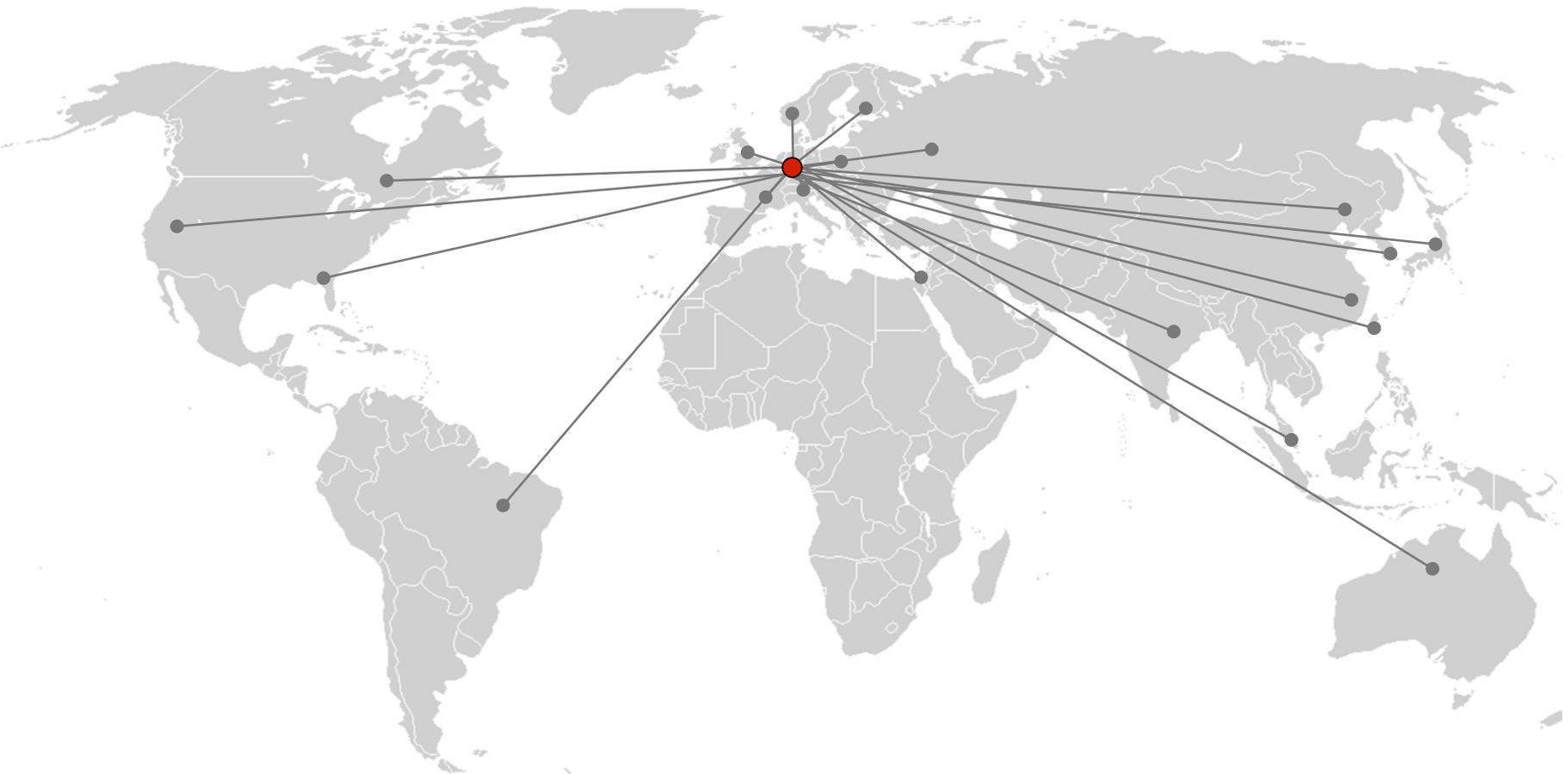
**WYROWSKI PHOTONICS**  
Development of fast  
physical optics software  
VirtualLab Fusion

WYROWSKI  
**VirtualLab FUSION**  
FAST PHYSICAL OPTICS SOFTWARE

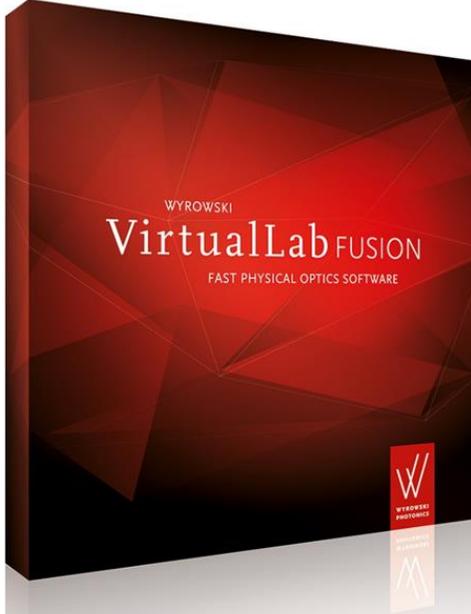
Jena

seit 1558

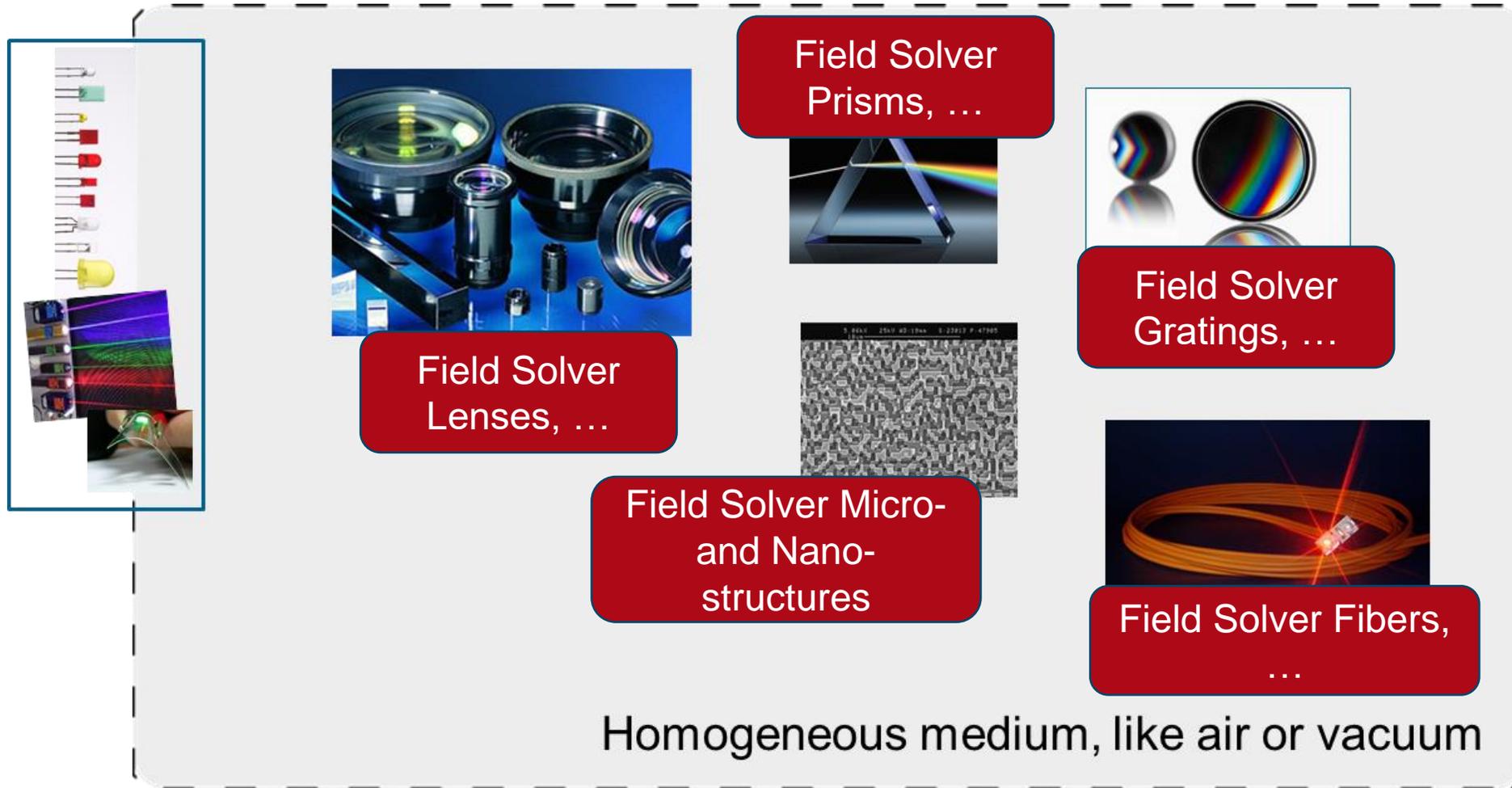
# Optical Design Software and Services



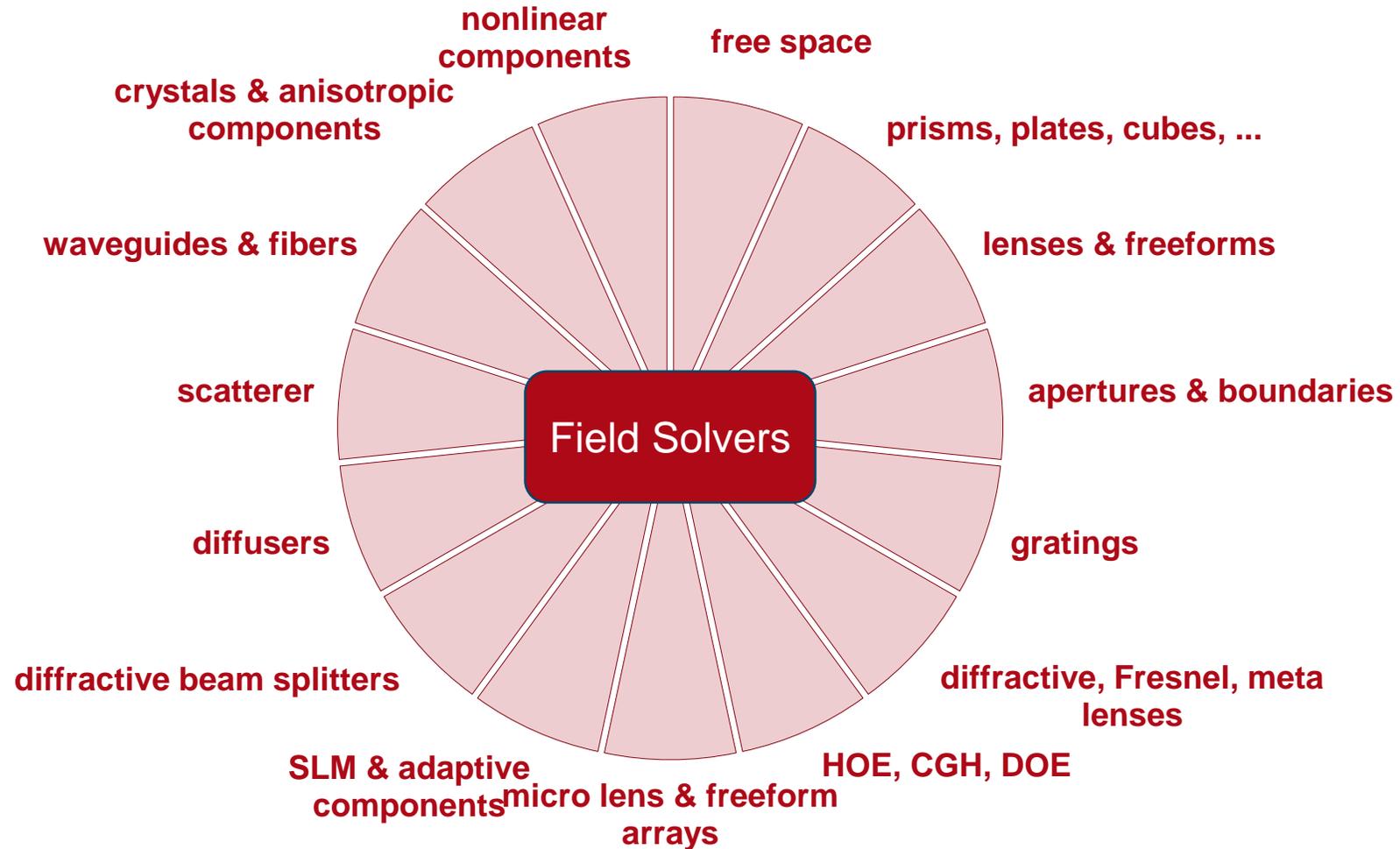
**Hall B1, 209**



# Physical-Optics System Modeling by Connecting Field Solvers

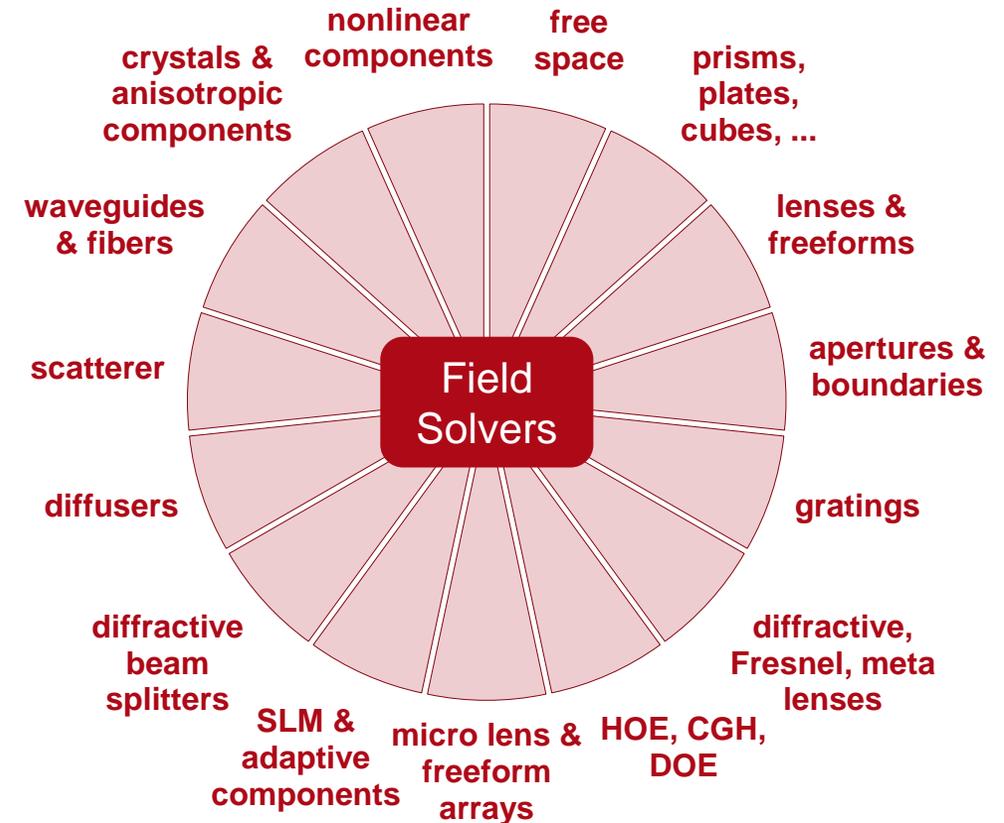


# Physical-Optics System Modeling: Regional Field Solvers



# Physical-Optics System Modeling by Connecting Field Solvers

VirtualLab Fusion is a unified software platform incorporating various field solvers



# VirtualLab Fusion – Summer Release 2019

Field Solver Lenses, ...

Field Solver Prisms, ...

Field Solver Gratings, ...

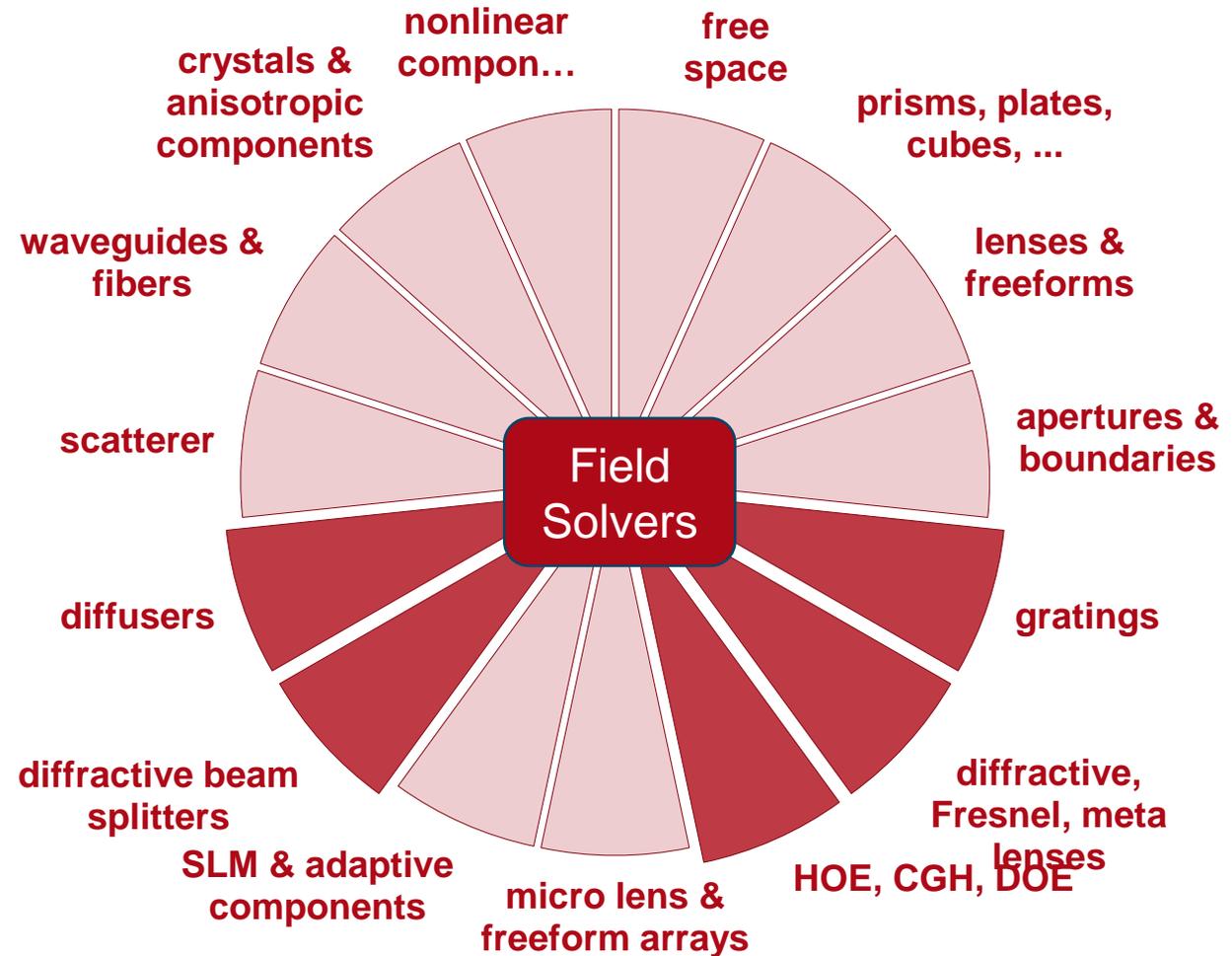
Field Solver Micro- and Nano-structures

Field Solver Fibers, ...

Homogeneous medium, like air or vacuum

# VirtualLab Fusion – Summer Release 2019

**VirtualLab Fusion  
Summer Release 2019**



# VirtualLab Fusion – Summer Release 2019

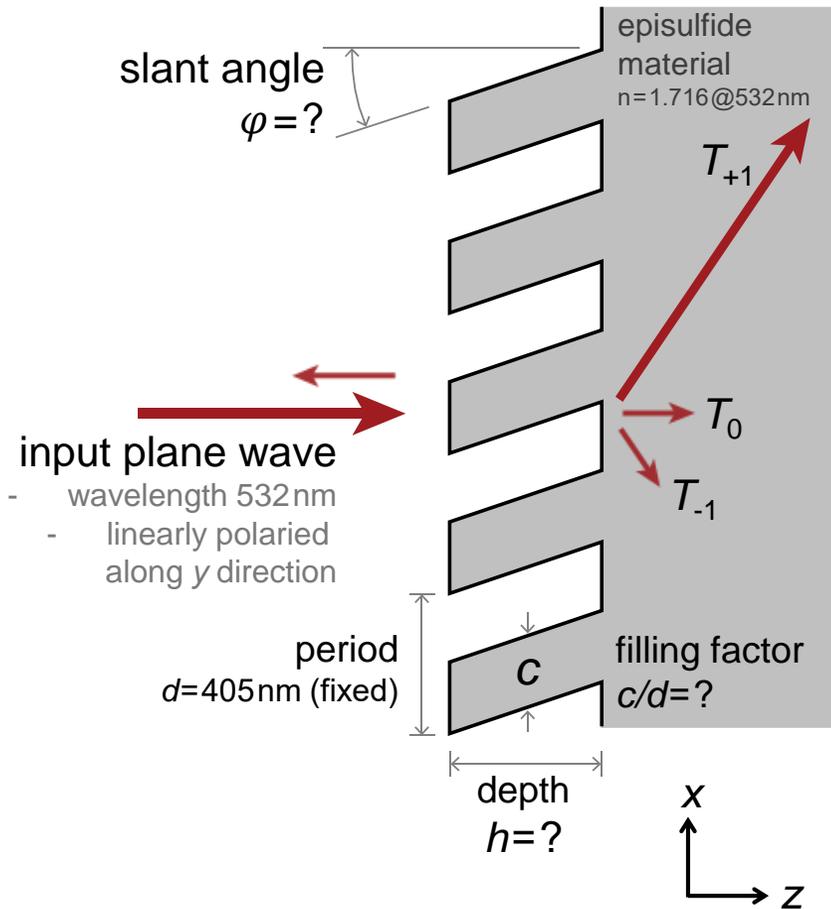
<p><b>Microstructure Components Modeling</b></p> <ul style="list-style-type: none"><li>▪ Modeling of microstructure components beyond paraxial situation</li><li>▪ Combined use with general input field</li><li>▪ Typical use for diffractive diffuser system modeling</li></ul>	<p><b>Diffractive Lens</b></p> <ul style="list-style-type: none"><li>▪ Complementary workflow with Zemax OpticStudio</li><li>▪ Direct import of e. g. Binary 2 surface</li><li>▪ Modeling based on real diffractive lens surface structures</li><li>▪ Export for fabrication</li></ul>	<p><b>Coming in 2019</b></p> <p><b>Metalens</b></p> <ul style="list-style-type: none"><li>▪ Unified software platform with both rigorous analysis of nano structures, and also whole lens modeling</li><li>▪ Rigorous Fourier modal method (FMM) for unit cell modeling with friendly structure configuration</li></ul>	<p><b>Integral Method for Grating Modeling</b></p> <ul style="list-style-type: none"><li>▪ In-built model for rectangular/slanted gratings with rounded edges</li><li>▪ Faster convergence than other techniques</li><li>▪ Suitable for fabrication tolerance analysis</li></ul>	<p><b>Grating Components in General Optical Setup</b></p> <ul style="list-style-type: none"><li>▪ Rigorous modeling based on in-built Fourier modal method (FMM/RCWA)</li><li>▪ Use together with other components in general optical setups</li><li>▪ Arbitrary orientation</li></ul>	<p><b>Simulation Engine Improvement</b></p> <ul style="list-style-type: none"><li>▪ Automatized sampling algorithm for free-space propagation</li><li>▪ Robust handling of aberrated wavefront phases</li><li>▪ Unified algorithm for propagation between tilted planes as well</li></ul>
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... and more at our booth

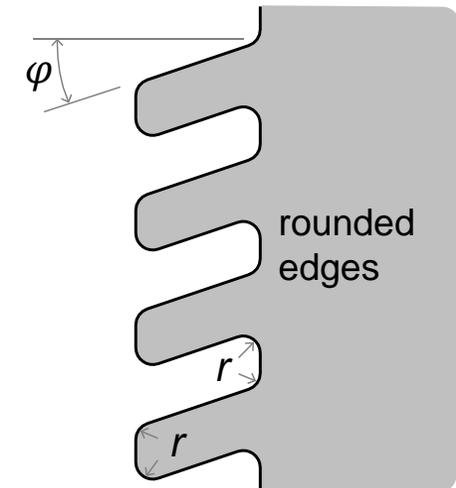
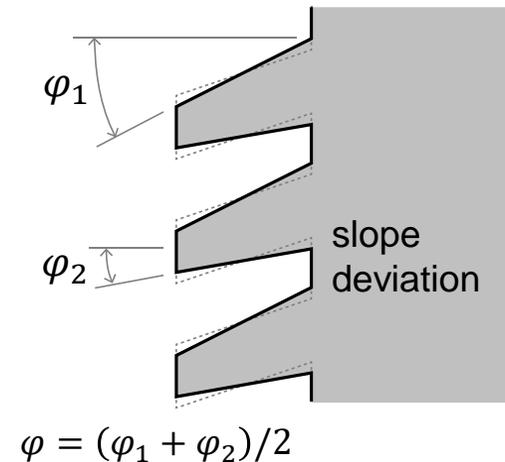
**Hall B1, 209**

# **Parametric Optimization and Tolerance Analysis of Slanted Gratings**

# Modeling Task

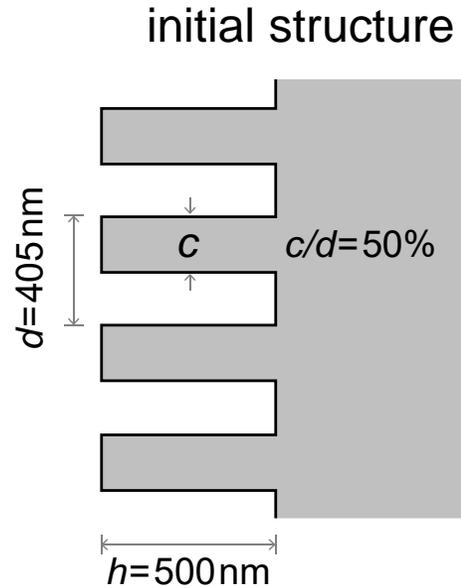


How to optimize the  $T_{+1}$  order diffraction efficiency, by adjusting the slant angle  $\varphi$ , grating depth  $h$ , and filling factor  $c/d$ ?

