

# Phase Mask [Stitching-Error]

## Digital Twin Specification

<b>Twin Code:</b>	CF-PMST01
<b>Twin Name:</b>	Phase Mask [Stitching-Error]
<b>Category:</b>	Component
<b>Type:</b>	Function-Based
<b>Version:</b>	1.0
<b>Package:</b>	Grating Package
<b>Last Updated:</b>	2026-03-19

## Description

The fabrication of a linear grating with period  $d$  can be affected by positional errors when writing successive grating rows. This results in stripes of height  $h$  with slight horizontal displacements, described by a stitching error parameter  $s$ , where  $-s_{\max} \leq s \leq +s_{\max}$ . The Stitching-Error Phase Mask is positioned directly behind a nominal grating component (without stitching error) to model this effect, as illustrated in Fig. 1.

## Simulation Model

The simulation model is based on the detour phase principle[1, 2]. A horizontal displacement  $s$  of a grating stripe results in a constant phase shift in its response. This detour phase  $\phi_s$  is given by

$$\phi_s = \frac{2\pi s}{d}. \quad (1)$$

The incident field from the grating is decomposed according to the stripe structure of height  $h$ . Each subfield is then assigned a random stitching error  $s$  (drawn uniformly from the range  $-s_{\max} \leq s \leq +s_{\max}$ ), and the corresponding detour phase  $\phi_s$  is applied, thereby simulating the stitching error.

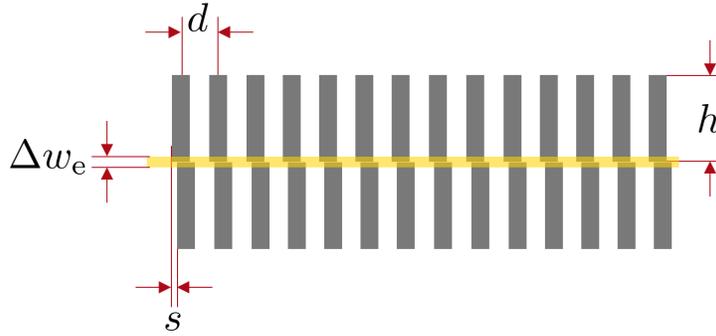


Figure 1: Illustration of parameters for simulating stitching errors in grating fabrication.

In VirtualLab Fusion, the field decomposition uses smooth edges of width  $\Delta w_e$  between subfields. This ensures proper numerical sampling and allows control over the physical sharpness of the edges to accurately model diffraction effects.

## Model Parameters

- **Period:**  $d$  of the linear grating.
- **Height:**  $h$  of the grating rows (without stitching error).
- **Maximum Stitching Error:**  $s_{\max}$ , expressed in meters ( $[s_{\max}] = \text{m}$ ).
- **Beam Diameter:**  $D$  of the incident beam; this information is used for proper field decomposition.
- **Seed:**  $a \in \mathbb{Z}$  determines the random number generation for the stitching error distribution.
  - $a > 0$ : A single, initially generated random distribution is reused for all simulations, ensuring reproducibility.
  - $a < 0$ : A new random distribution is generated for each simulation run.
- **Edge Width:**  $\Delta w_e$ , specified as a percentage of  $h$  (default:  $\Delta w_e = 5\%$ ).

## Channel Information

The digital twin is function-based and defined on a single plane. Light can strike the plane from either side and be either transmitted or reflected. Consequently, four channels must be specified:

**Channel +/+** In this channel, the intended functionality is provided.

**Channel +/-** Not activated.

**Channel -/-** This channel can be selected, but it does not alter the incident light.

**Channel -/+** Not activated.

## Recommended Usage

The stripe pattern with height  $h$  is aligned along the component's x-axis. By rotating the component relative to the grating, the stripes can be aligned orthogonally to the grating grooves.

The beam diameter can be initially determined by the Beam Size Detector. Select a larger beam size if you are unsure about the actual beam size.

The edge width  $\Delta w_e$  is given as a percentage of the height  $h$ . Reducing  $\Delta w_e$  allows for more accurate modeling of diffraction effects in the y-direction but requires a higher spatial sampling rate, which increases computational cost. For faster simulations, the edge width can be increased. Adjust this parameter carefully to balance accuracy and performance.

## References

- [1] A. Lohmann and B. P. Paris. "Binary Fraunhofer holograms generated by computer". In: *Appl. Opt.* 6.10 (1967), pp. 1739–1748.
- [2] J. Bucklew and N. C. Gallagher Jr. "Comprehensive error models and a comparative study of some detour-phase holograms". In: *Appl. Opt.* 18.16 (1979), pp. 2861–2869.

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**Related Twins:** CF-PHMC01, CF-PHMV01, CF-PPUD01, CS-GRRO01