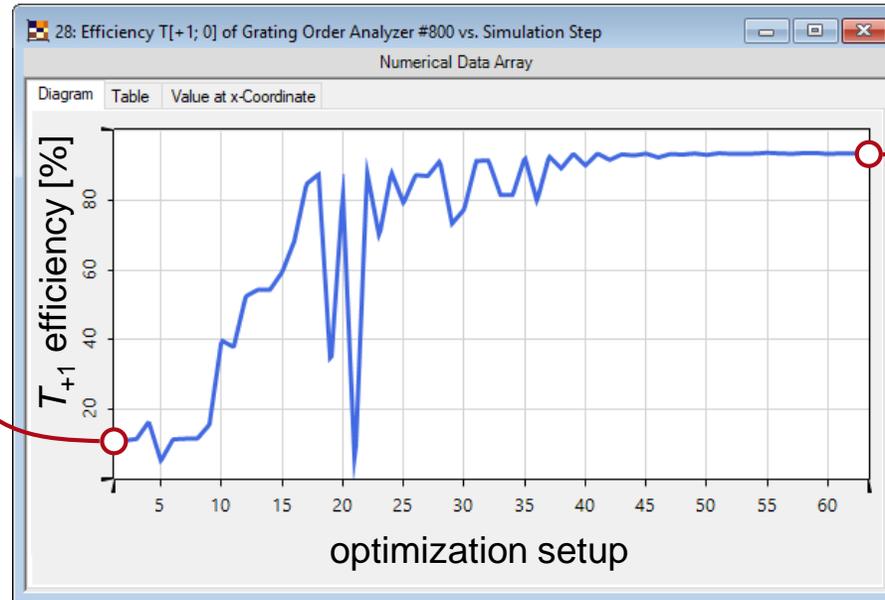


In addition, how to evaluate the grating performance with the slope deviation and the rounded edges due to the fabrication technique taken into account?

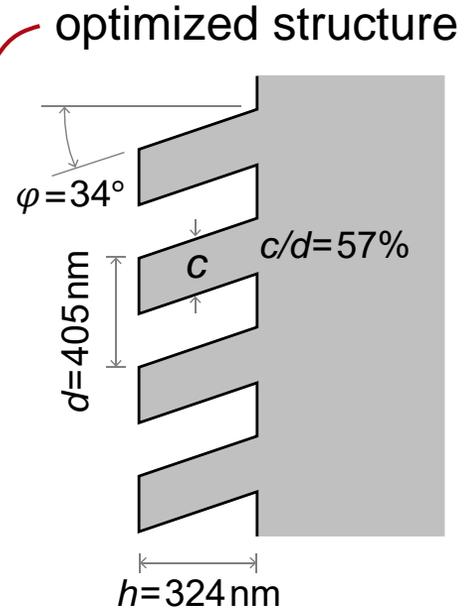
# Parametric Optimization for 1<sup>st</sup> Order



Order	Efficiency
-1	11.551%
0	72.795%
+1	11.551%



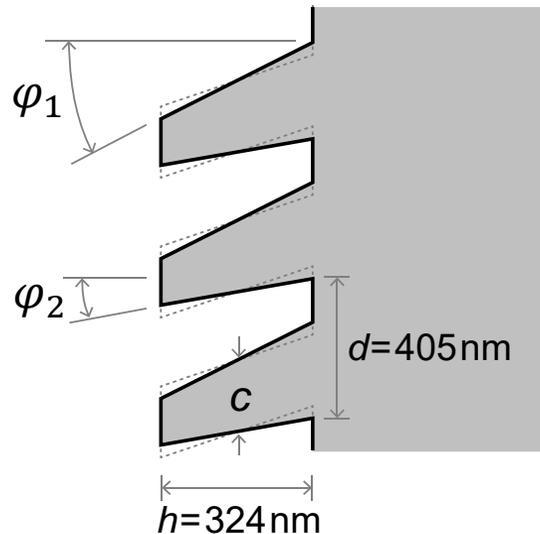
parametric optimization – downhill simplex method – with rigorous Fourier modal method (FMM) used for grating efficiency calculation



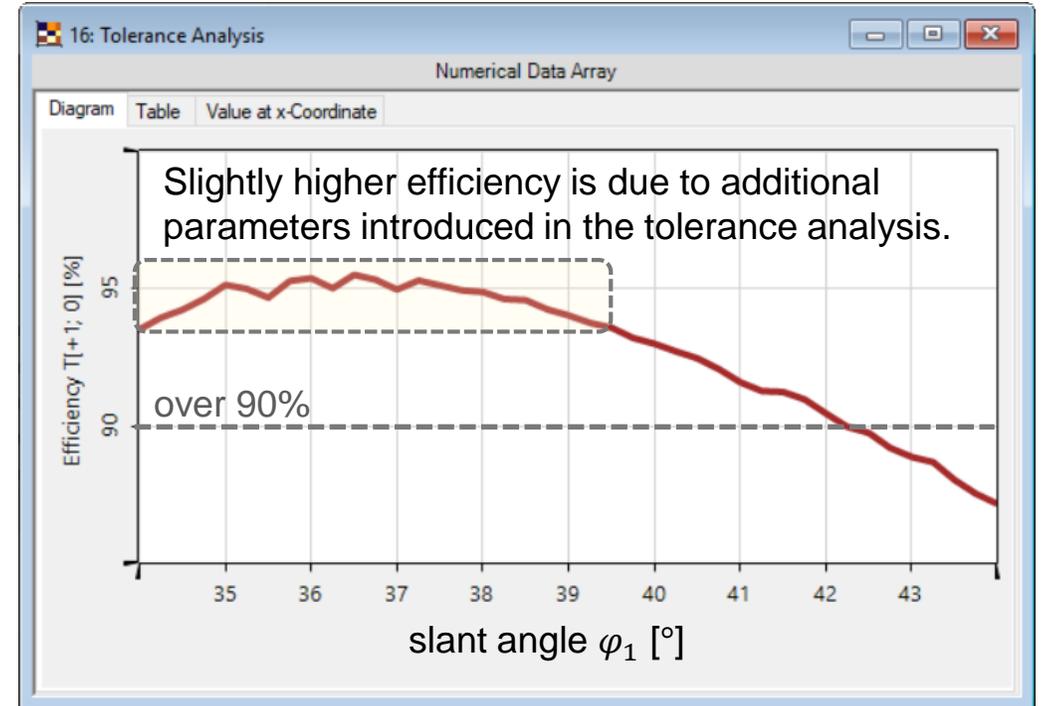
Order	Efficiency
-1	3.257%
0	0.365%
<b>+1</b>	<b>93.659%</b>

# Results – Tolerance Analysis

The fabricated slanted gratings often shows a deviation from the perfect parallel grating lines. Such slope deviations should be taken into account for the tolerance analysis.



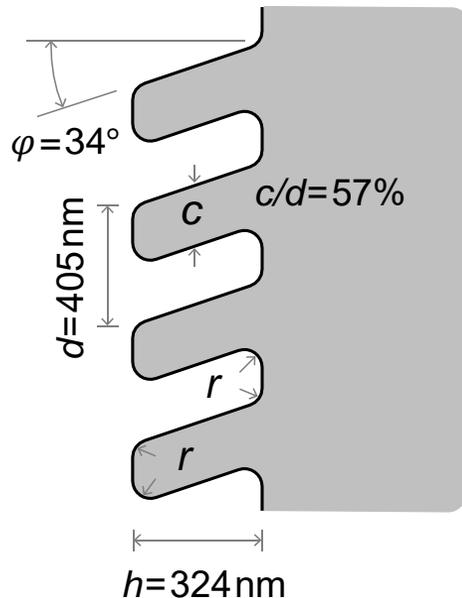
- fixed average slant angle  $\varphi = (\varphi_1 + \varphi_2) / 2 = 34^\circ$
- fixed filling factor (average)  $c/d = 57\%$
- varying  $\varphi_1$  from  $34$  to  $44^\circ$



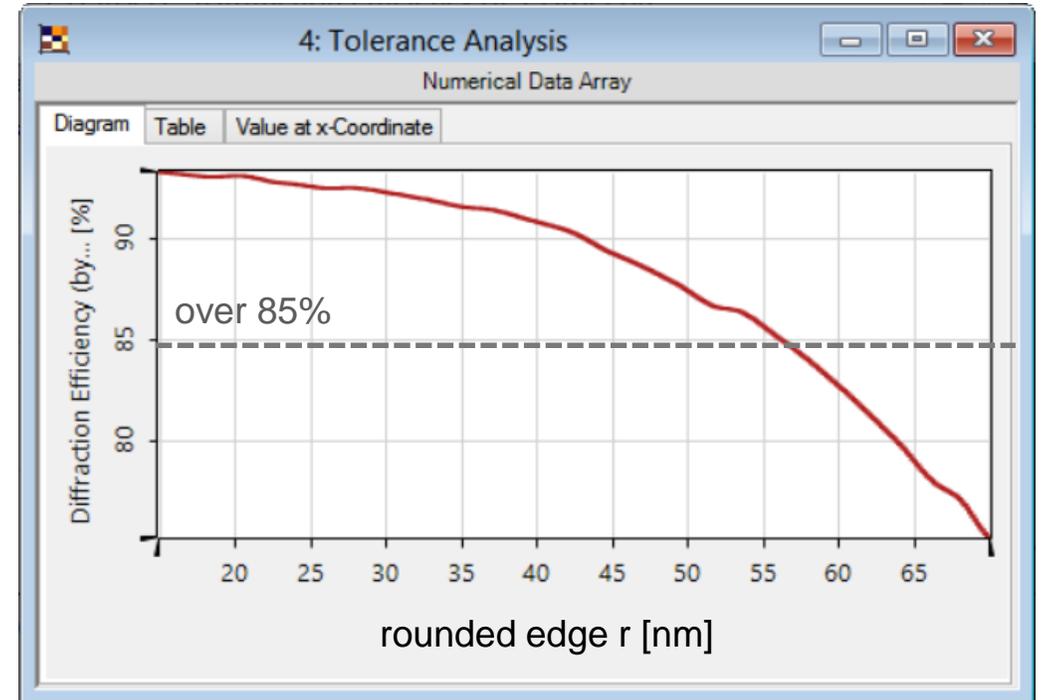
Rigorous simulation with Fourier modal method (FMM), for tolerance analysis over 50 steps, takes 30 seconds.

# Results – Tolerance Analysis

The fabricated slanted gratings often shows a deviation from the perfect parallel grating lines. The rounded edges should be taken into account for the tolerance analysis.



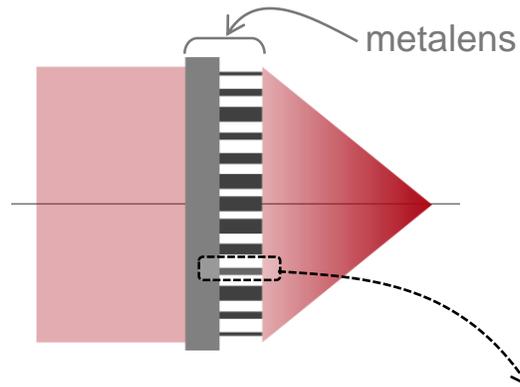
- fixed average slant angle  $\varphi = 34^\circ$
- fixed filling factor  $c/d = 57\%$
- varying  $r$  from 15nm 70nm



Rigorous simulation with **Integral Method (IM)**, for tolerance analysis over 30 steps, takes 9 seconds.

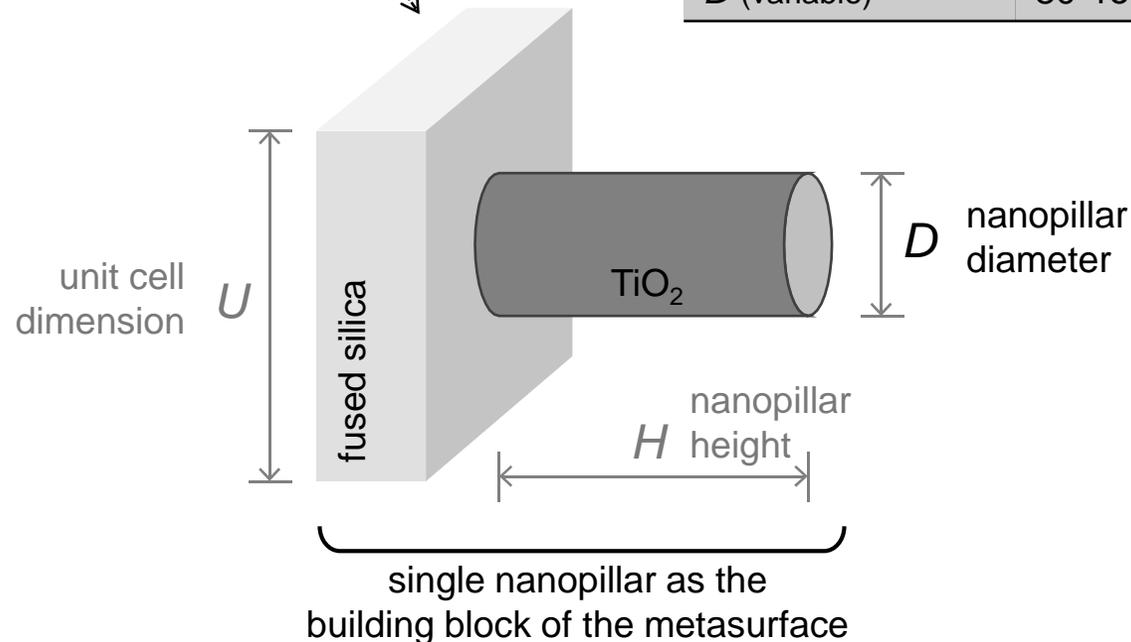
# **Rigorous Analysis of Nanopillar Metasurface Building Block**

# Modeling Task



parameters from M. Khorasaninejad,  
*Nano Lett.* 2016, 16, 7229-7234

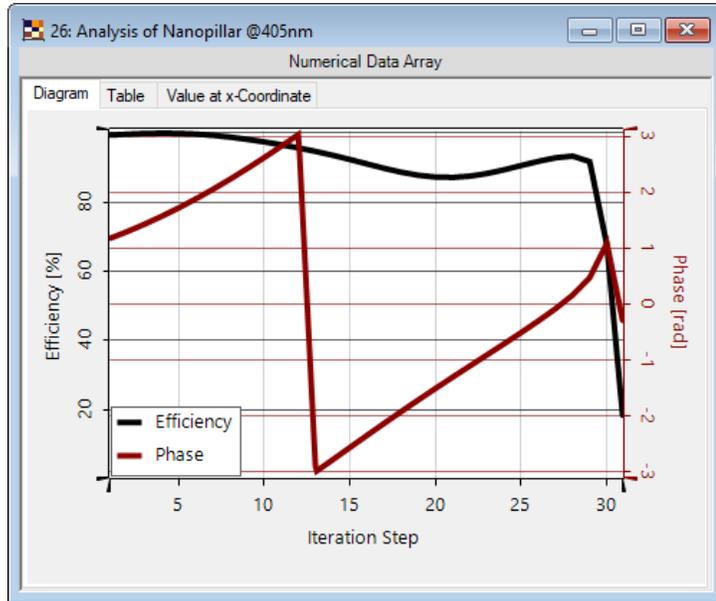
Nanopillars No.	#1 (405nm)	#2 (532nm)	#3 (660nm)
$U$	180nm	250nm	350nm
$H$	400nm	600nm	600nm
$D$ (variable)	80-155nm	100-220nm	100-320nm



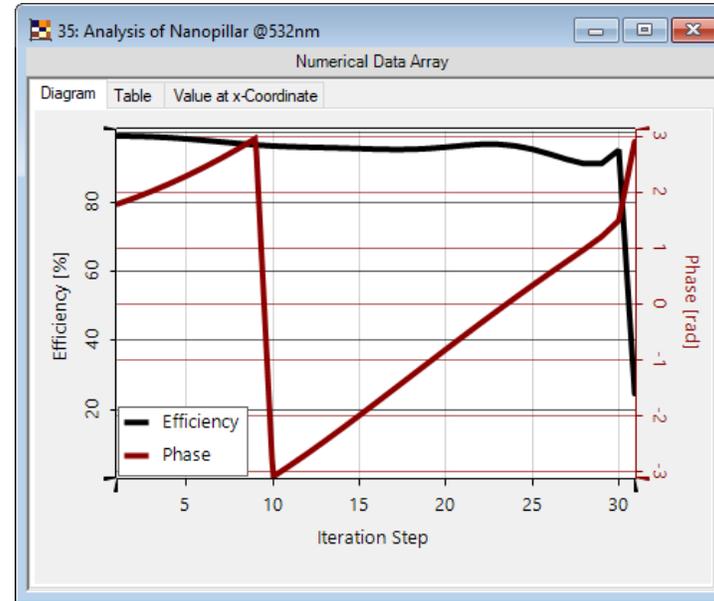
By varying the nanopillar diameter, the metasurface building block is supposed to have phase modulation covering  $2\pi$ . How to evaluate such nanopillar structure rigorously?

# Nanopillar Analysis vs. Pillar Diameter

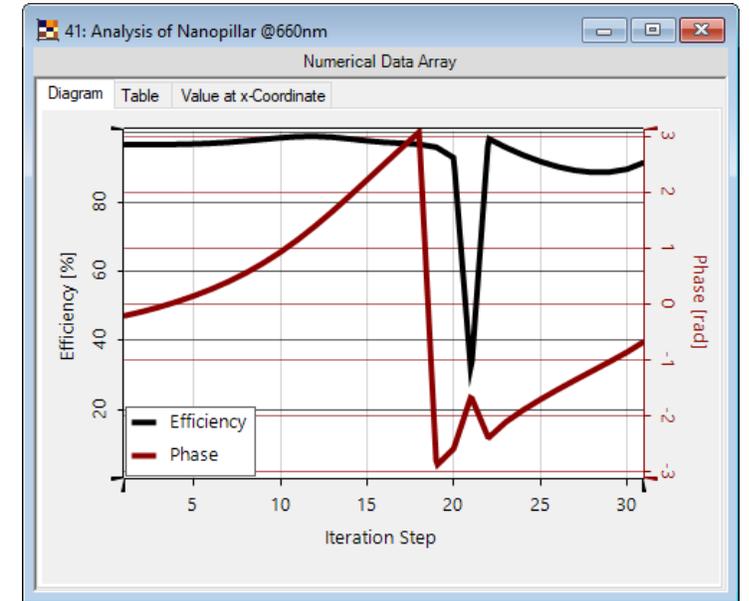
nanopillar #1



nanopillar #2



nanopillar #3



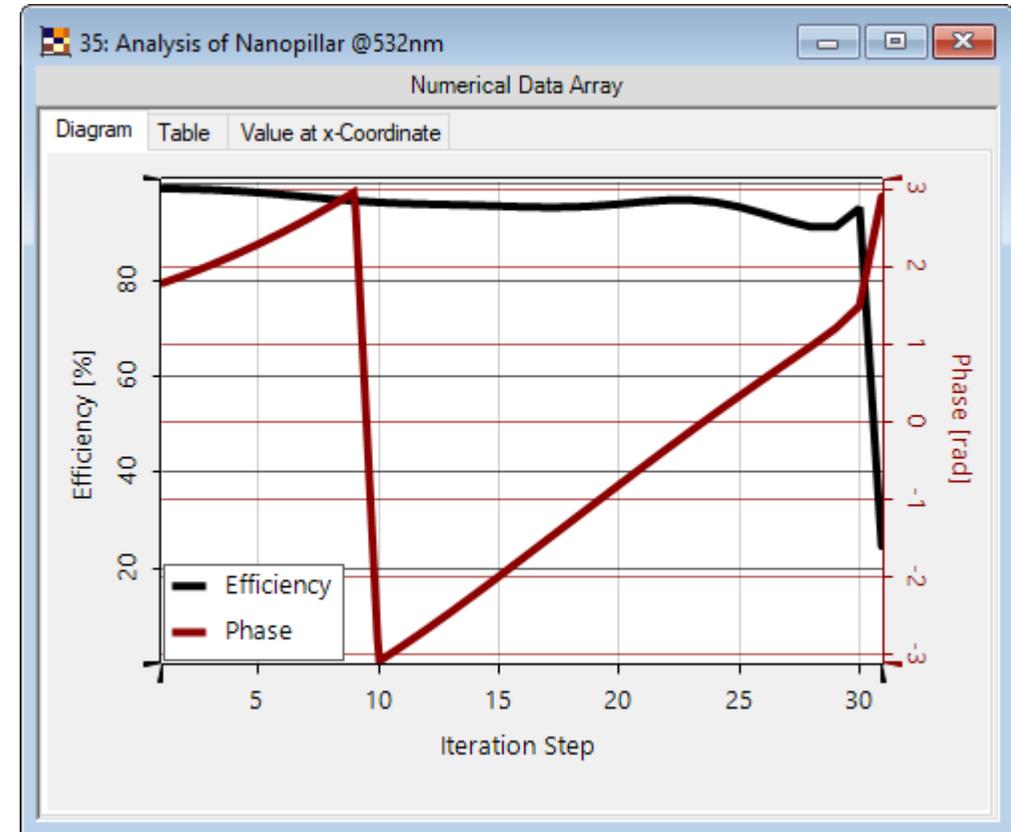
Nanopillars No.	#1 (405nm)	#2 (532nm)	#3 (660nm)
<i>U</i>	180nm	250nm	350nm
<i>H</i>	400nm	600nm	600nm
<i>D</i> (variable)	80-155nm	100-220nm	100-320nm

# Nanopillar Analysis vs. Pillar Diameter

- The phase modulation covers  $2\pi$  range, and it changes almost linearly with pillar diameter, which enables convenient phase control.
- The transmission efficiency remains above 90% for varying pillar diameter over the design range.

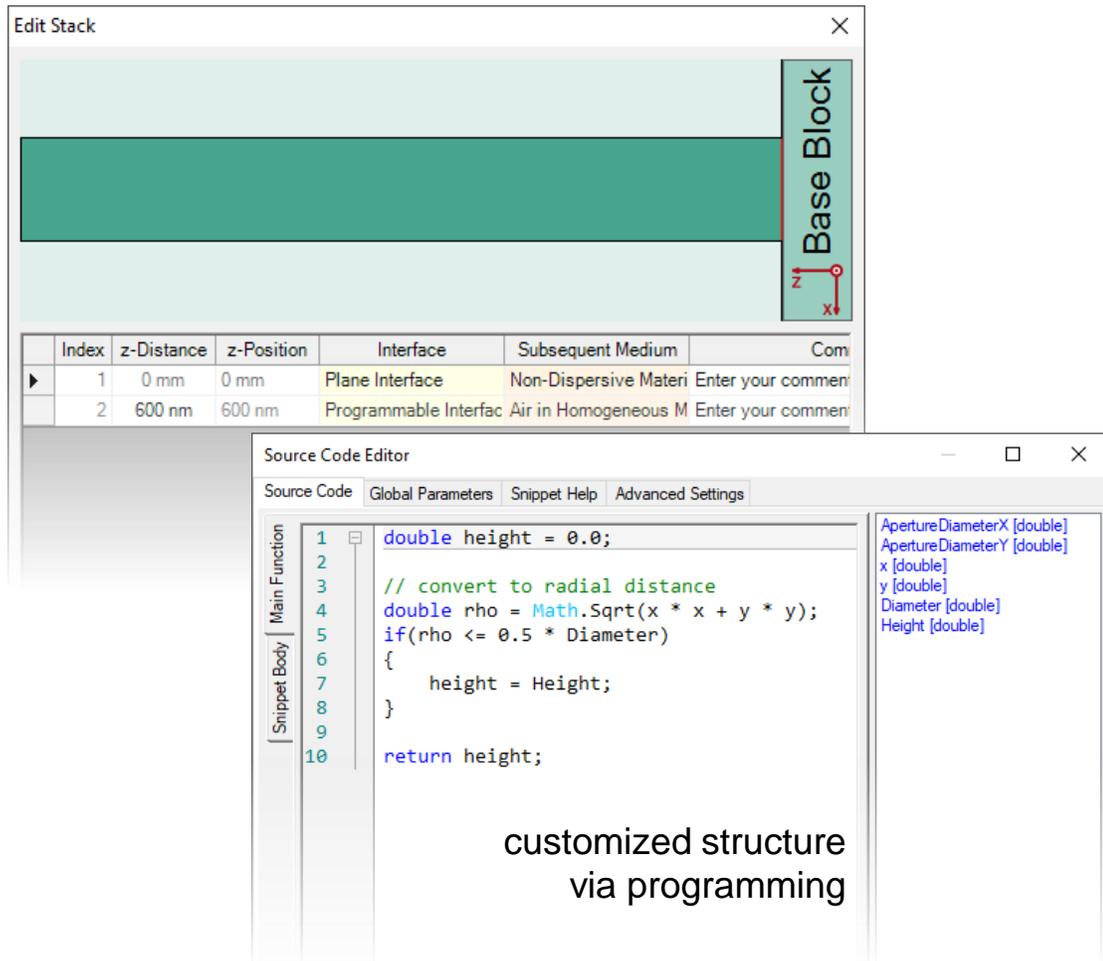
Nanopillars No.	#1 (405nm)	#2 (532nm)	#3 (660nm)
<i>U</i>	180nm	250nm	350nm
<i>H</i>	400nm	600nm	600nm
<i>D</i> (variable)	80-155nm	100-220nm	100-320nm

nanopillar #2



# Peek into VirtualLab Fusion

flexible pillar structure definition



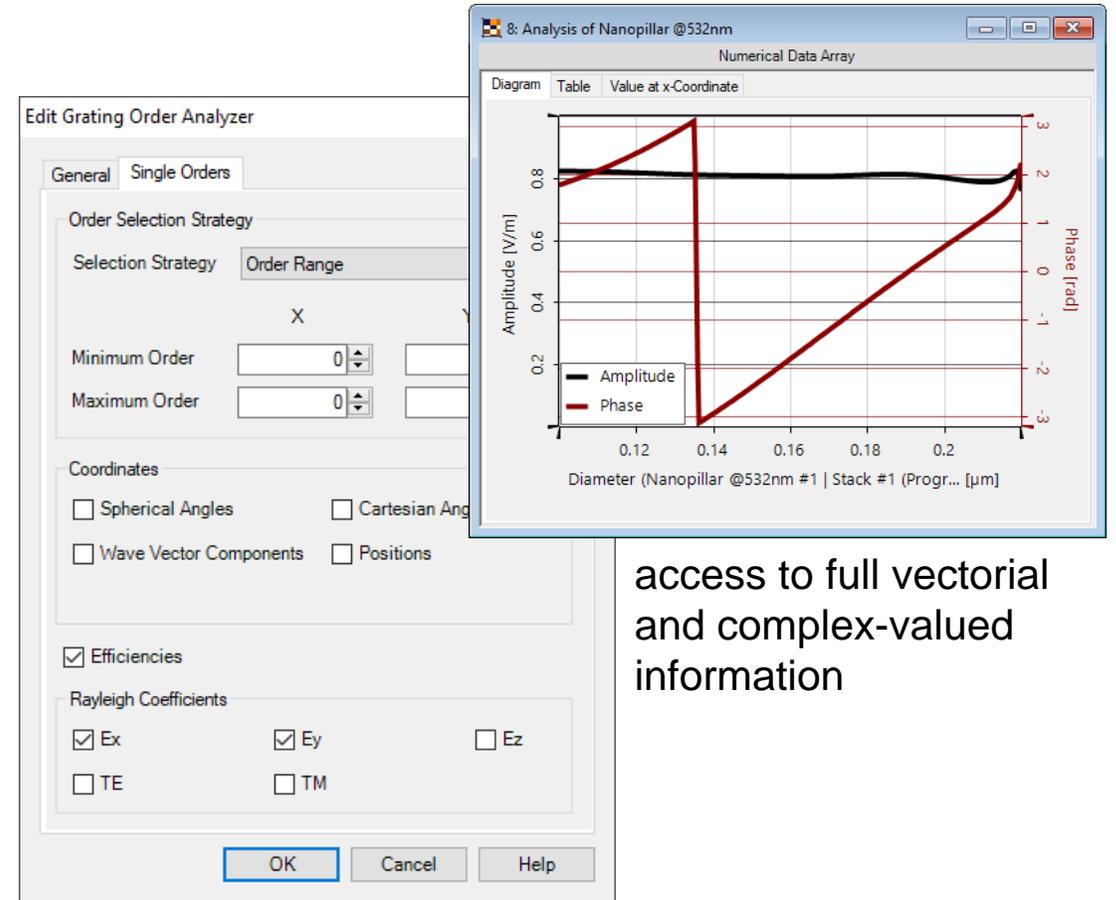
The screenshot displays two windows from the VirtualLab Fusion interface. The top window, titled "Edit Stack", shows a 3D stack of layers. The bottom layer is highlighted in green and labeled "Base Block". Below the 3D view is a table with the following data:

Index	z-Distance	z-Position	Interface	Subsequent Medium	Comments
1	0 mm	0 mm	Plane Interface	Non-Dispersive Materi	Enter your comment
2	600 nm	600 nm	Programmable Interfac	Air in Homogeneous M	Enter your comment

The bottom window is the "Source Code Editor", showing a C# script for defining a pillar structure:

```
1 double height = 0.0;
2
3 // convert to radial distance
4 double rho = Math.Sqrt(x * x + y * y);
5 if(rho <= 0.5 * Diameter)
6 {
7     height = Height;
8 }
9
10 return height;
```

Customized structure via programming



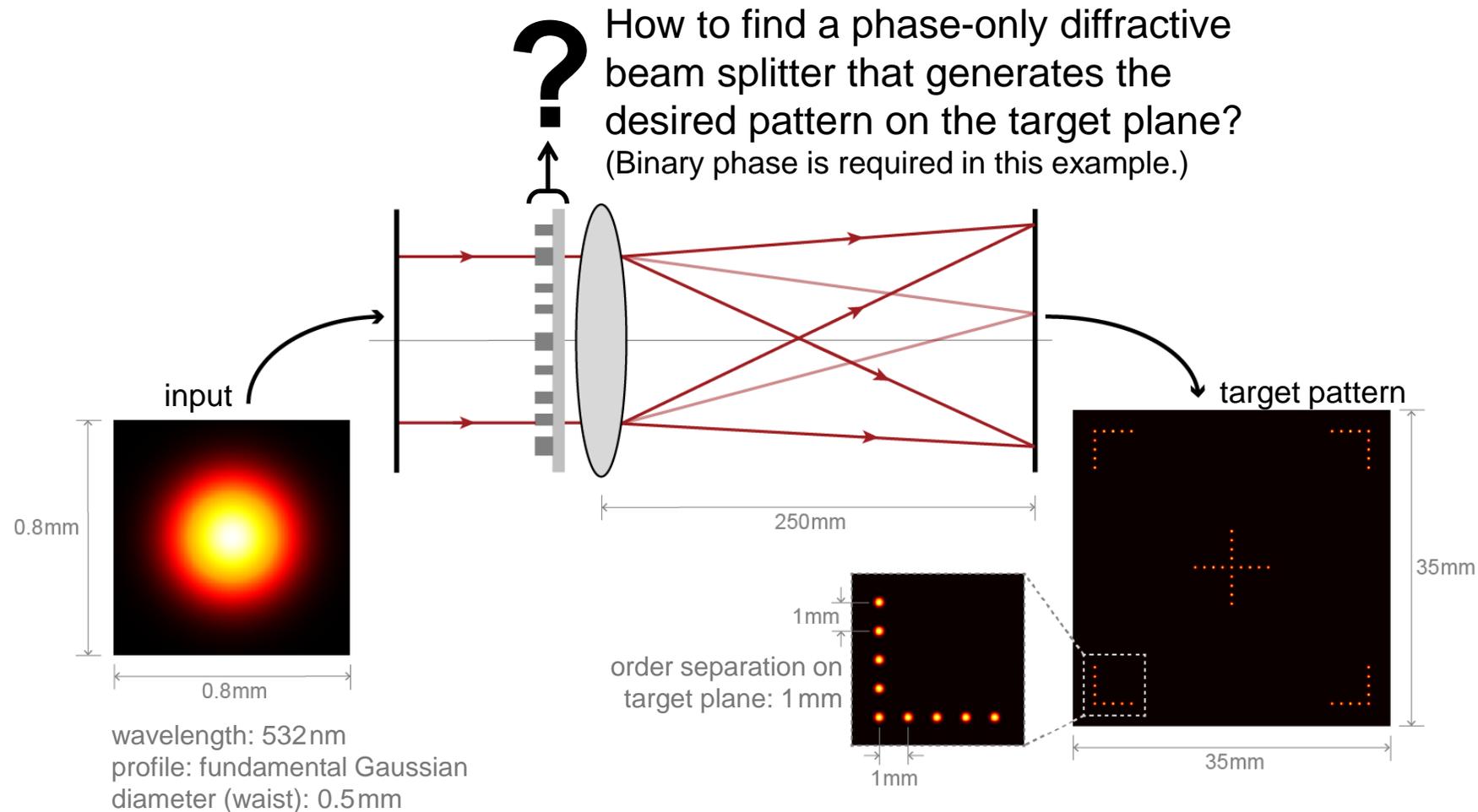
The screenshot displays two windows from the VirtualLab Fusion interface. The left window is the "Edit Grating Order Analyzer" dialog box, showing the "Single Orders" tab. The "Order Selection Strategy" is set to "Order Range". The "Minimum Order" and "Maximum Order" are both set to 0. The "Coordinates" section has "Spherical Angles" and "Cartesian Ang" checked. The "Efficiencies" section has "Ex", "Ey", and "Ez" checked. The "Rayleigh Coefficients" section has "TE" and "TM" checked. The "OK" button is highlighted.

The right window is a "Numerical Data Array" plot showing "Amplitude [V/m]" on the left y-axis (0.2 to 0.8) and "Phase [rad]" on the right y-axis (-3 to 3). The x-axis is "Diameter (Nanopillar @532nm #1 | Stack #1 (Progr... [μm])" (0.12 to 0.2). The plot shows a black line for Amplitude and a red line for Phase. A vertical red line is drawn at approximately 0.135 μm diameter.

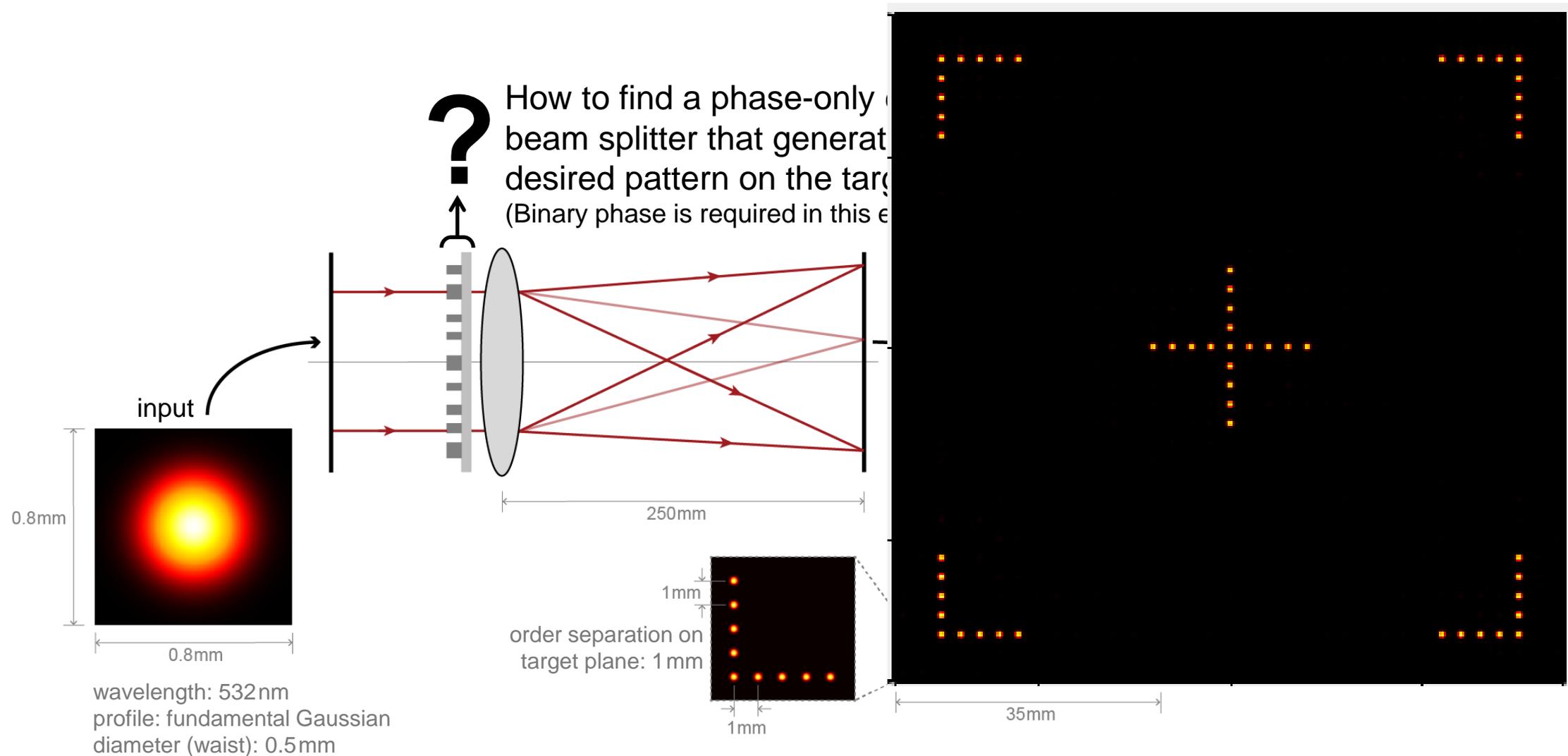
access to full vectorial and complex-valued information

# **Design of Diffractive Beam Splitters for Generating a 2D Light Mark**

# Design Task

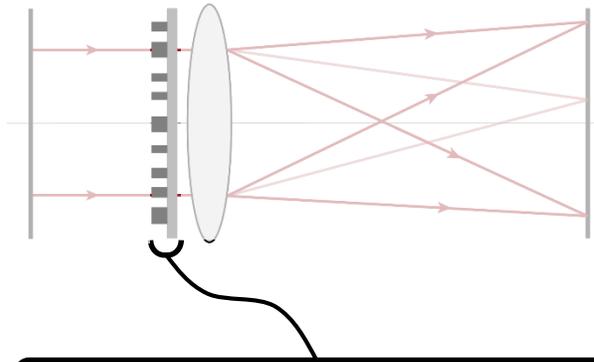


# Design Task

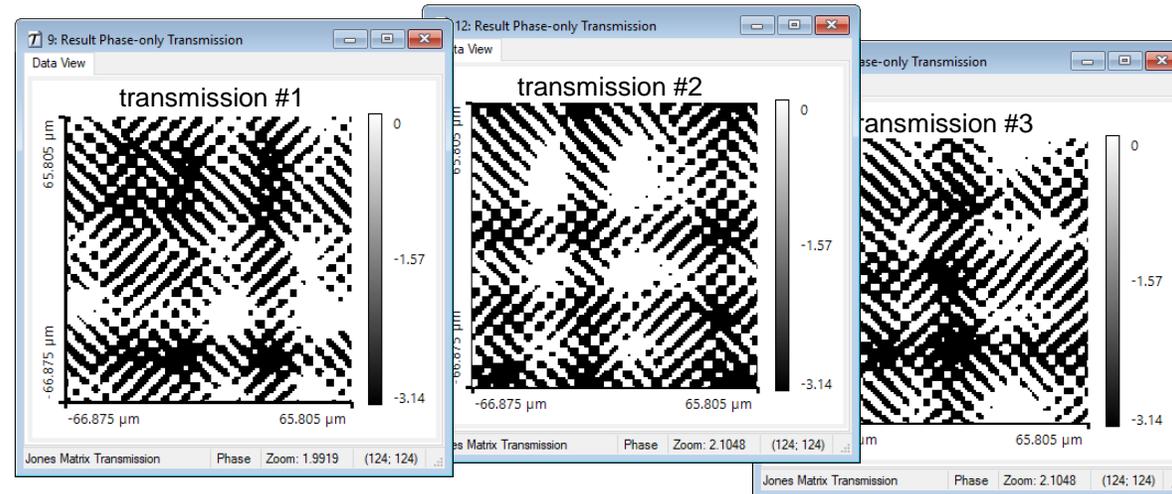


# Results

- Designed binary-phase for beam splitter



Beginning with different random phase distributions on the target plane, the iterative Fourier transform algorithm (IFTA) calculates different possible design results.

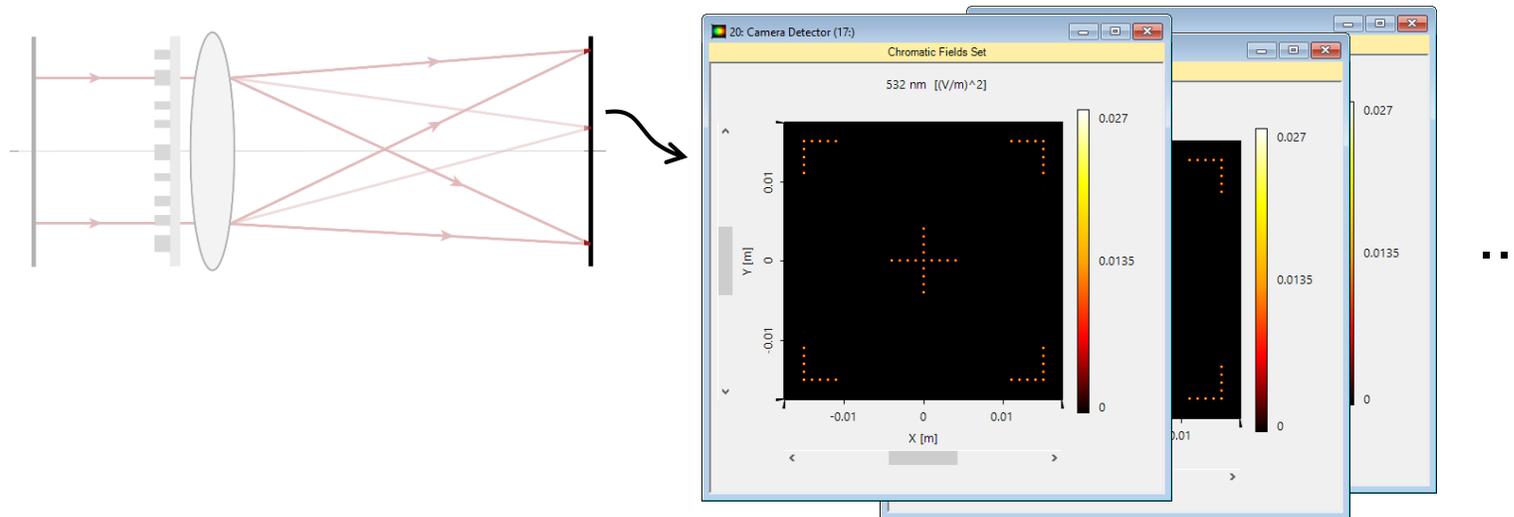


...

100 designs delivered  
within 200 seconds!  
(2 seconds per design)

# Results

- Performance evaluation

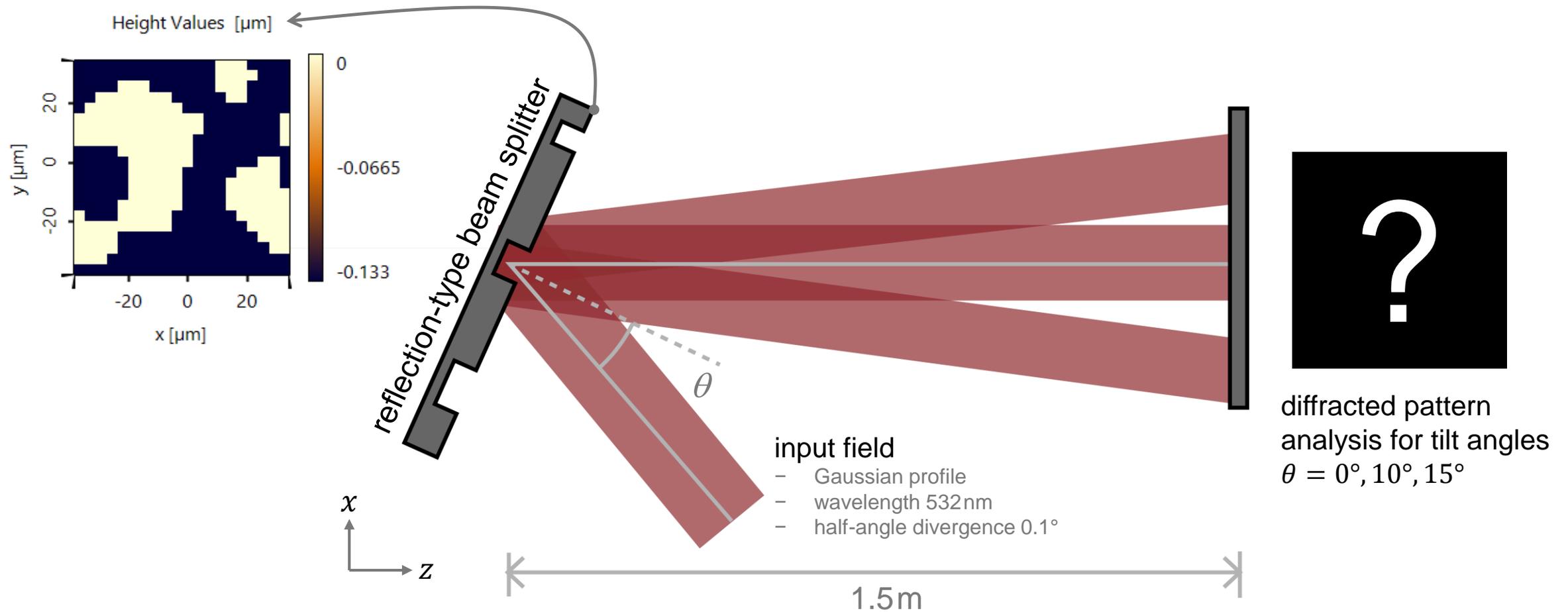


Fast physical-optics simulation of the complete optical system gives access to multiple merit functions at once.

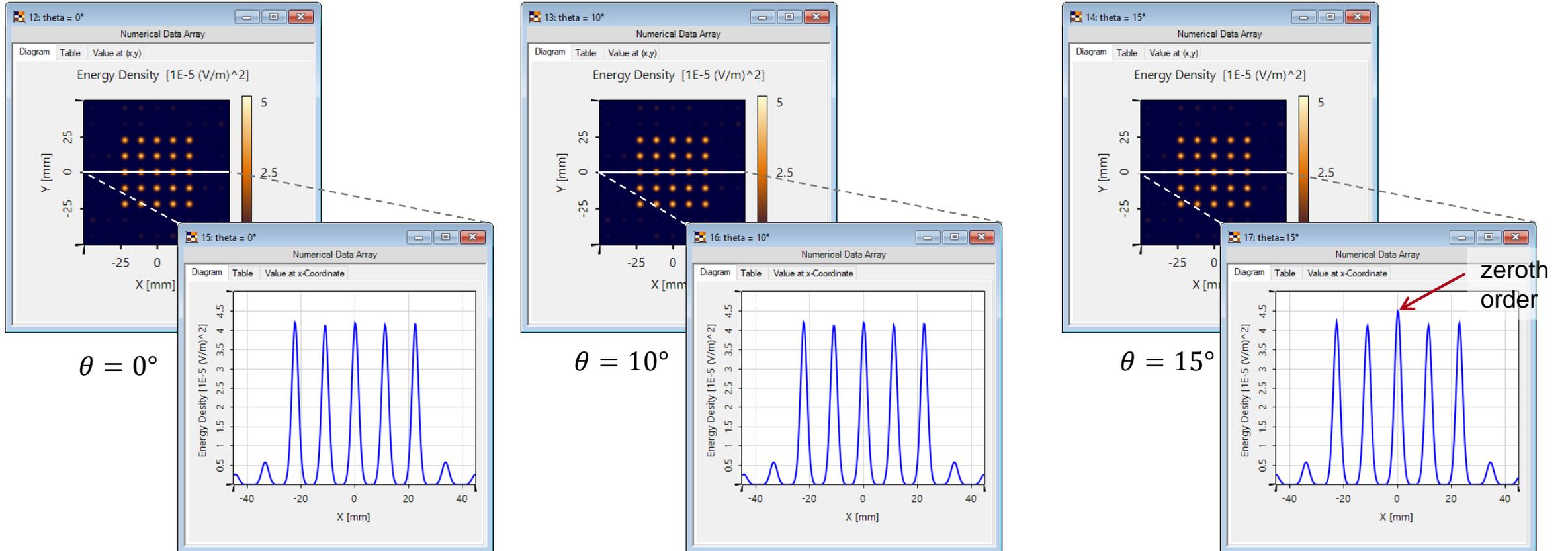
Merit functions	Design #1	Design #2	Design #3	...
conversion efficiency	65.92%	66.38%	64.71%	
uniformity error	4.31%	3.69%	6.76%	
stray light	3.99%	5.17%	3.11%	

# **Diffraction Pattern Calculation from a Reflection-Type Diffractive Beam Splitter**

# Modeling Task



# Diffracted Pattern in Detector Plane



$\theta = 0^\circ$

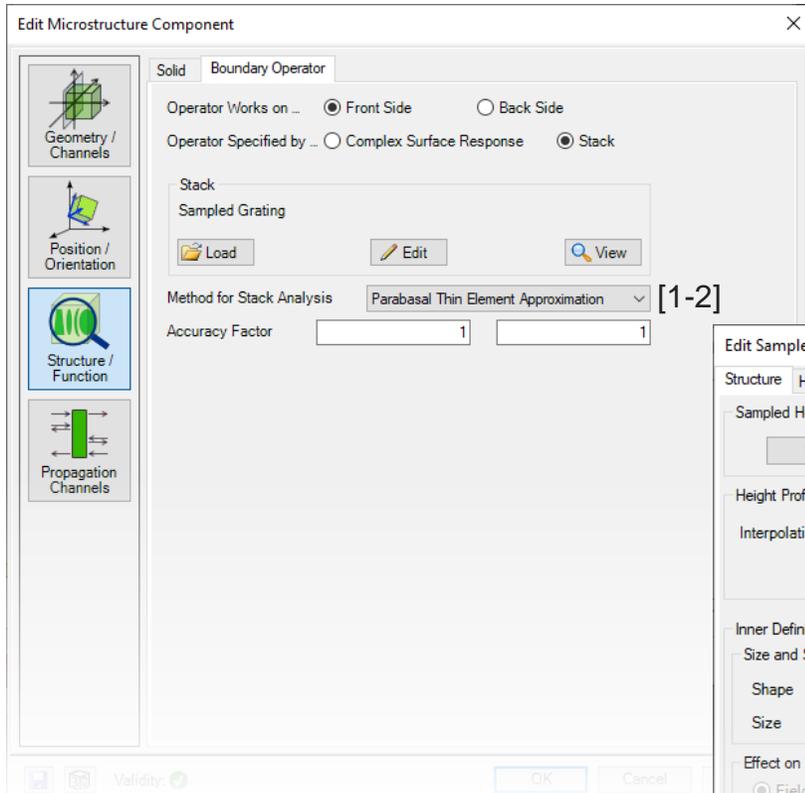
$\theta = 10^\circ$

$\theta = 15^\circ$

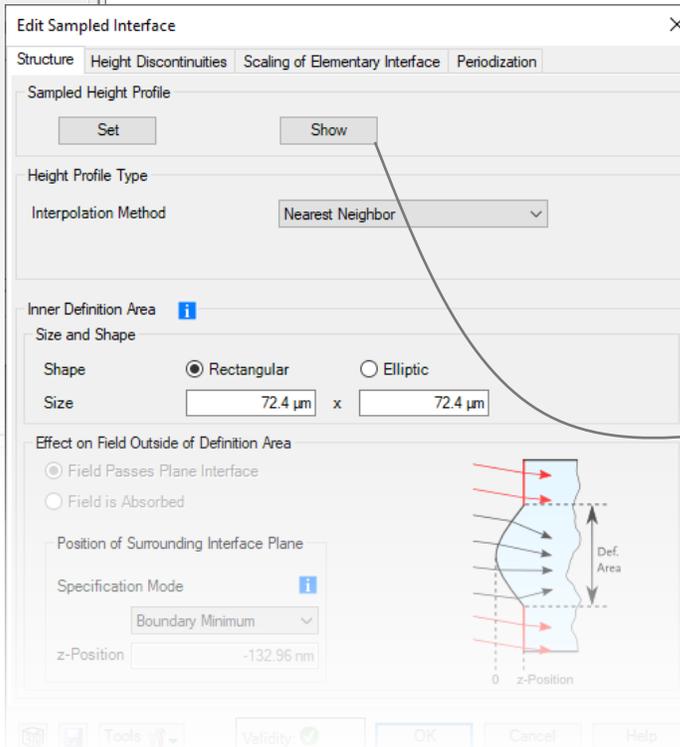
The beam splitter is designed under normal incidence, and for small angle ( $< 10^\circ$ ) it delivers uniformly split diffraction orders.

The efficiency of zeroth order exceeds other orders, when  $\theta$  increases to  $15^\circ$ . Such situation shall be avoided in practice.

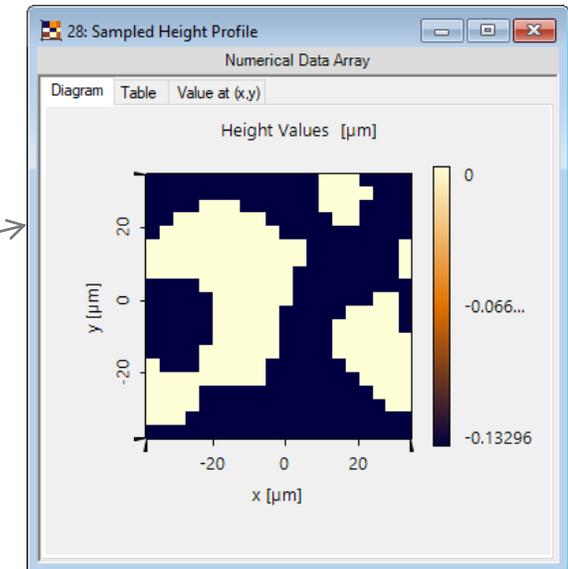
# Peek into VirtualLab Fusion



Microstructure Component is used to configure the diffractive beam splitter.



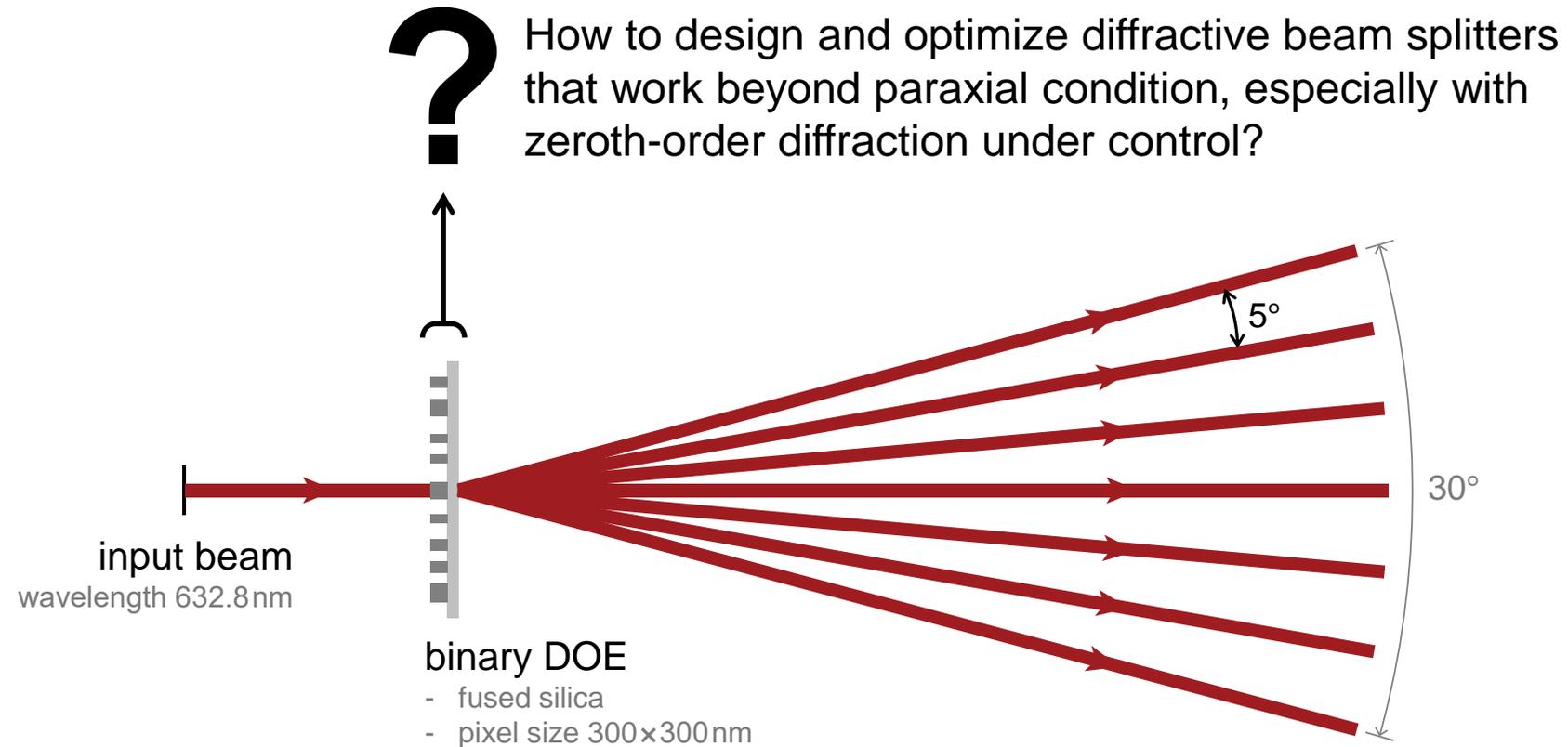
The microstructure can be defined by an imported data matrix.



- [1] Jari Turunen *et al.*, "Storage of multiple images in a thin synthetic Fourier hologram," *Optics Communications*, **84**(5-6), 383-392 (1991)  
[2] Huiying Zhong *et al.*, "**Parabasal thin-element approximation approach** for the analysis of microstructured interfaces and freeform surfaces," *J. Opt. Soc. Am. A* **32**, 124-129 (2015)

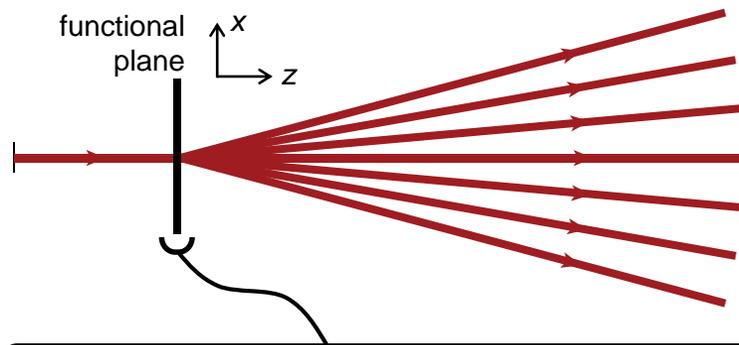
# **Design and Rigorous Analysis of Non-Paraxial Diffractive Beam Splitter**

# Design Task

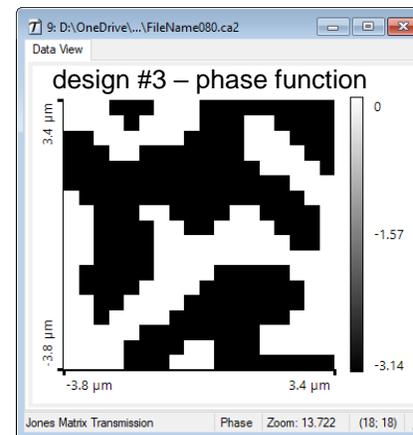
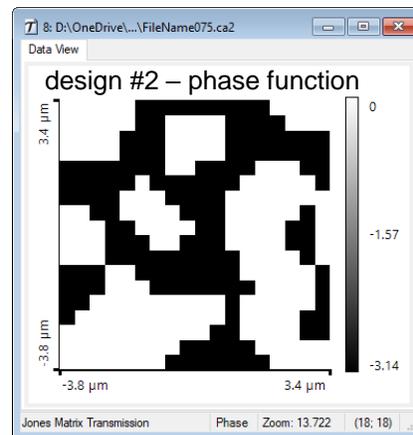
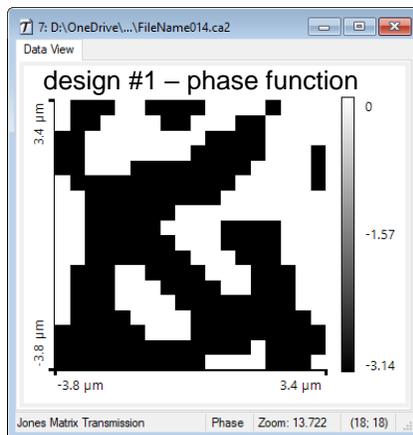


# Results

- Phase-only transmission design  
[with iterative Fourier transform algorithm (IFTA)]



With differently random phase distributions as starting points, IFTA calculates different possible design results. 3 designs are selected out of 100 according to customized criteria.

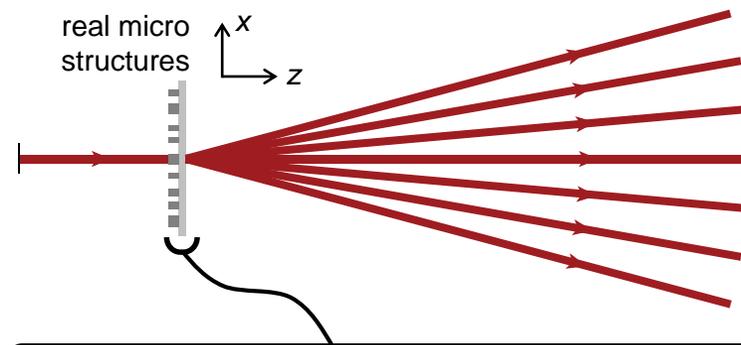


...

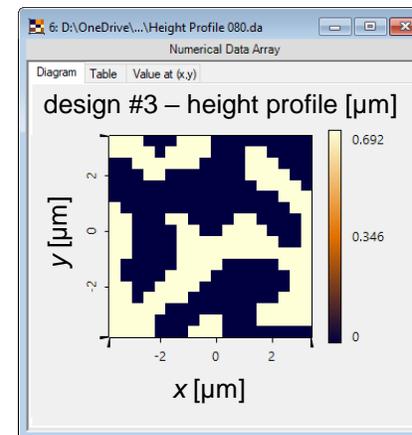
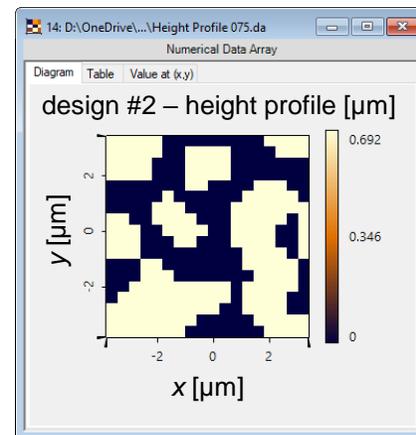
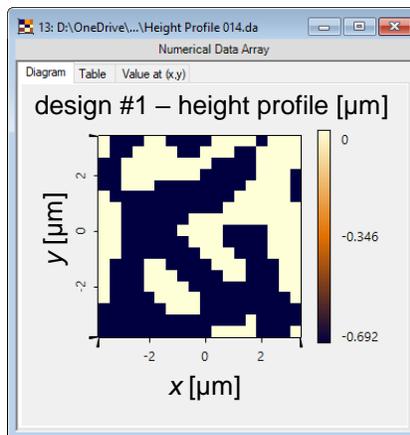
delivery of 100 designs  
within 20 seconds!

# Results

- Structure design  
[with thin-element approximation (TEA)]

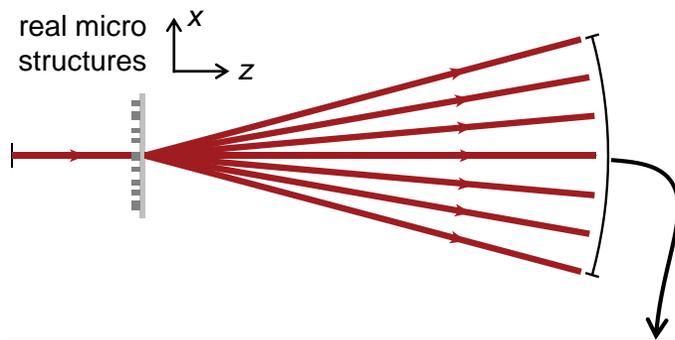


Automatic conversion from phase-only transmission to structure height profile, according to given wavelength and material.

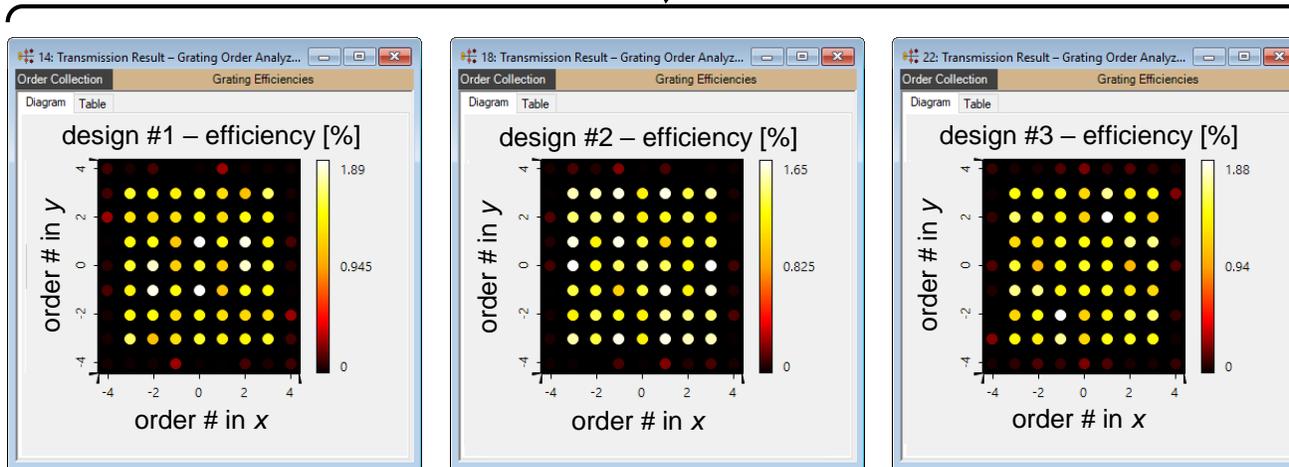


# Results

- Performance evaluation with TEA



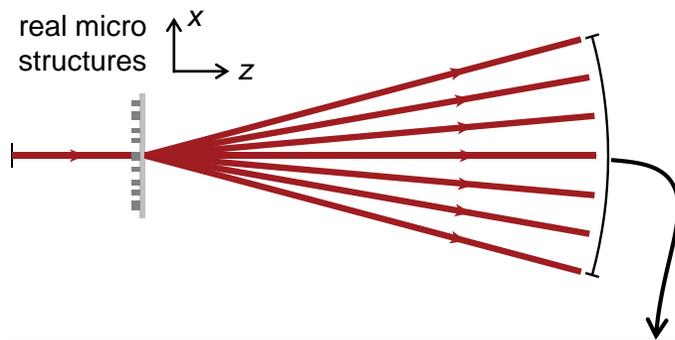
Merit functions	Design #1	Design #2	Design #3
total efficiency	69.057%	68.068%	69.613%
average efficiency	1.4093%	1.3892%	1.4207%
zeroth efficiency (zeroth order error)	1.4888% (5.6374%)	1.4888% (7.1723%)	1.4704% (3.5%)
uniformity error	14.422%	<b>12.266%</b>	12.989%



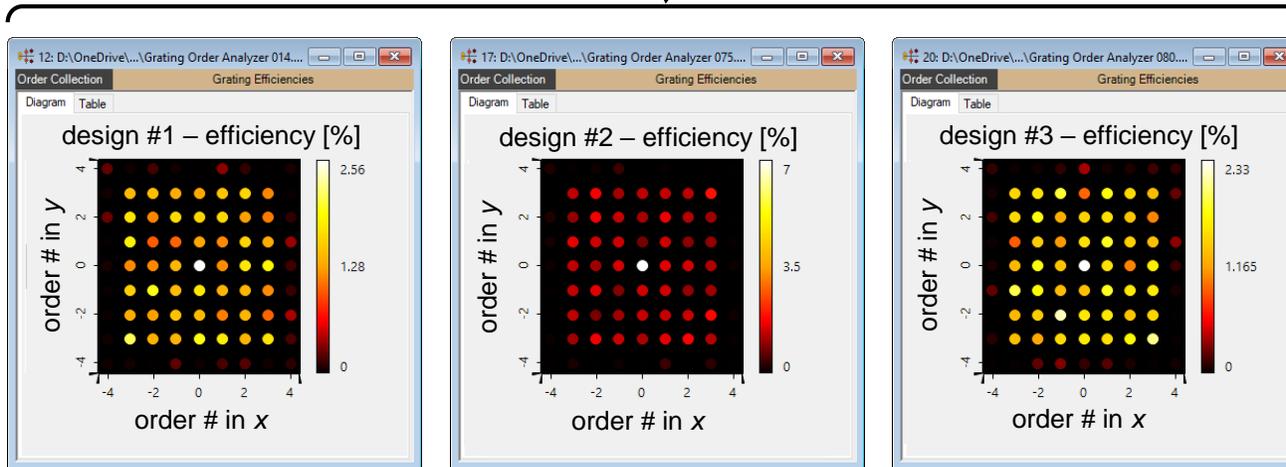
Design #2 seems to give the best uniformity, based on the evaluation results from thin-element approximation. But, is it still true for the non-paraxial situation?

# Results

- Performance evaluation with Fourier modal method



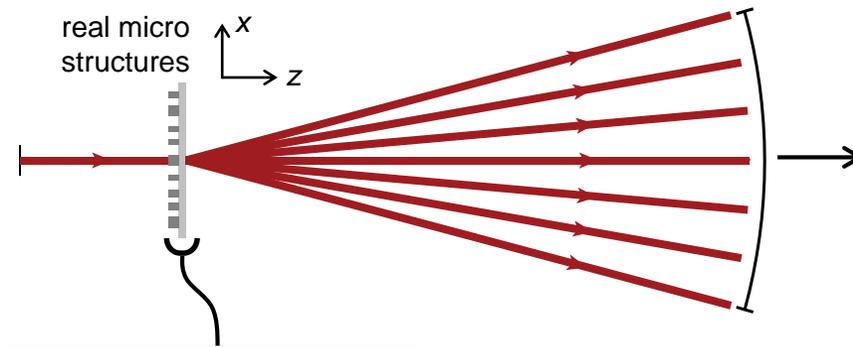
Merit functions	Design #1	Design #2	Design #3
total efficiency	72.122%	70.619%	74.311%
average efficiency	1.4719%	1.4412%	1.5165%
zeroth efficiency (zeroth order error)	2.5574% (73.753%)	7.011% (386.47%)	2.3324% (53.799%)
uniformity error	21.064%	<b>58.431%</b>	18.946%



With the rigorous Fourier modal method (FMM), it turns out that design #2 produces strong zeroth diffraction order, resulting in very poor uniformity in fact.

# Results

- Further optimization – zeroth order tuning

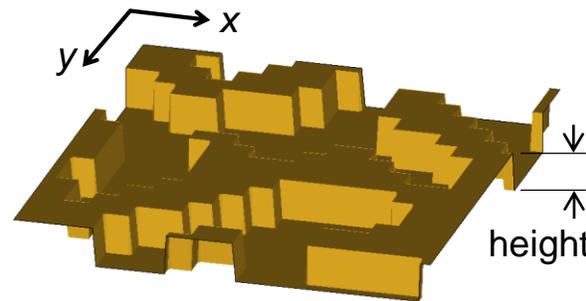
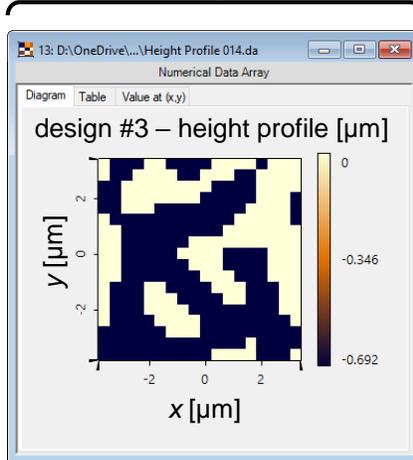


FMM evaluation results

Merit functions	Design #3
total efficiency	74.311%
average efficiency	1.5165%
zeroth efficiency (zeroth order error*)	<b>2.3324%</b> <b>(53.799%)</b>
uniformity error	18.946%

Design #3 gives good overall performance but still produces undesired zeroth order error.

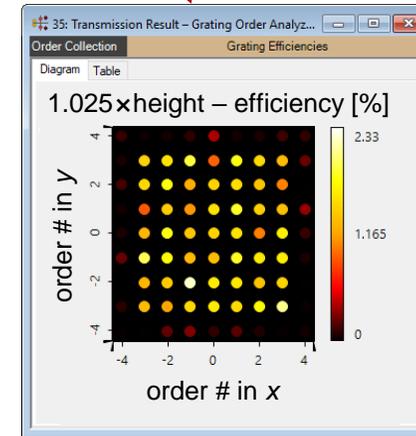
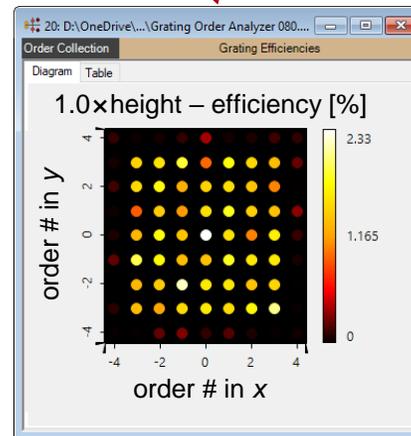
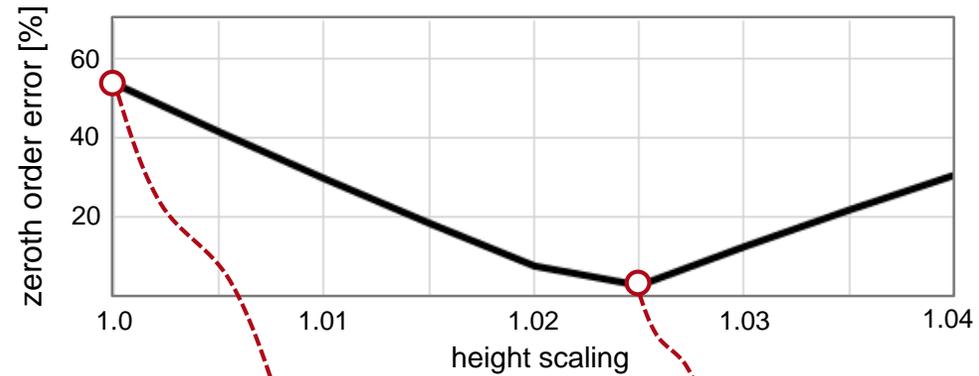
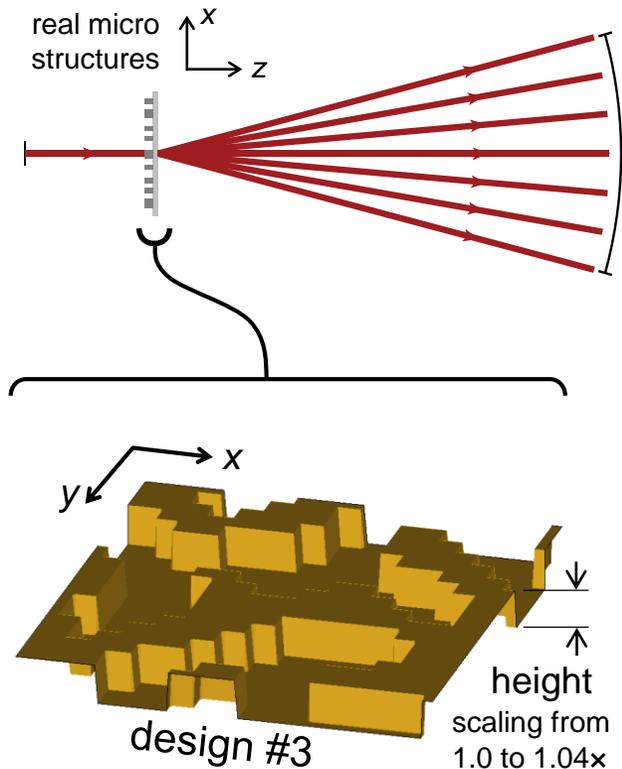
$$*\text{zeroth order error} = \frac{\text{zeroth efficiency} - \text{average efficiency}}{\text{average efficiency}}$$



Sometimes, the zeroth order error can be reduced by tuning the height of the binary structure.

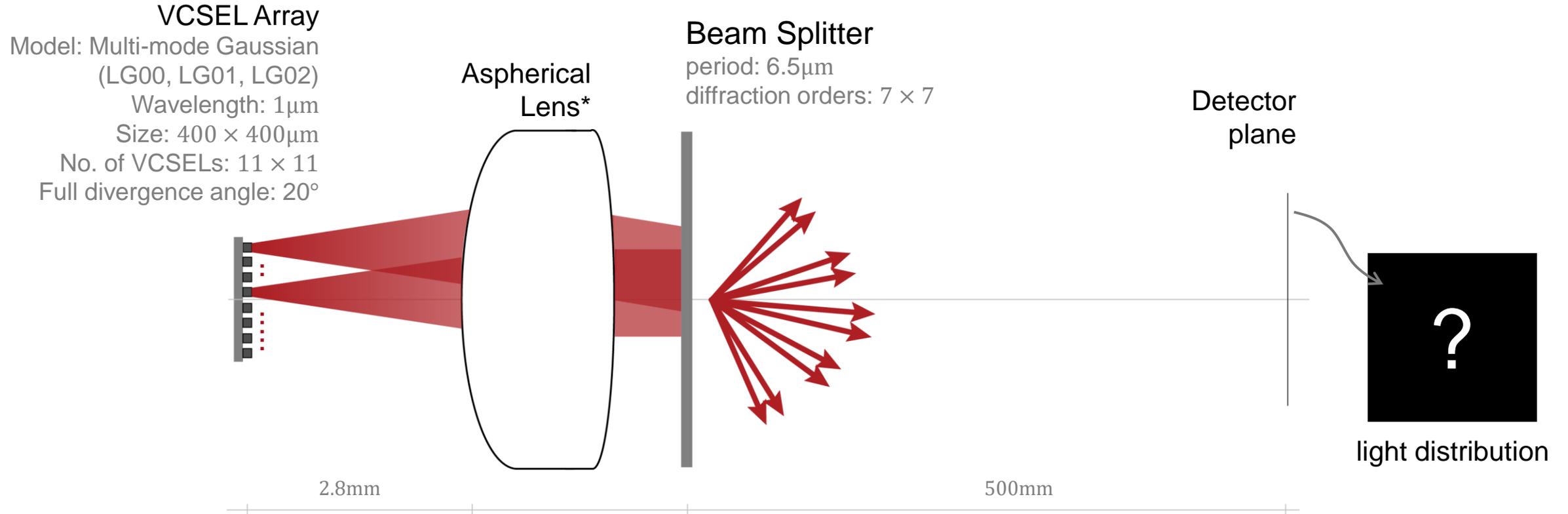
# Results

- Further optimization – zeroth order tuning



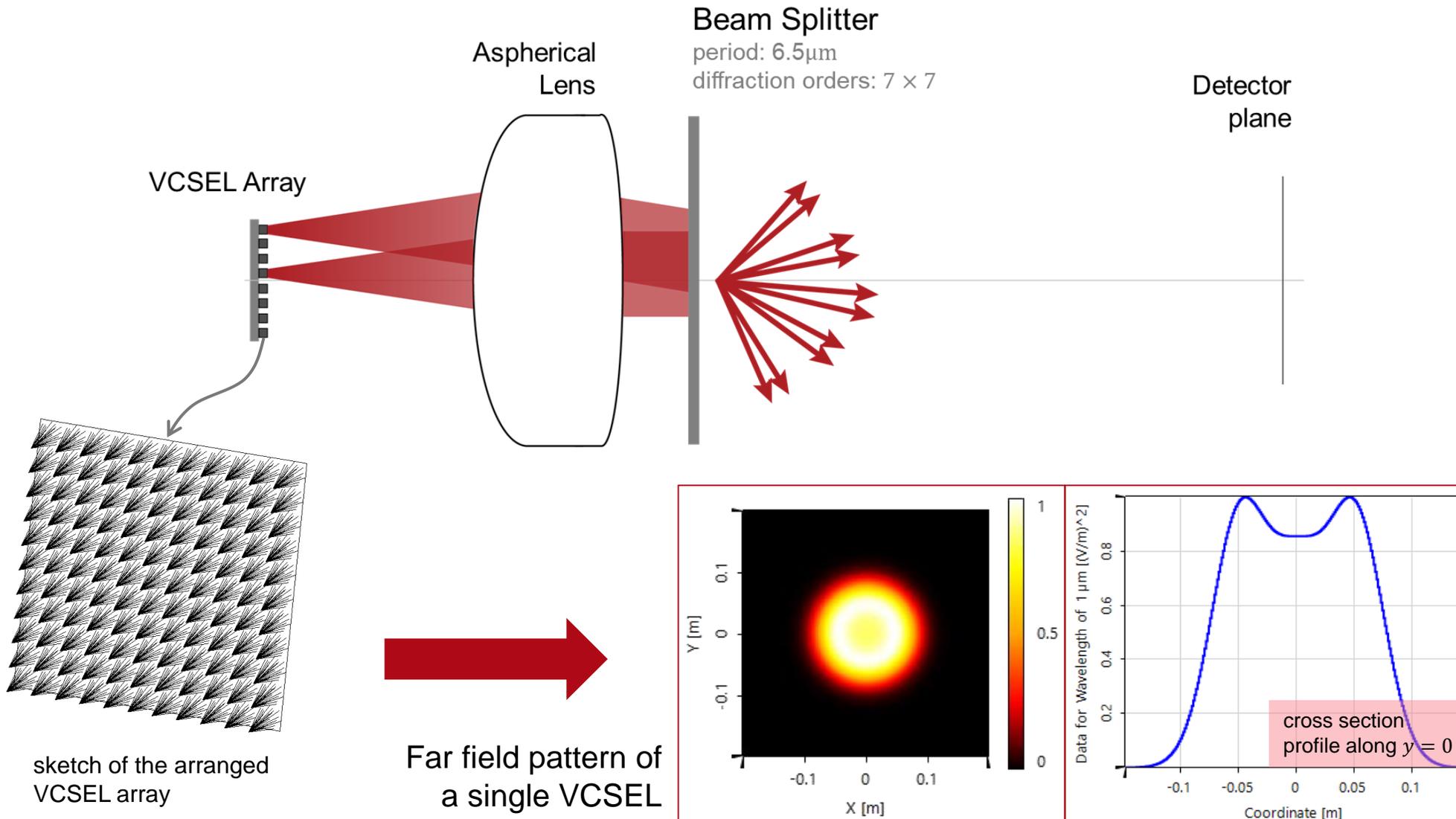
# **Working Principle Demonstration of the Dot Projector with Physical Optics Modeling**

# Modeling Task

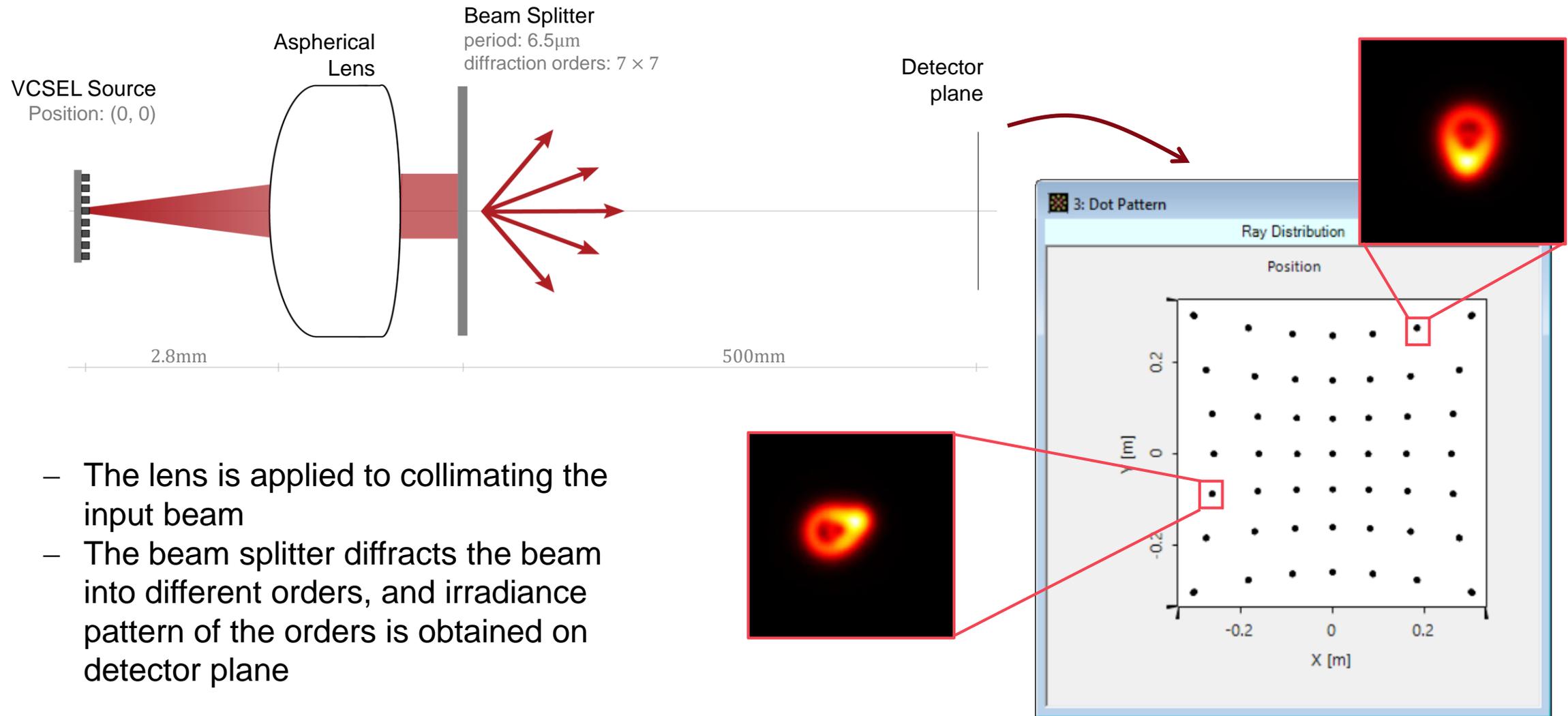


\* The aspherical lens in the document is designed with OpticStudio

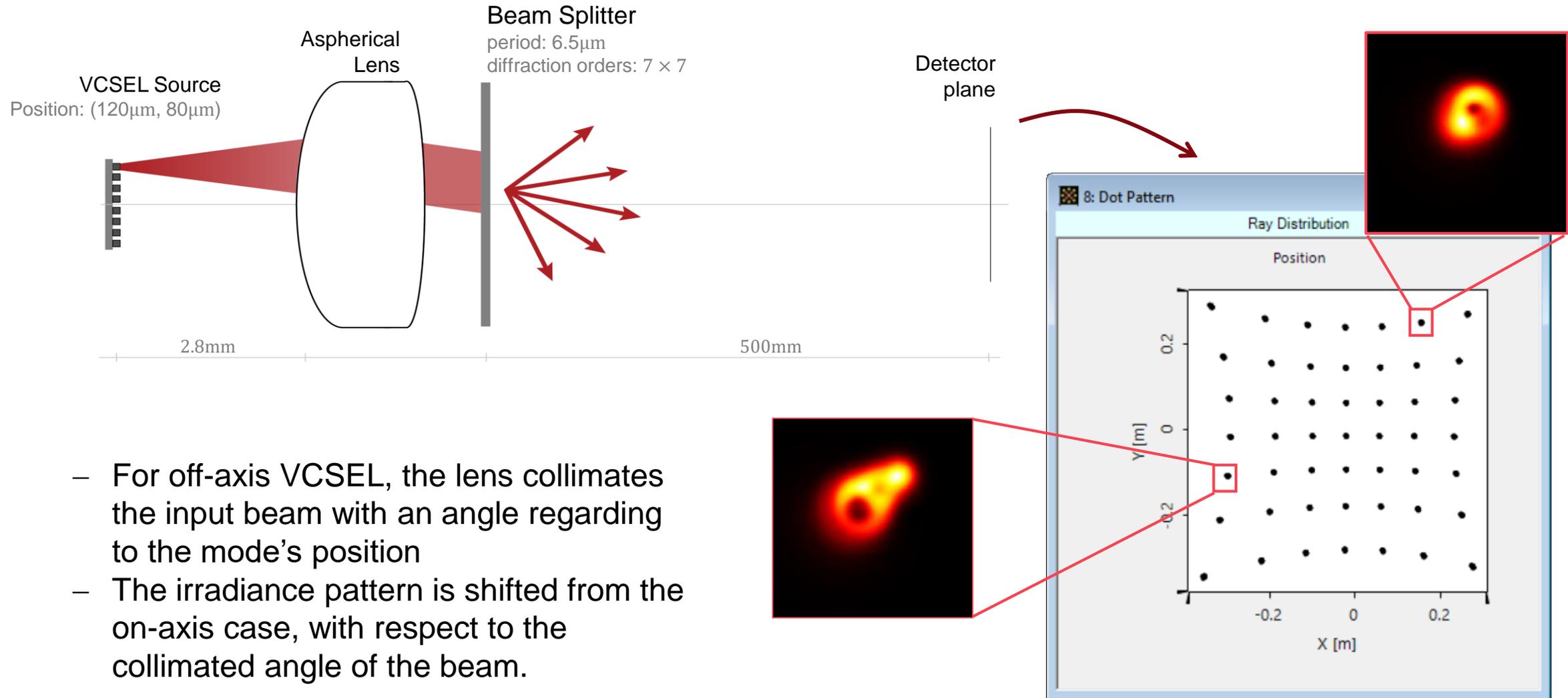
# Source Modeling



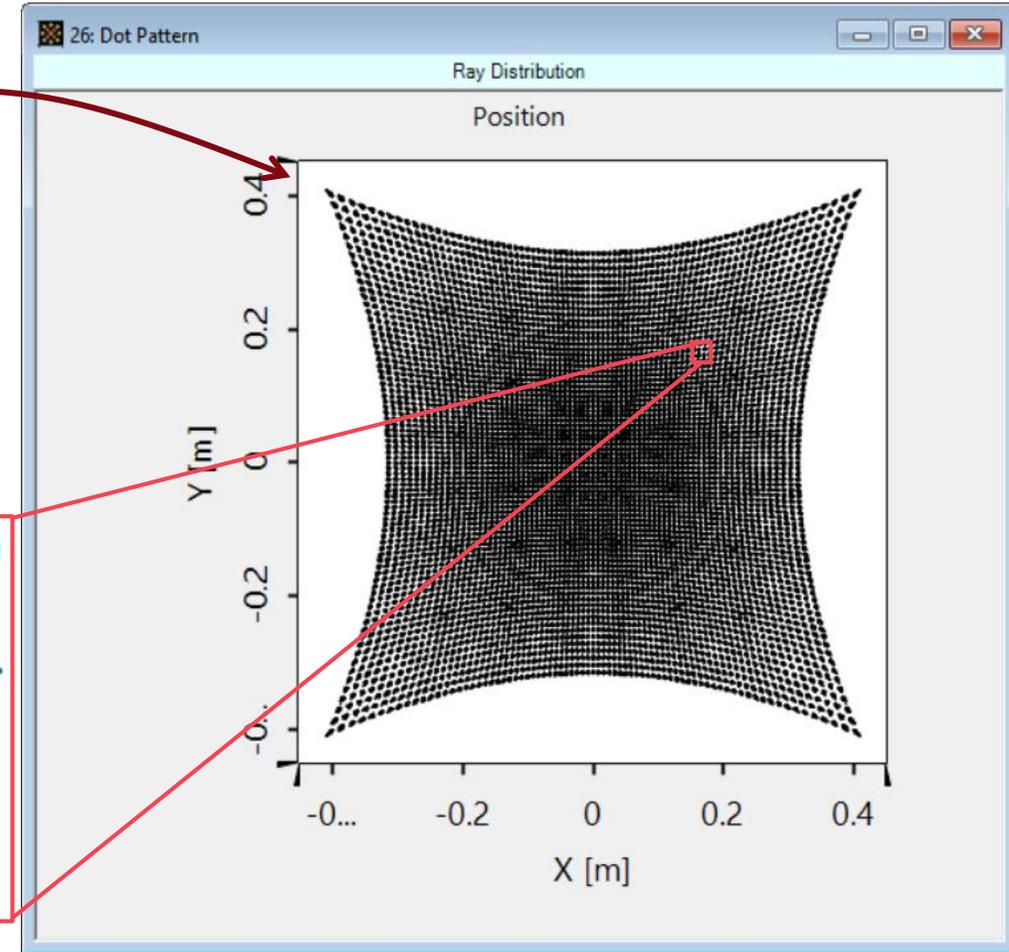
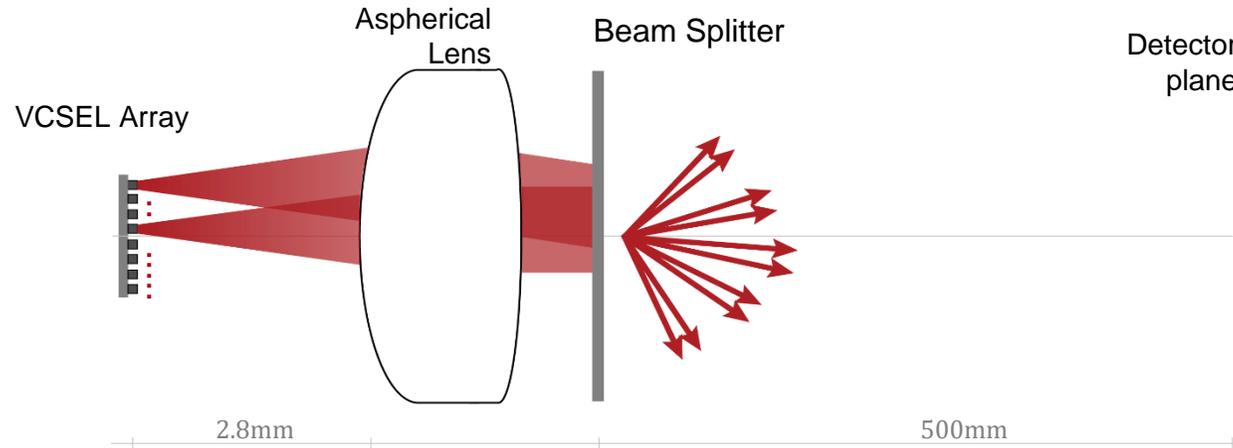
# Simulation with the On-axis VCSEL



# Simulation with an Off-axis VCSEL

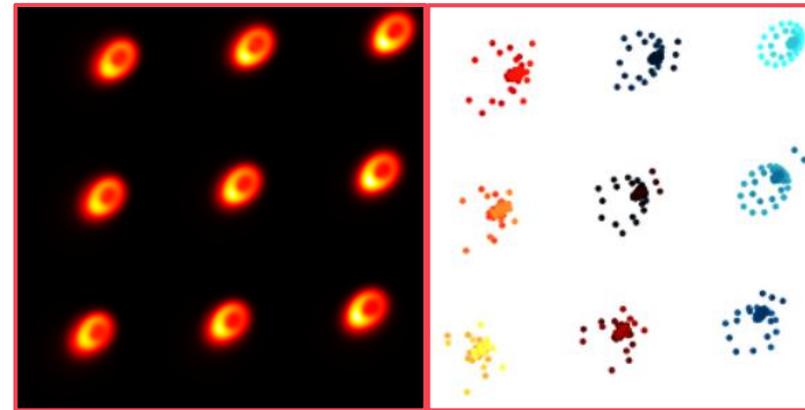


# Simulation with All Modes of the VCSEL Array



## Simulation results

The beam splitter duplicates the irradiance pattern of different VCSELs with a lateral shifted on detector plane, and the whole dot pattern is generated.



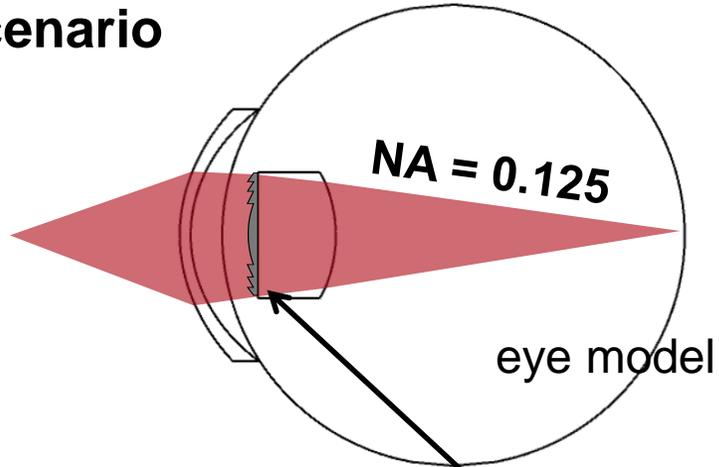
Field Tracing

Ray Tracing

# Design and Analysis of Intraocular Diffractive Lens

# Design Task for a Diffractive Lens

## Near View Scenario

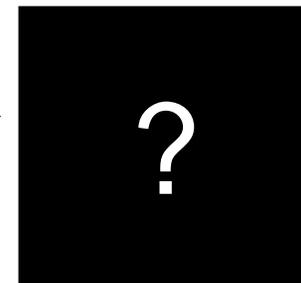
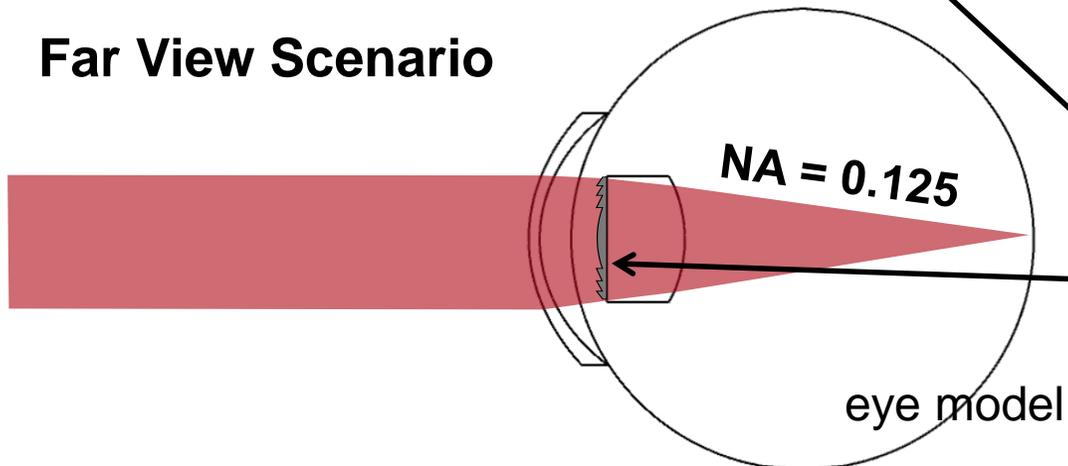


Each configuration of the two intraocular lens requires a certain wavefront surface response function.

$$\Delta\psi(\rho) = m\Delta\psi(\rho)$$

Where  $m = 0$  for the far view scenario and  $m = 1$  for the near view scenario

## Far View Scenario

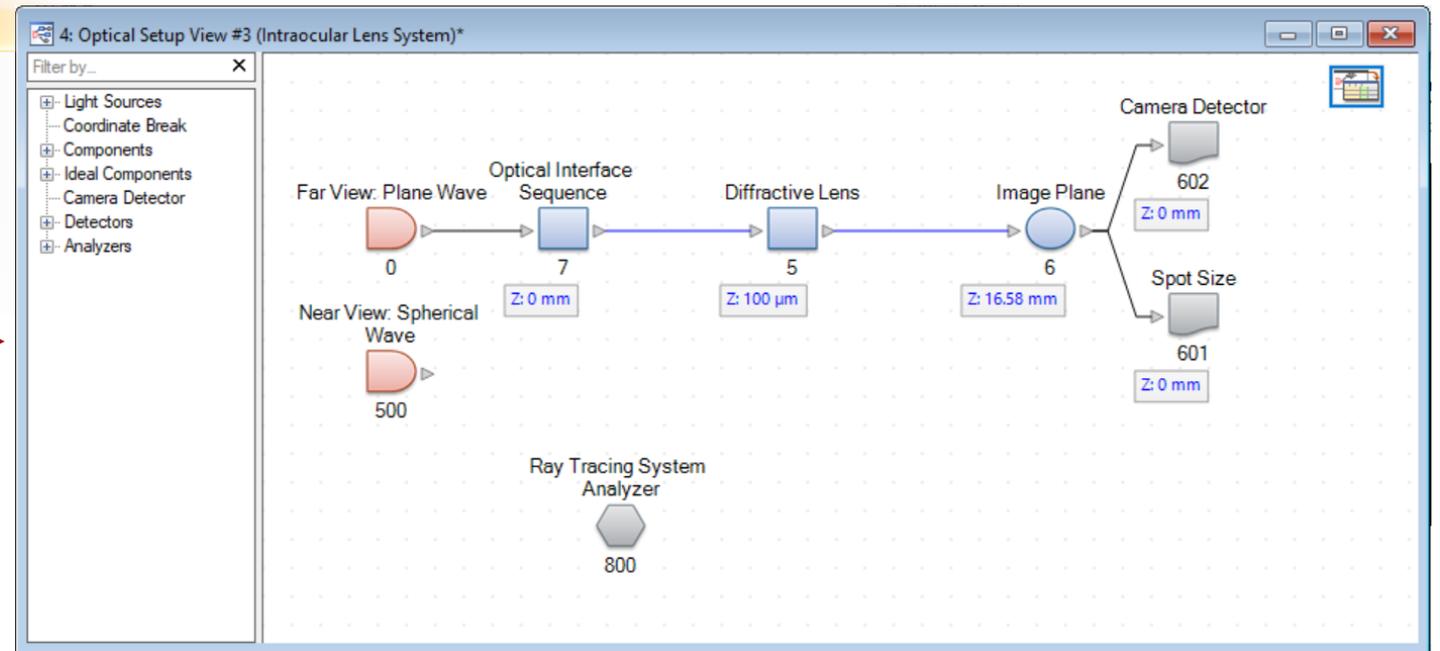
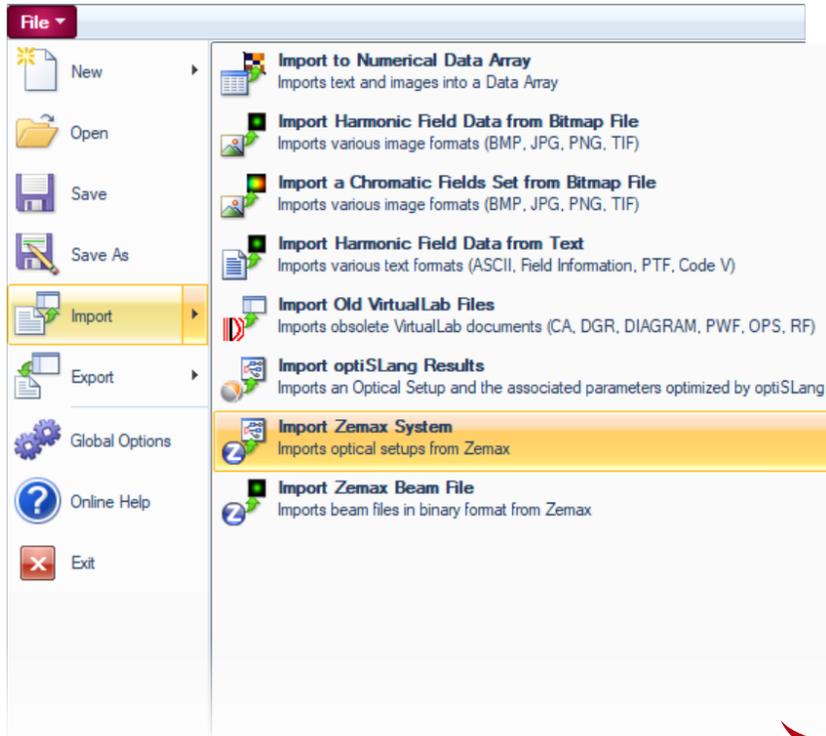


How to design a diffractive lens to achieve different wavefront effects for the two configurations?

# Import of Optical System from OpticStudio

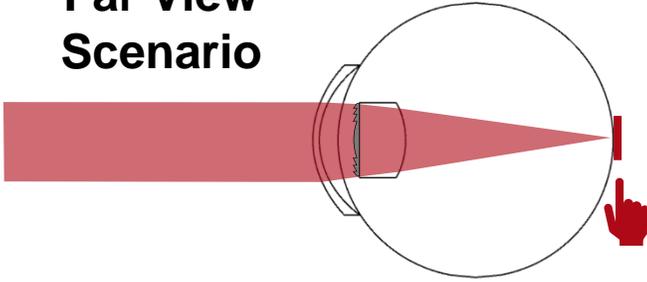
The configuration of the optical setup as well as the design of the wavefront surface response by a Binary-2 surface was generated in OpticStudio.

VirtualLab Fusion provides the capability to import the optical setups and merge them in a single optical setup configuration.



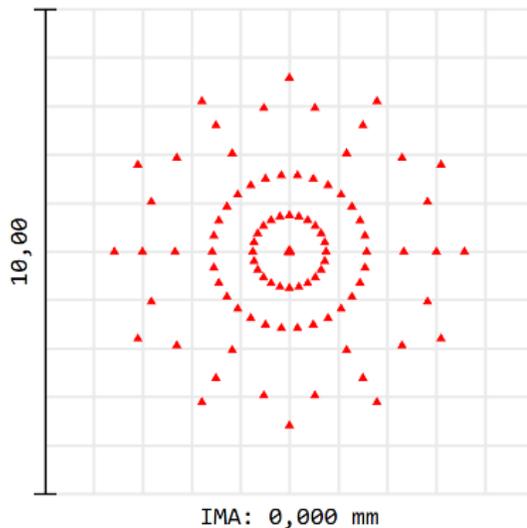
# Far View: Conformity of OpticStudio Import

Far View Scenario

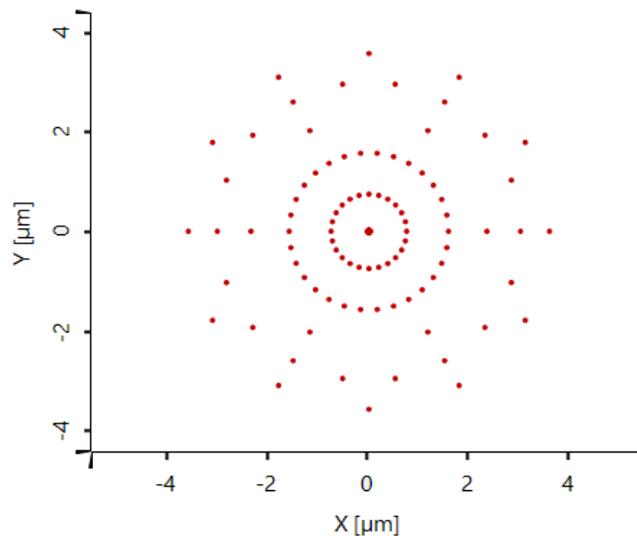


spot diagram of central wavelength (555 nm) calculated by:

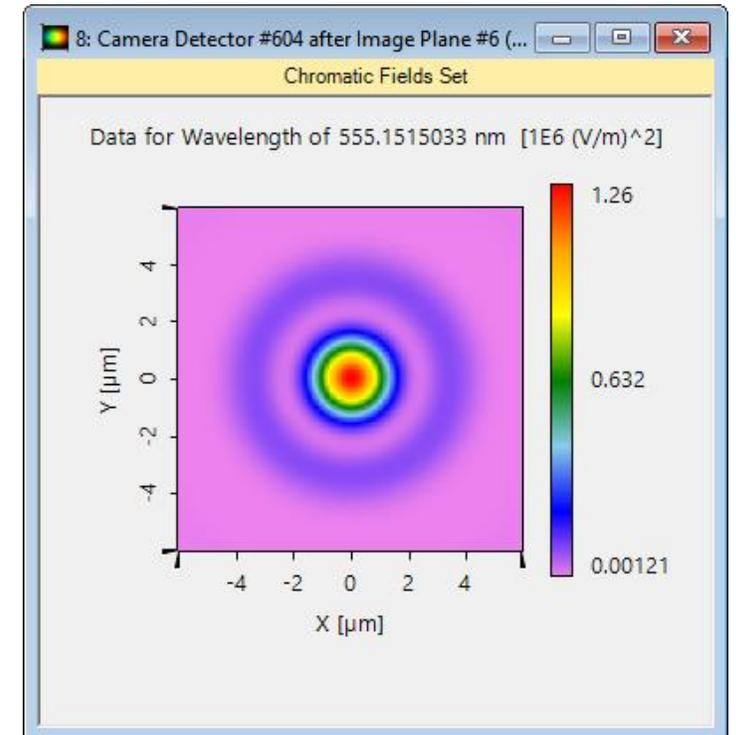
**OpticStudio**



**VirtualLab Fusion**

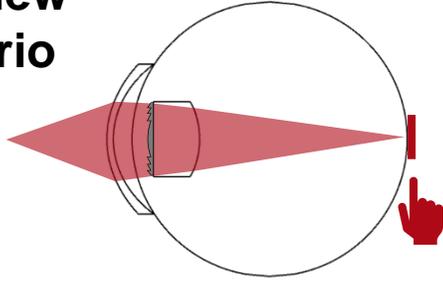


PSF calculation with the wavefront surface response by **VirtualLab Fusion**



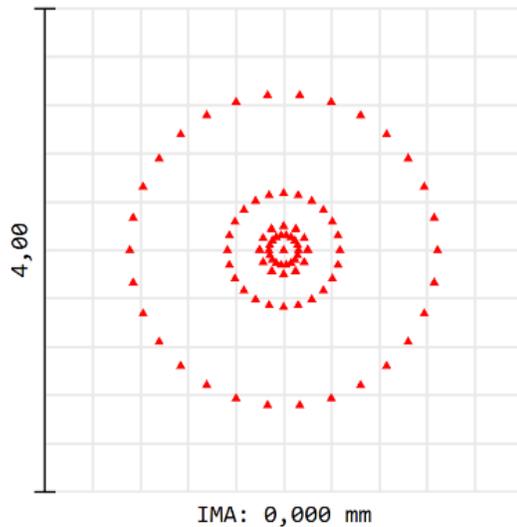
# Near View: Conformity of OpticStudio Import

Near View Scenario

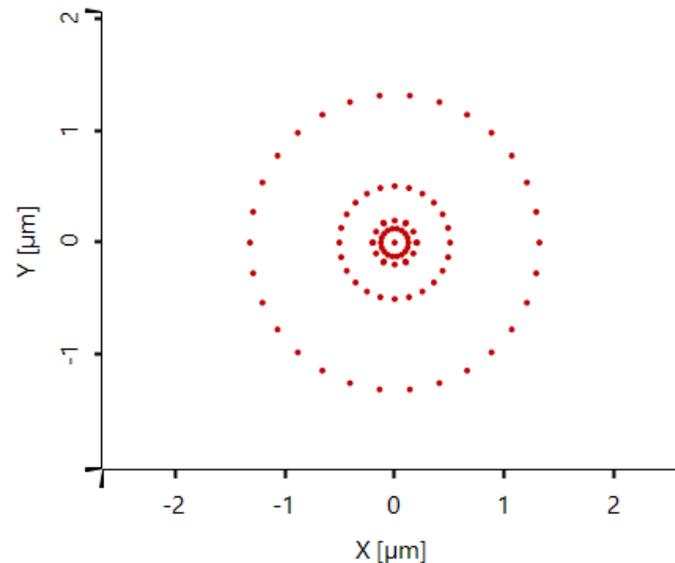


spot diagram of central wavelength (555 nm) calculated by:

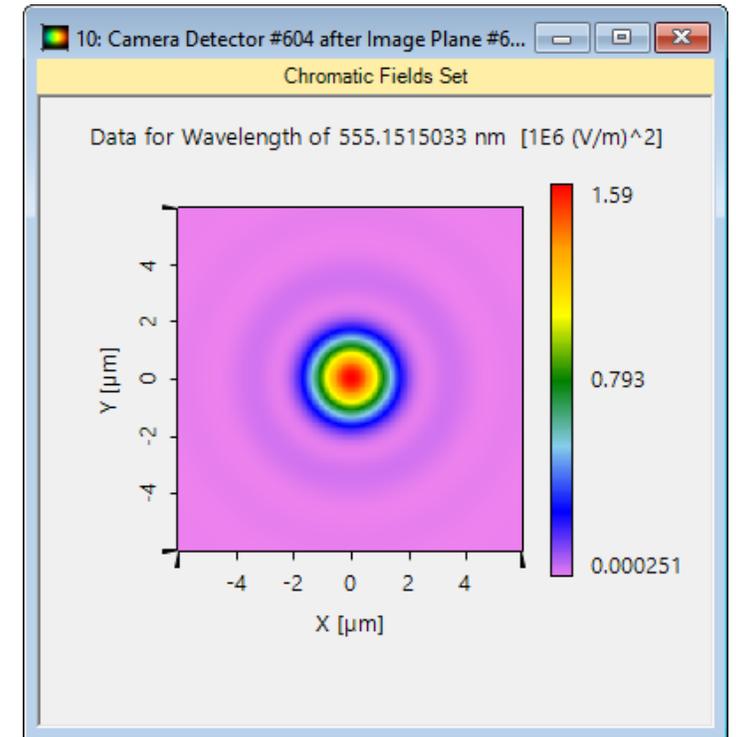
**OpticStudio**



**VirtualLab Fusion**



PSF calculation with the wavefront surface response by **VirtualLab Fusion**



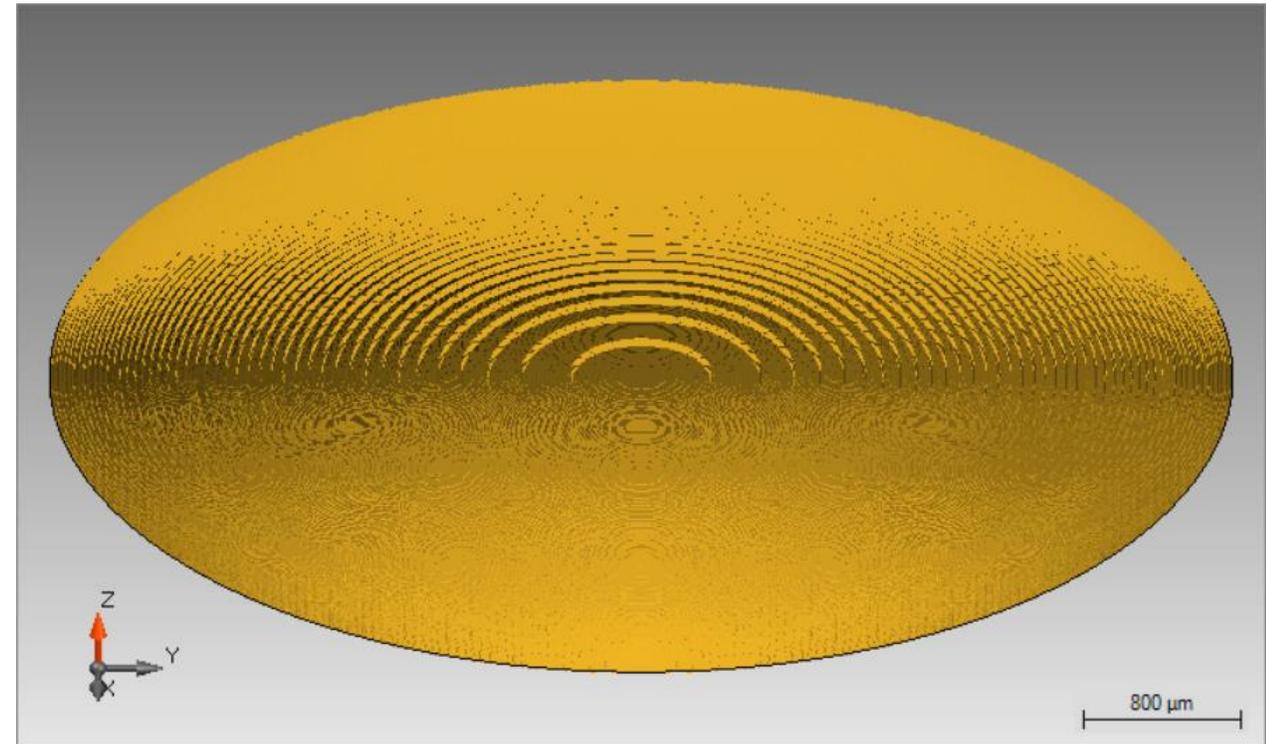
# Structure Design: Diffractive Lens Profile Height

- The structure profile of the diffractive lens is calculated by Thin Element Approximation (TEA) according to the wavefront surface response:

$$h^{\text{DOE}}(\rho) = \beta \frac{\lambda}{2\pi \Delta n} \Delta\psi(\rho)^{\text{DOE}}$$

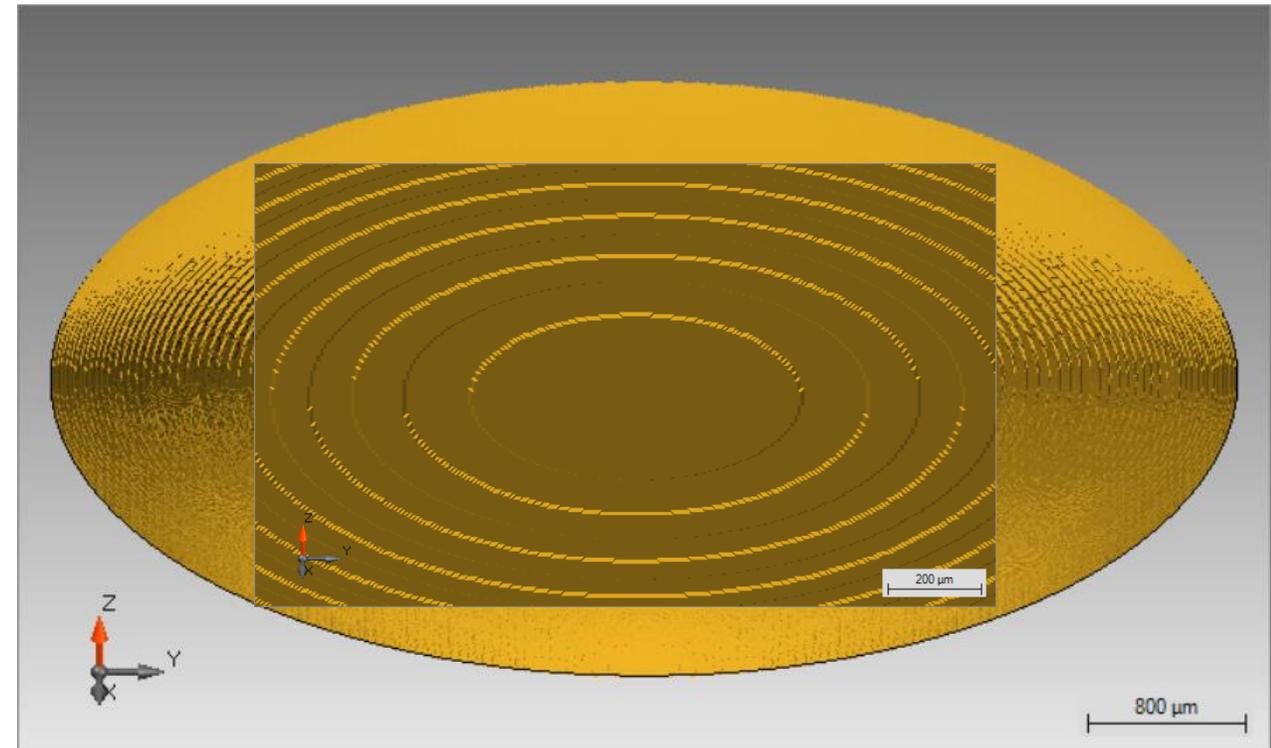
with a scaling factor  $\beta$  to modulate the height and control the efficiency of the diffraction orders

TEA provides directly a very high efficiency for the 1<sup>st</sup> order



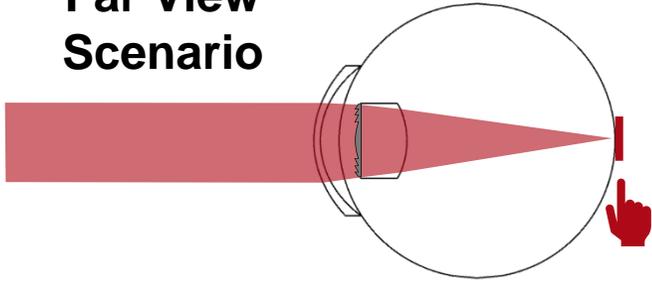
# Structure Design: Diffractive Lens Profile Height

- A quantization of the structure with 2 height levels is chosen because the binary diffractive lens
  - is beneficial for manufacturing (cost, easier to fabricate)
  - gives a better control of the efficiencies especially for the 0<sup>th</sup> and 1<sup>st</sup> order using the height modulation approach

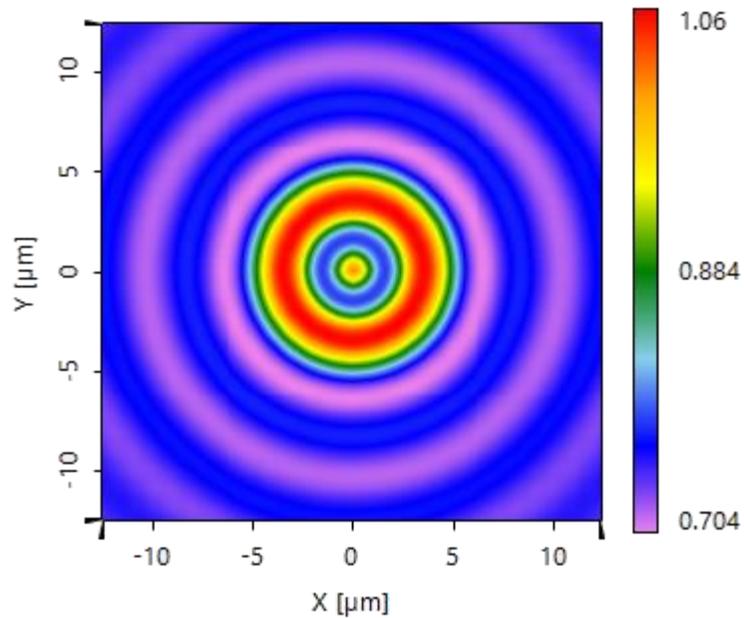


# Structure Design: Height Modulation of 1.00

Far View Scenario

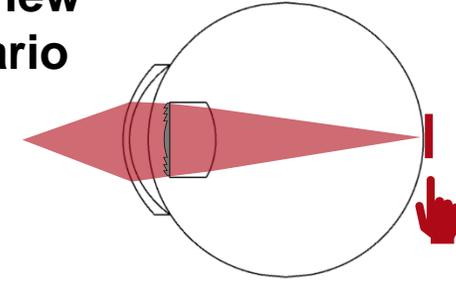


$\propto$  Electric Energy Density [1E2](V/m)<sup>2</sup>

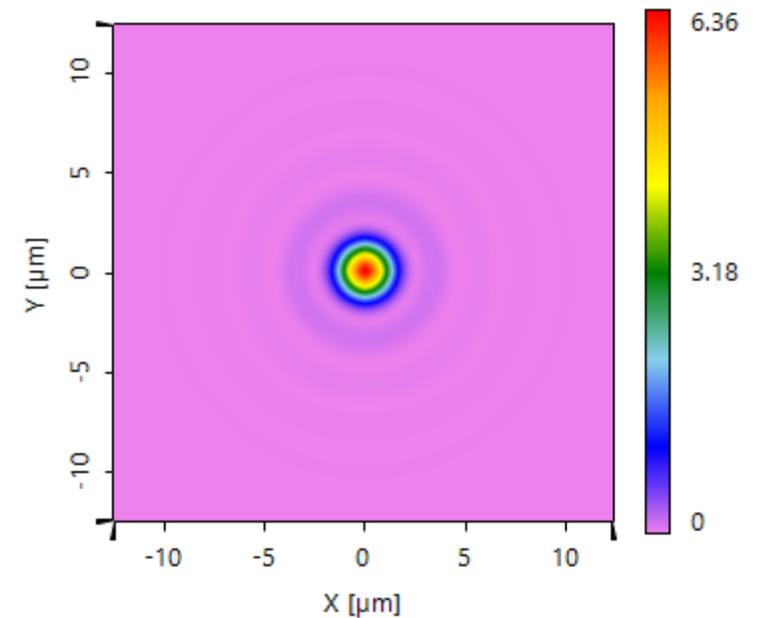


scaling of modulation height by  $\beta = 1.00$

Near View Scenario

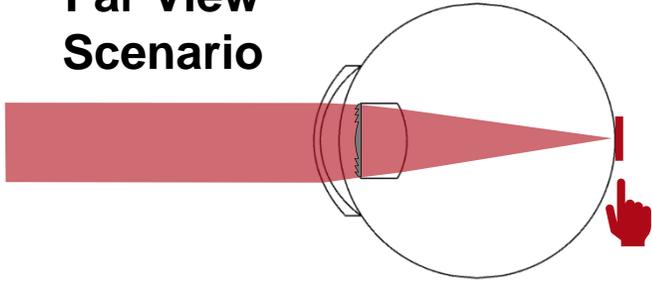


$\propto$  Electric Energy Density [1E5](V/m)<sup>2</sup>

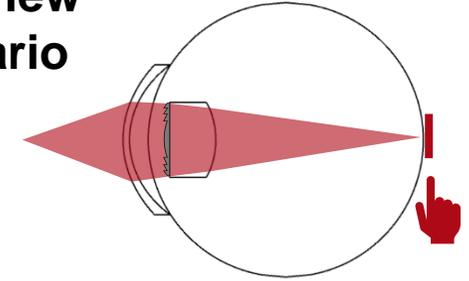


# Structure Design: Height Modulation of 0.95

Far View Scenario

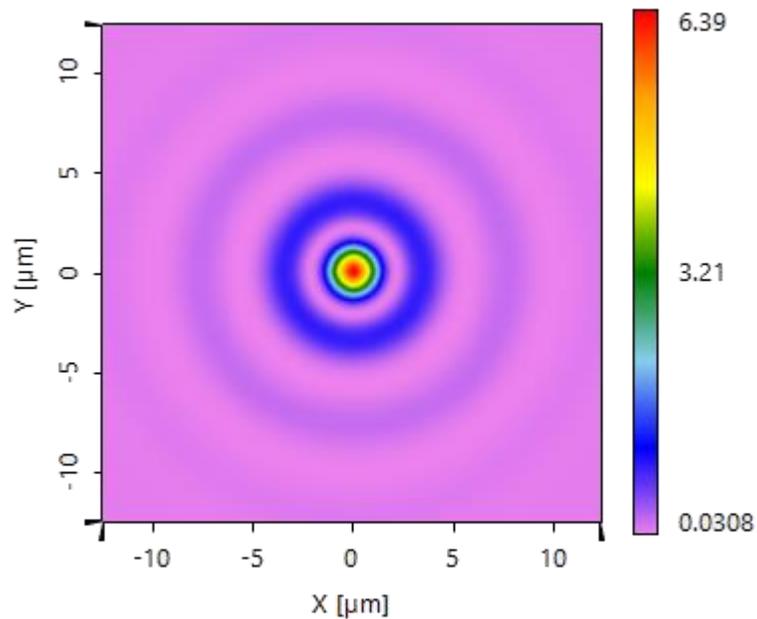


Near View Scenario

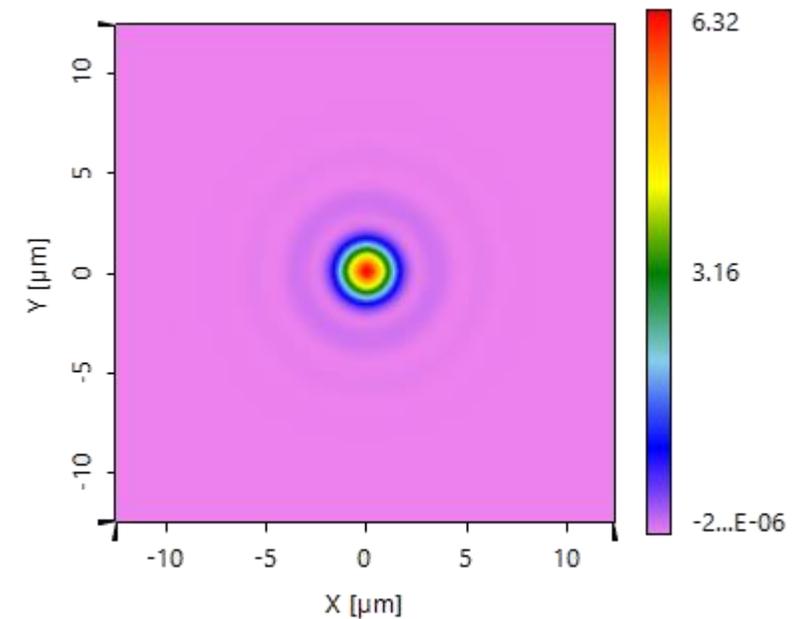


scaling of modulation height by  $\beta = 0.95$

$\propto$  Electric Energy Density  $[1E3(V/m)^2]$

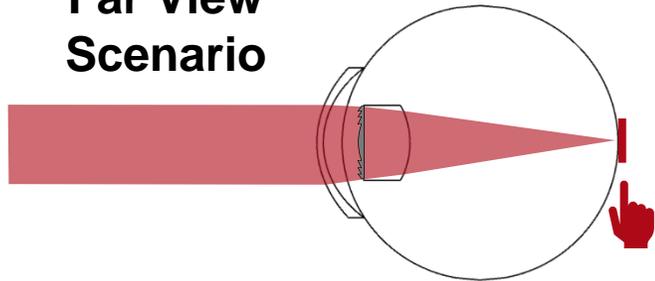


$\propto$  Electric Energy Density  $[1E5(V/m)^2]$



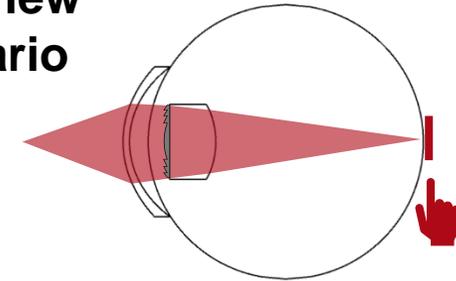
# Structure Design: Height Modulation of 0.90

Far View Scenario

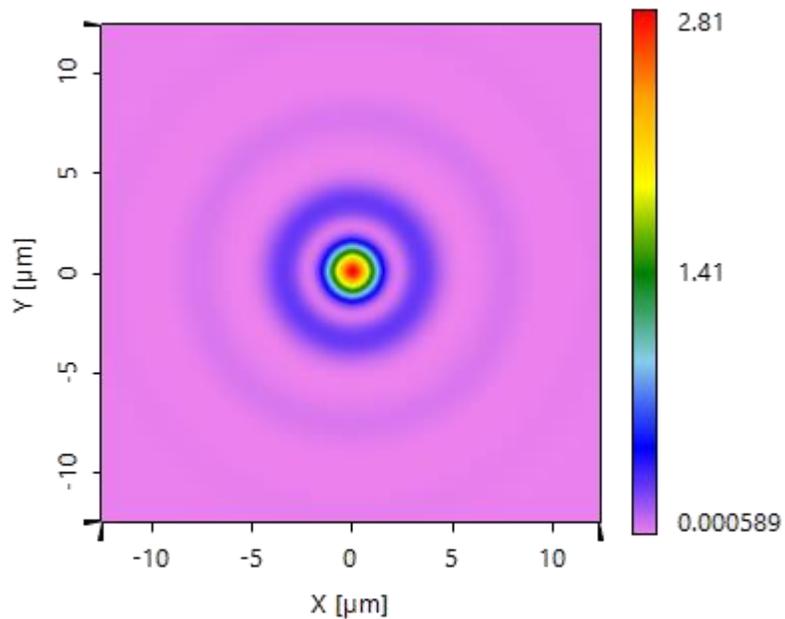


scaling of modulation height by  
 $\beta = 0.90$

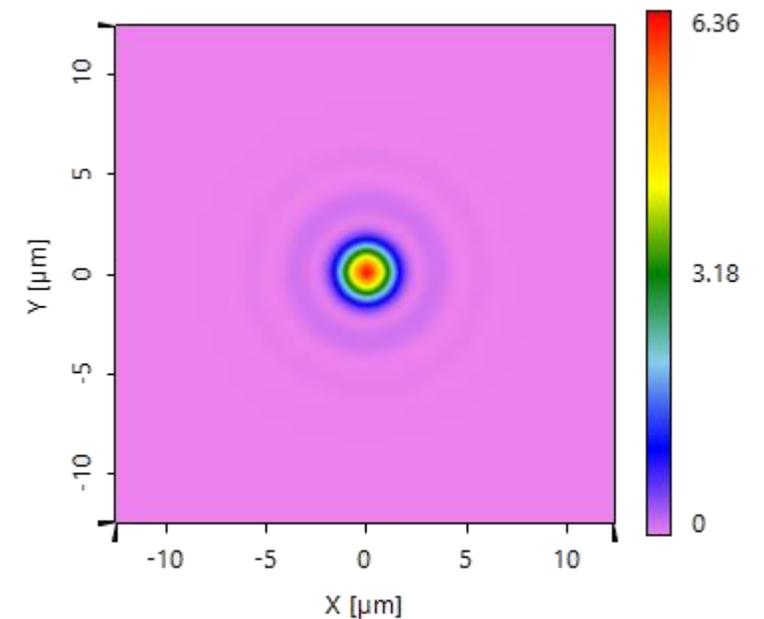
Near View Scenario



$\propto$  Electric Energy Density [ $1E4(V/m)^2$ ]



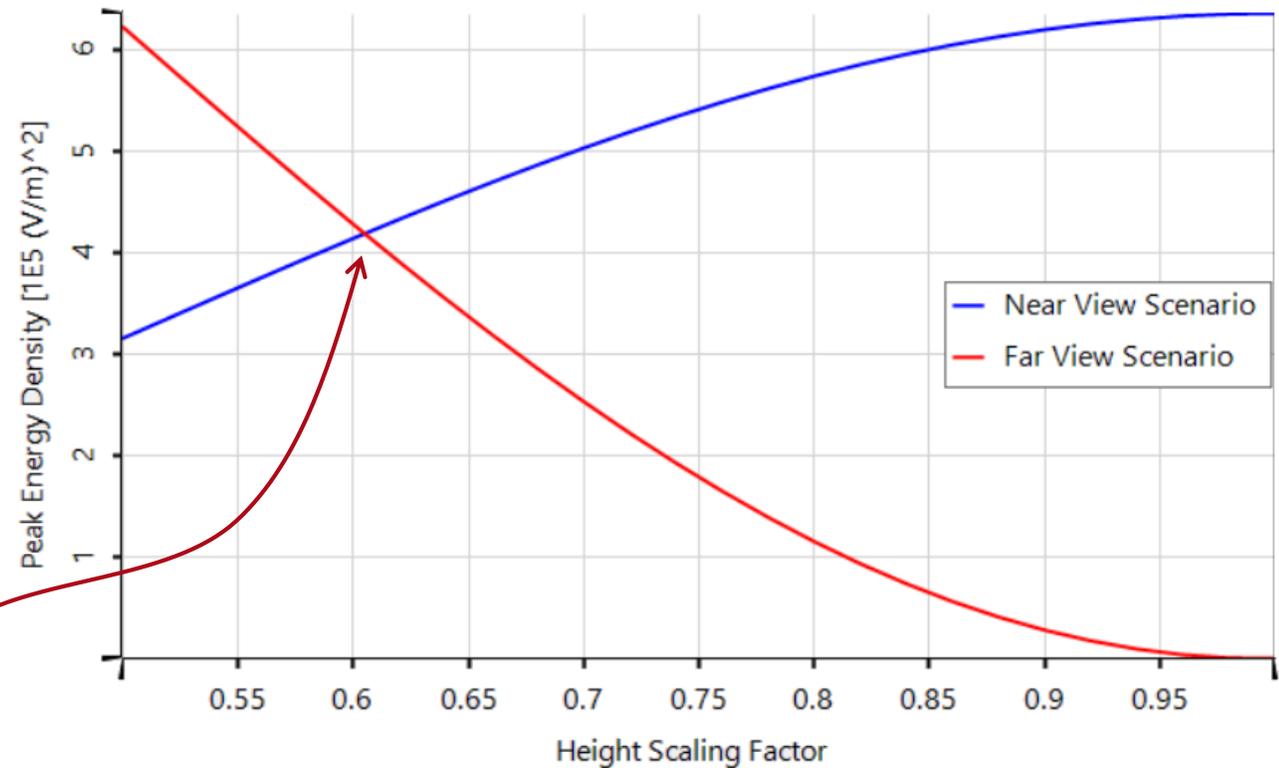
$\propto$  Electric Energy Density [ $1E5(V/m)^2$ ]



# Structure Design: Find the Optimum Scaling Factor

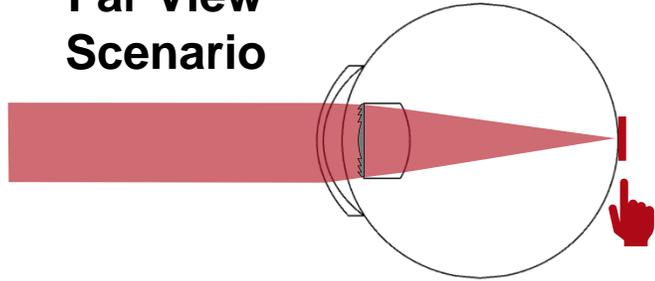
- As a goal, the peak energy density of the foci for both far view and near view scenario shall be the same.
- Therefore, the peak energy density is calculated with respect to the height scaling factor for both scenarios.

Optimum of the scaling factor for equivalent peak energy density for both foci (near and far view)

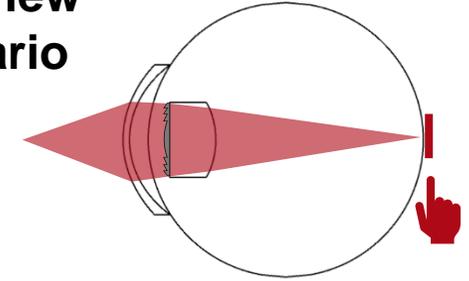


# Structure Design: Optimum Height Modulation of 0.605

Far View Scenario

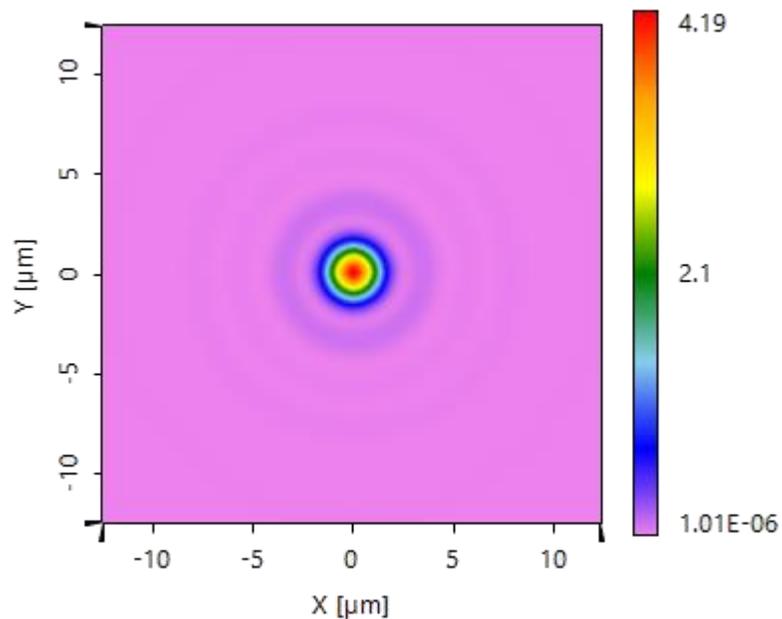


Near View Scenario

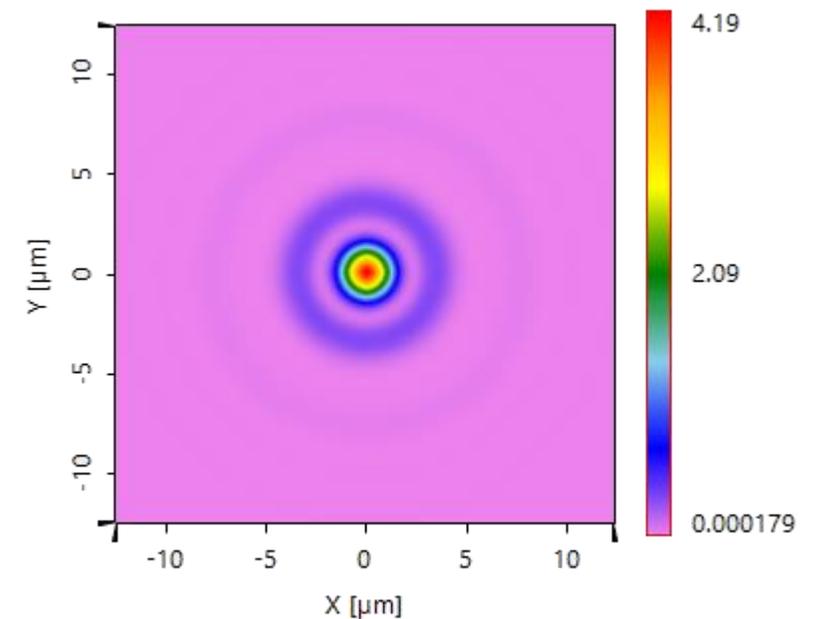


scaling of modulation height by  
 $\beta = 0.605$

$\propto$  Electric Energy Density  $[1E5](V/m)^2]$



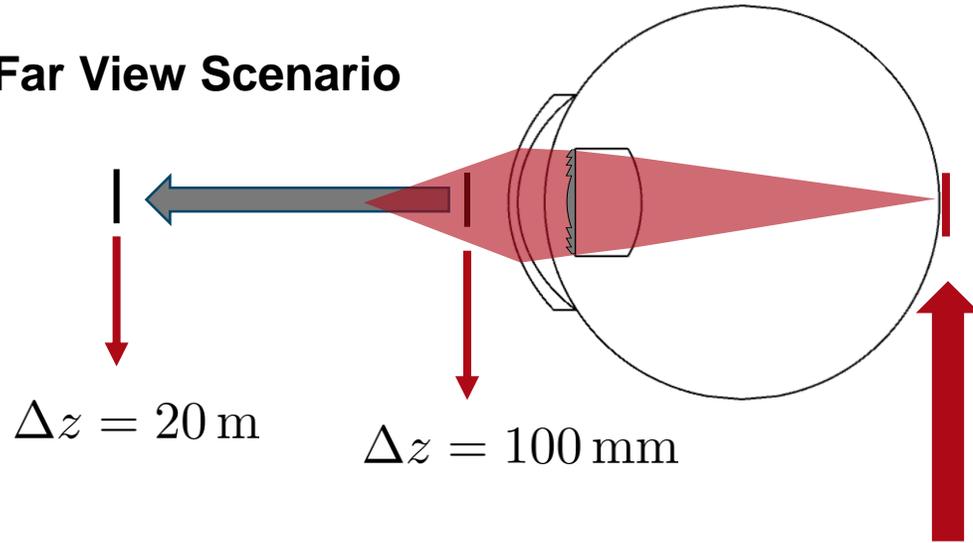
$\propto$  Electric Energy Density  $[1E5](V/m)^2]$



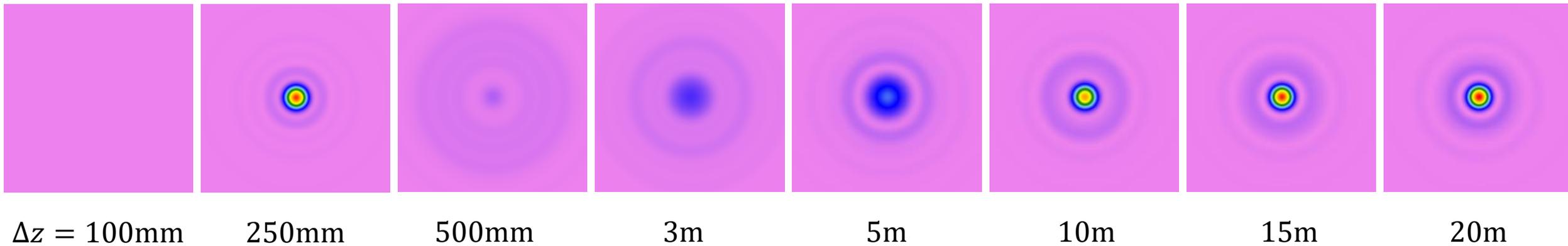
Goal of equivalent maximum energy density for both foci achieved!

# Illustration of Focus Development from Near to Far Region

Near to Far View Scenario

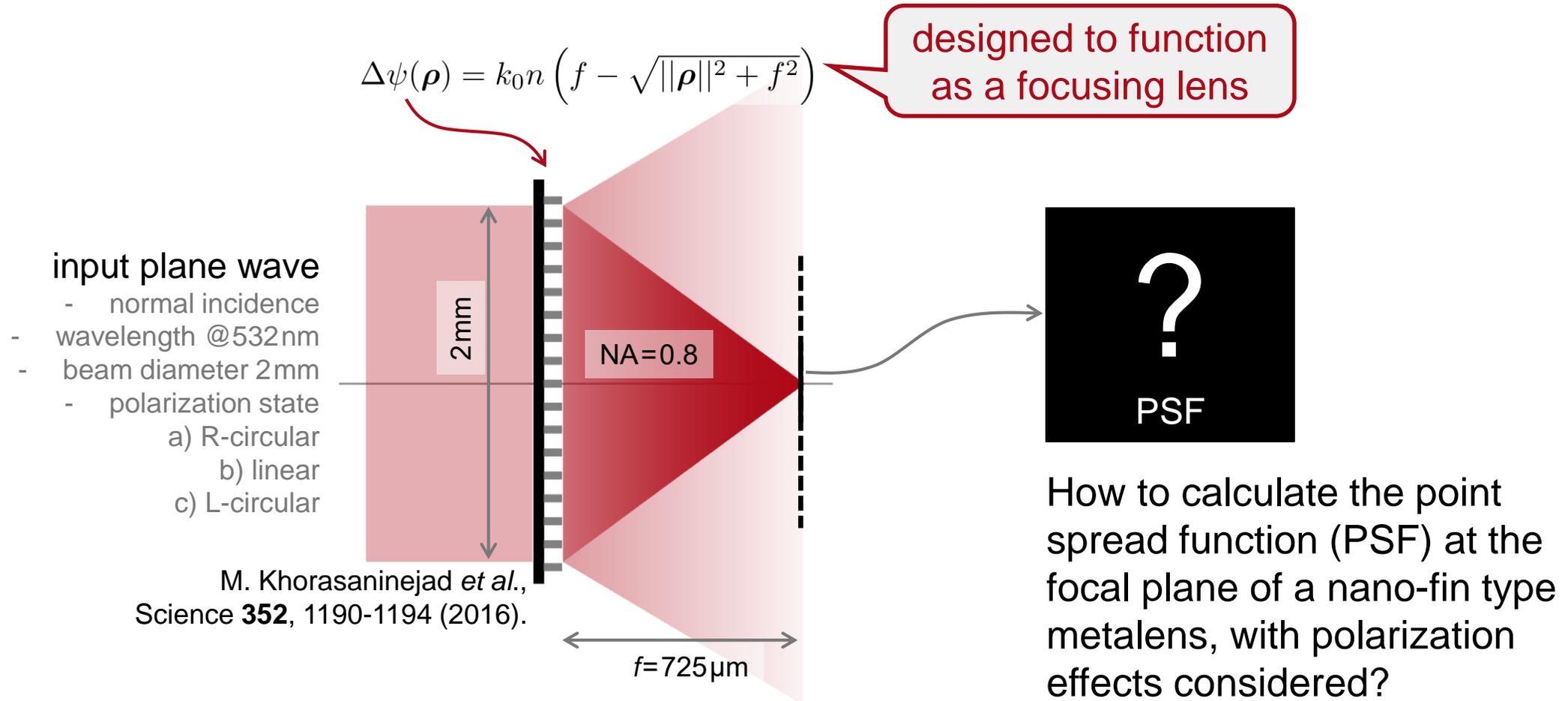


Focus spots with different object positions

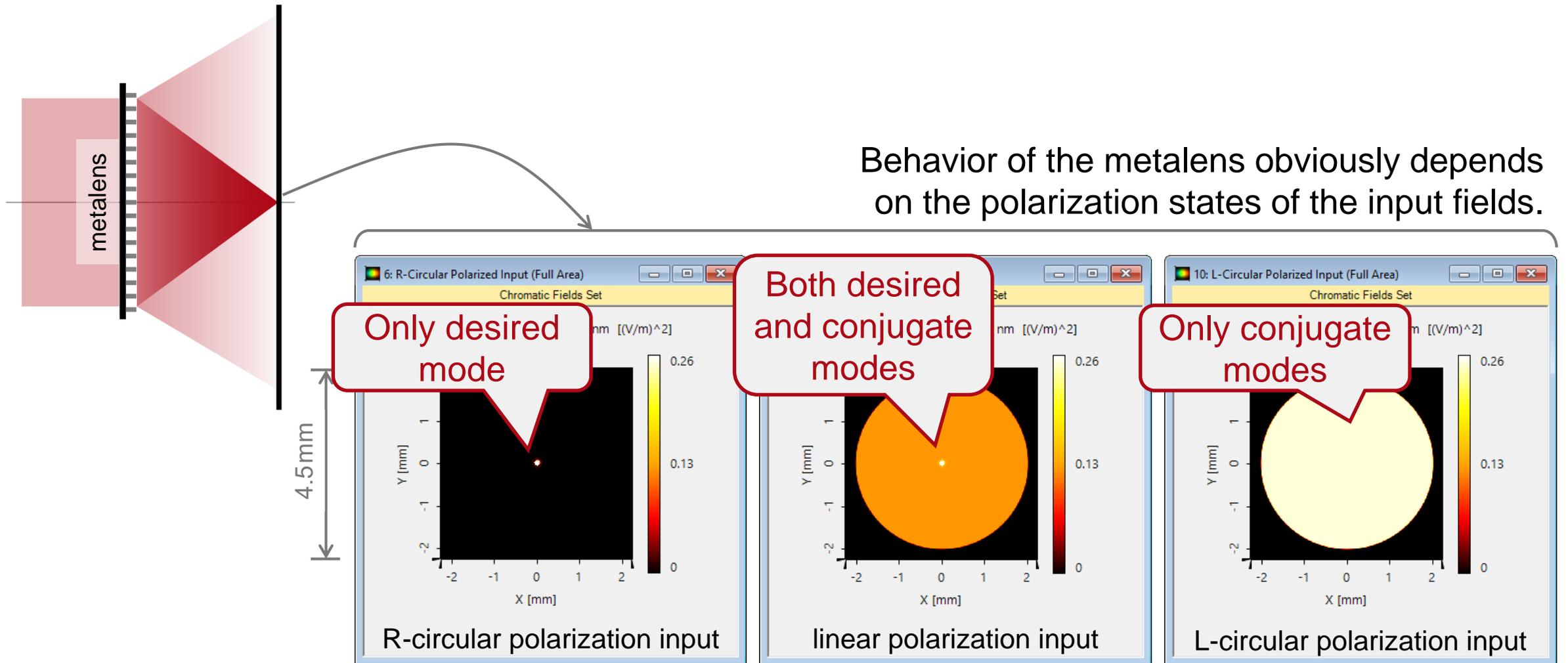


# Modeling of a Metalens Singlet Based on Half-Wave Plate Model

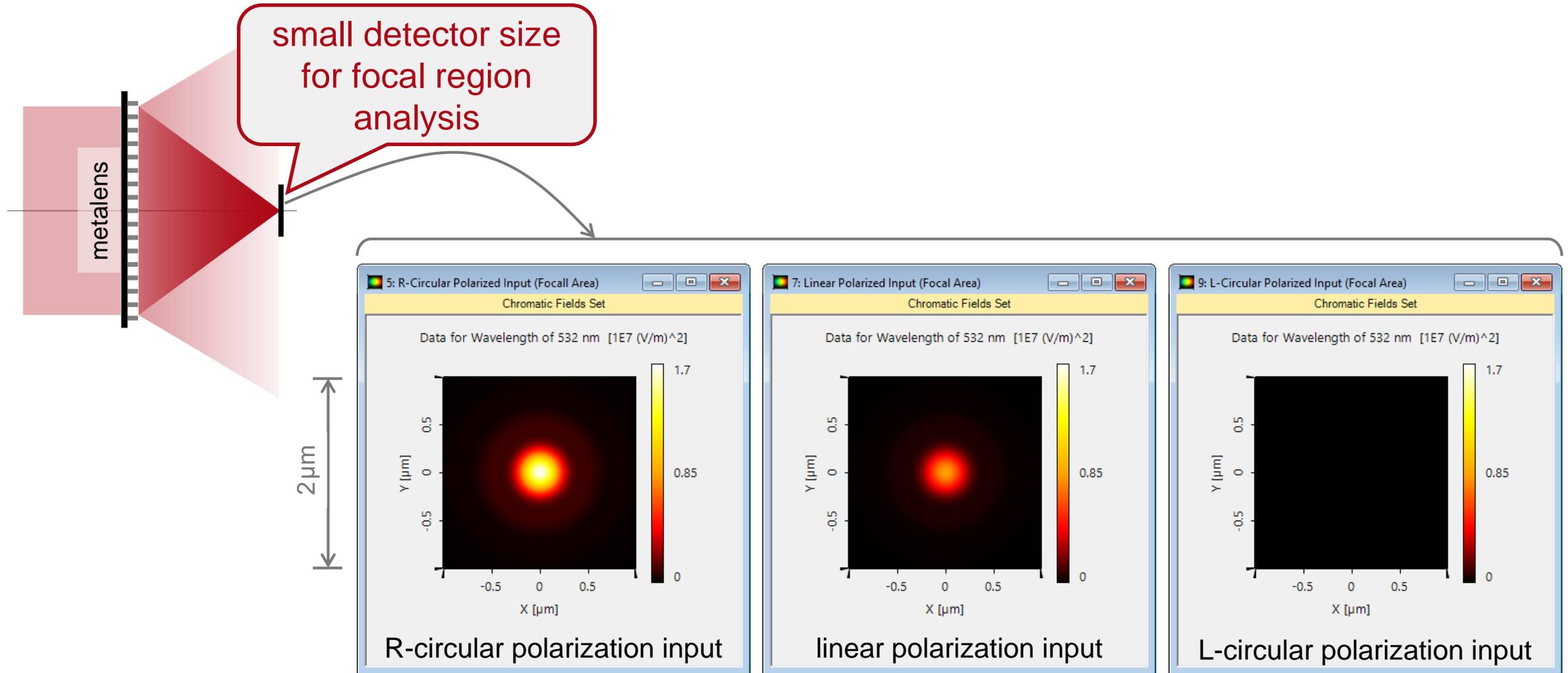
# Modeling Task



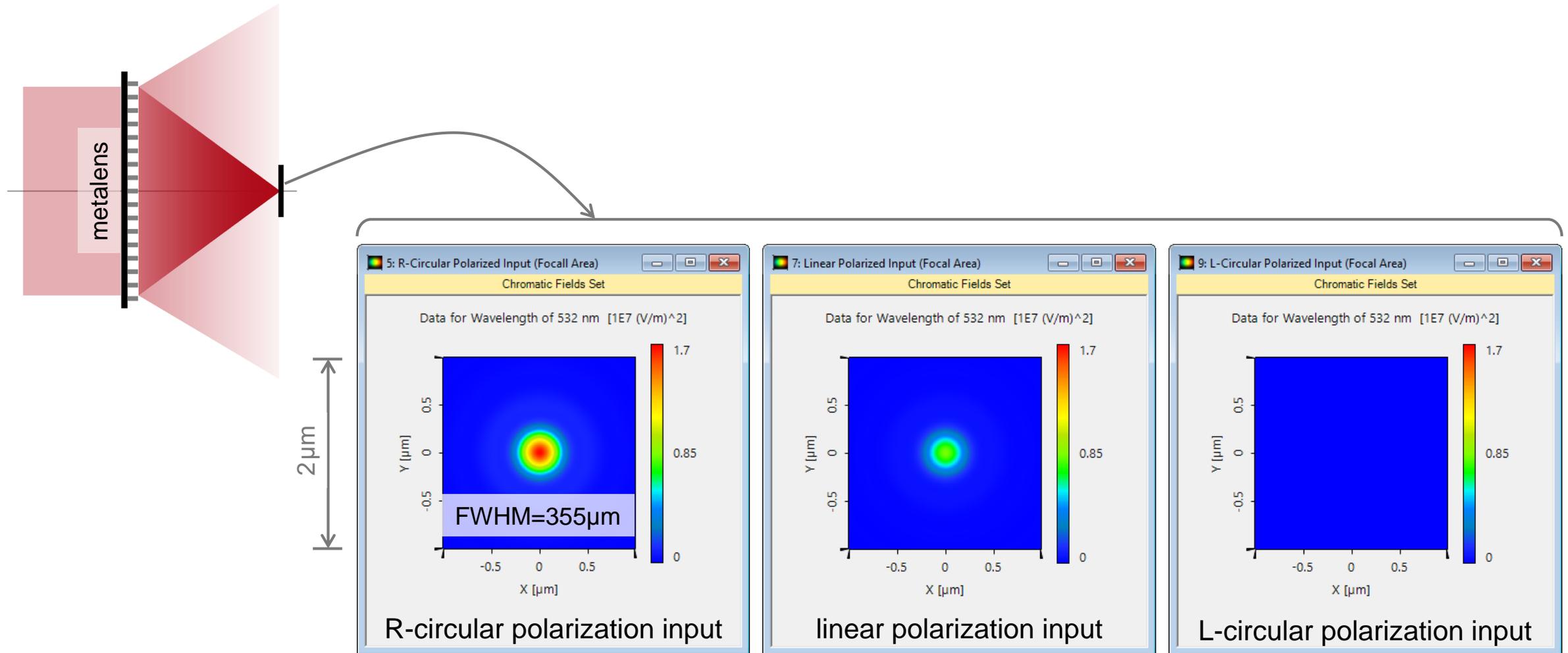
# Simulation Results on Whole Detector Plane



# Focal Area Analysis

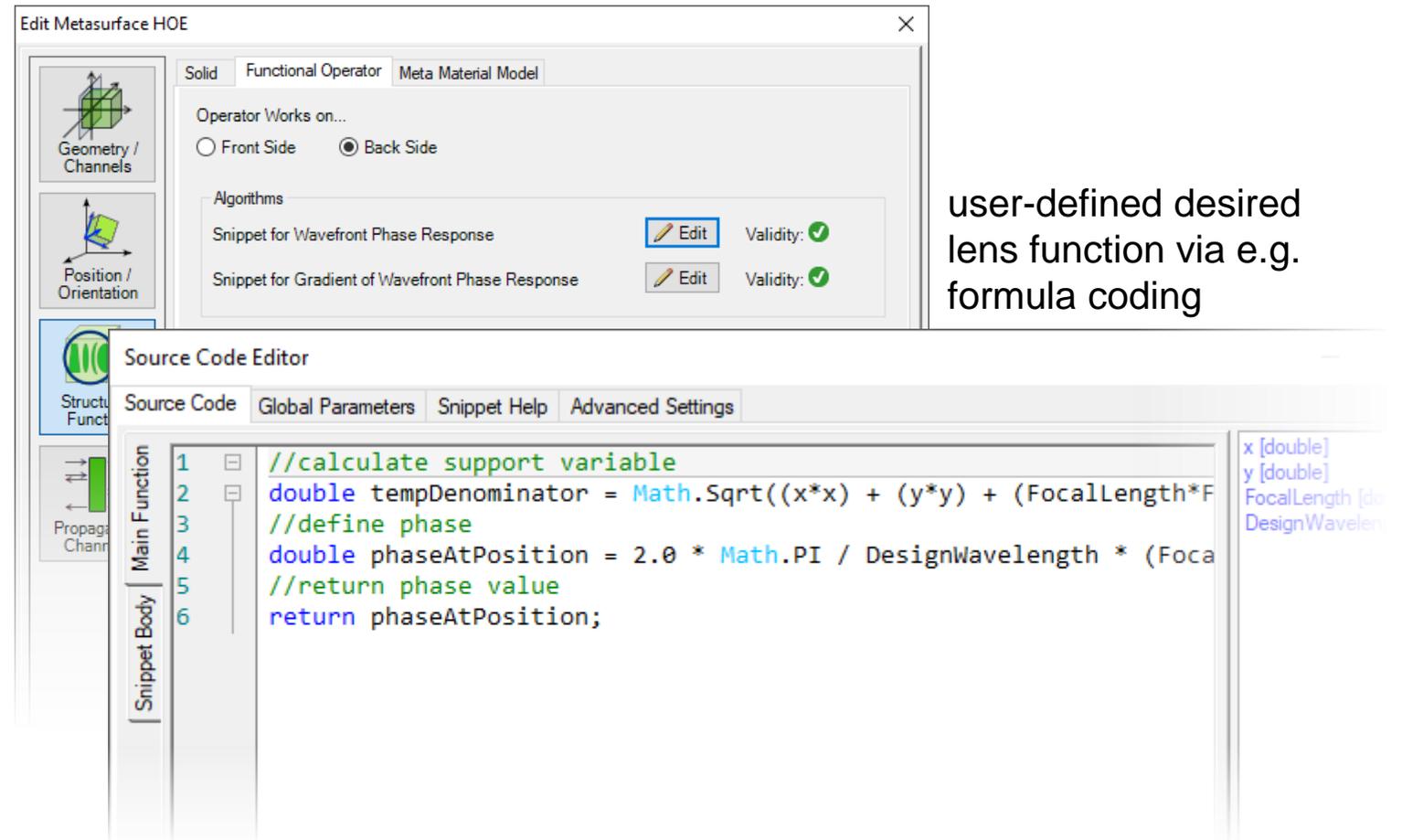
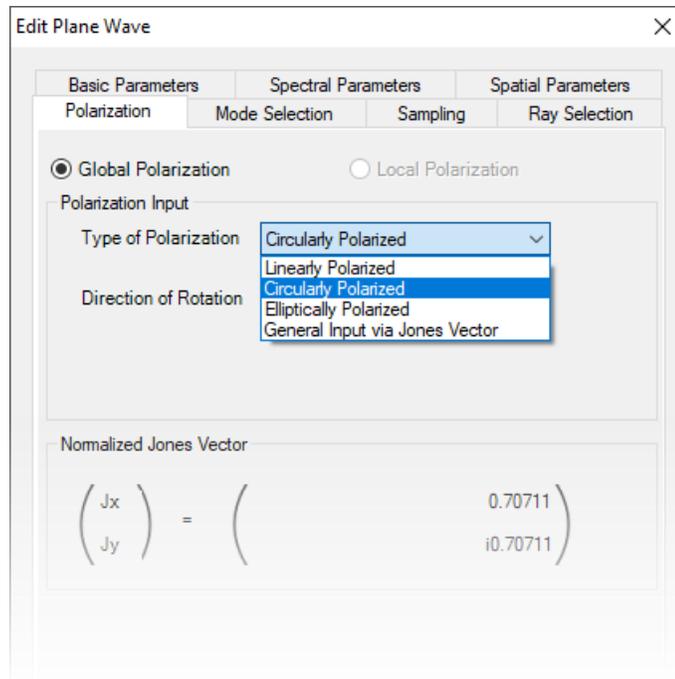


# Focal Area Analysis



# Peek into VirtualLab Fusion

polarization definition via pre-defined or customized Jones vectors



user-defined desired lens function via e.g. formula coding

# VirtualLab Fusion – Summer Release 2019

<p><b>Microstructure Components Modeling</b></p> <ul style="list-style-type: none"><li>▪ Modeling of microstructure components beyond paraxial situation</li><li>▪ Combined use with general input field</li><li>▪ Typical use for diffractive diffuser system modeling</li></ul>	<p><b>Diffractive Lens</b></p> <ul style="list-style-type: none"><li>▪ Complementary workflow with Zemax OpticStudio</li><li>▪ Direct import of e. g. Binary 2 surface</li><li>▪ Modeling based on real diffractive lens surface structures</li><li>▪ Export for fabrication</li></ul>	<p><b>Coming in 2019</b></p> <p><b>Metalens</b></p> <ul style="list-style-type: none"><li>▪ Unified software platform with both rigorous analysis of nano structures, and also whole lens modeling</li><li>▪ Rigorous Fourier modal method (FMM) for unit cell modeling with friendly structure configuration</li></ul>	<p><b>Integral Method for Grating Modeling</b></p> <ul style="list-style-type: none"><li>▪ In-built model for rectangular/slanted gratings with rounded edges</li><li>▪ Faster convergence than other techniques</li><li>▪ Suitable for fabrication tolerance analysis</li></ul>	<p><b>Grating Components in General Optical Setup</b></p> <ul style="list-style-type: none"><li>▪ Rigorous modeling based on in-built Fourier modal method (FMM/RCWA)</li><li>▪ Use together with other components in general optical setups</li><li>▪ Arbitrary orientation</li></ul>	<p><b>Simulation Engine Improvement</b></p> <ul style="list-style-type: none"><li>▪ Automatized sampling algorithm for free-space propagation</li><li>▪ Robust handling of aberrated wavefront phases</li><li>▪ Unified algorithm for propagation between tilted planes as well</li></ul>
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... and more at our booth

**Hall B1, 209**